

# The LITTLUN S-box and the FLY block cipher

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## Abstract

We present the construction and implementation of an 8-bit S-box with a differential and linear branch number of 3. We show an application by designing FLY, a simple block cipher based on bitsliced evaluations of the S-box and bit rotations that targets the same platforms as PRIDE, and which can be seen as a variant of PRESENT with 8-bit S-boxes. The round function of FLY achieves the same performance as the one of PRIDE on 8-bit microcontrollers (in terms of number of instructions per round and code size) while having 1.5 times more equivalent active S-boxes on average. The S-box also has an efficient implementation with SIMD instructions, a low implementation cost in hardware and it can be masked efficiently thanks to its sparing use of non-linear gates and to the fact that it has a natural expression in terms of a single 4-bit S-box.

**Keywords.** Block cipher design, Lai-Massey S-box, bitsliced implementation, SPN.

## 1 Introduction

Since the late 1990’s and the end of the AES competition, the academic community and the industry have been provided with excellent block ciphers. In most cases where a cipher is needed, AES [32] can readily be used and there is currently little need for a replacement. Consequently, the symmetric cryptographic community shifted focus to *e.g.* the wider picture of *authenticated encryption* through the CAESAR competition, or to more specific applications of block ciphers. In the latter case, an important topic is the design of “lightweight” block ciphers intended to be implemented on low-cost, resource-constraint devices. An early successful example following this trend is the block cipher PRESENT [10], which can be implemented in small hardware circuits. Most lightweight algorithms similarly target one (or a few) platform(s) on which they are expected to perform particularly well; good performance in other cases are however not usually expected and lightweight ciphers are in general not very versatile. Typical platforms of interest include hardware circuits and 8-bit to 32-bit microcontrollers.

In this work, we design a conceptually simple block cipher targeting efficient *light* implementations on 8-bit microcontrollers<sup>1</sup>. The chief academic proposal to date for this scenario is the PRIDE block cipher<sup>2</sup>, that was presented at CRYPTO 2014 [1]. Our block cipher is built around LITTLUN-1, a compact 8-bit S-box with branch number 3. This allows to define a round function similar to a scaled-up variant of PRESENT, composing the S-box application with a simple bit permutation<sup>3</sup>. This offers a trade-off between hardware and light software implementations: LITTLUN-1 is more expensive in hardware than (two applications of) the S-box of PRESENT, but the bit permutation is simple to implement with 8-bit rotations. Owing to Golding, we name our block cipher “FLY”.

Excluding on-the-fly key expansion, the round function of FLY costs 4 instructions less to implement than PRIDE’s on AVR. Using the good branch number of LITTLUN-1, we can show that with a similar number of rounds, FLY is more resistant than PRIDE to statistical (differential and linear) attacks. This is all the more relevant as the security margin of PRIDE seems to be quite thin [39]. Taking the key-schedule into account, one round of FLY costs 8 more instructions than one round of PRIDE. However, unlike PRIDE, we do not use an FX construction for the key-schedule and thus the generic

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<sup>1</sup>By *light* implementations, we mean in particular that the size of the code is small, typically of the order of 200 bytes. If more resources are available, the best current block cipher is probably the AES (see *e.g.* [7]).

<sup>2</sup>Notable “non-academic” ciphers for the same scenario are the “NSA ciphers” SIMON and SPECK [6].

<sup>3</sup>As a bit permutation obviously does not increase the number of active bits, an important part of the diffusion in such a cipher is played by the S-box. The typical measure of the quality of the diffusion of an S-box is its “branch number” which plays a role similar to the minimum distance of the linear codes used in AES-like designs.

security of FLY does not decrease with the amount of data available to the adversary (Dinur also showed how the FX construction can lead to more efficient time-memory-data trade-offs [23]).

As implementations on resource-constraint devices are more likely to be vulnerable to side-channel attacks, one should also consider the additional cost of protection against, say, differential power analysis when evaluating schemes that target such platforms. In that respect, the small number of gates necessary to implement the LITTLUN-1 S-box, as well as its simple expression in terms of light 4-bit S-boxes allows one to produce masked implementations of FLY with limited overhead.

**Related work.** The block cipher literature is so numerous that most new proposal will bear some similarity with past designs. In that respect, apart from PRESENT, FLY is quite similar to RECTANGLE [38], which also combines a SERPENT-like bitsliced application of an S-box [8] with a rotation-implemented bit permutation. However, the S-box in RECTANGLE is on 4 bits, it does not have a branch number of 3 and the rotations are on 16-bit words. The construction of the LITTLUN S-box uses the Lai-Massey structure from the IDEA block cipher [29]; this structure was already used to build the second S-box of the WHIRLPOOL hash function [4] and the S-box of the block cipher FOX [27].

## 2 Preliminaries

We start by defining the main notions that will be used in evaluating the cryptographic properties of our construction. Although we will mostly consider S-boxes as defined over binary strings, we may see an  $n$ -bit S-box as a mapping  $\mathbf{F}_2^n \rightarrow \mathbf{F}_2^n$  whenever convenient.

**Definition 2.1** (Differential uniformity of an S-box). Let  $\mathcal{S}$  be an  $n$ -bit S-box. We define its *difference distribution table* (or DDT) as the function  $\delta_{\mathcal{S}}$  defined extensively by:

$$\delta_{\mathcal{S}}(a, b) := \#\{x \in \mathbf{F}_2^n \mid \mathcal{S}(x) + \mathcal{S}(x + a) = b\}.$$

The *differential uniformity*  $\Delta$  of  $\mathcal{S}$  is defined as:

$$\max_{(a,b) \neq (0,0)} \delta_{\mathcal{S}}(a, b).$$

Put another way, an  $n$ -bit S-box with differential uniformity  $\Delta$  has a maximal differential probability of  $\Delta/2^n$  over its inputs.

**Definition 2.2** (Linearity of an S-box). Let  $\mathcal{S}$  be an  $n$ -bit S-box. We define its *linear approximation table* (or LAT) as the function  $\mathcal{L}_{\mathcal{S}}$  defined extensively by:

$$\mathcal{L}_{\mathcal{S}}(a, b) := \sum_{x \in \mathbf{F}_2^n} (-1)^{\langle b, \mathcal{S}(x) \rangle + \langle a, x \rangle}.$$

The *linearity*  $\ell$  of  $\mathcal{S}$  is defined as:

$$\max_{(a,b) \neq (0,0)} |\mathcal{L}_{\mathcal{S}}(a, b)|.$$

Roughly speaking, the linearity measures the maximum (absolute) difference between how many times a (non-trivial) linear approximation takes the value 1 and how many times it takes the value 0. It is therefore twice the difference between  $2^{n-1}$  (for an  $n$ -bit S-box) and how many times either value is taken. In particular, if we define the *bias*  $b$  of a probability  $p$  as  $|p - 1/2|$ , it means that the bias of any linear approximation of an  $n$ -bit S-box of linearity  $\ell$  is upper-bounded by  $(\ell/2)/2^n$ .

**Definition 2.3** (Branch number of an S-box). The *differential branch number* of an S-box  $\mathcal{S}$  is:

$$\min_{\{(a,b) \neq (0,0) \mid \delta_{\mathcal{S}}(a,b) \neq 0\}} \text{wt}(a) + \text{wt}(b),$$

where  $\text{wt}(x)$  is the Hamming weight of  $x$ .

The *linear branch number* of an S-box  $\mathcal{S}$  is:

$$\min_{\{(a,b) \neq (0,0) \mid \mathcal{L}_{\mathcal{S}}(a,b) \neq 0\}} \text{wt}(a) + \text{wt}(b).$$

**Definition 2.4** (Algebraic normal form). Let  $f : \mathbf{F}_2^n \rightarrow \mathbf{F}_2$  be an  $n$ -bit Boolean function, its *algebraic normal form* (or ANF) is defined as the polynomial  $g \in \mathbf{F}_2[x_0, x_1, \dots, x_{n-1}] / \langle x_i^2 - x_i \rangle_{i < n}$  such that for all  $x \in \mathbf{F}_2^n$ ,  $f(x) = g(x[0], \dots, x[n-1])$ . Similarly, the ANF of an  $n$ -bit S-box  $\mathcal{S}$  is the sequence of the ANFs of its  $n$  constituent Boolean functions projected on the canonical basis of  $\mathbf{F}_2^n$ .



























