

#### **Frontiers of Characterization and Metrology for Nanoelectronics**



Purpose:

The Joth World Conference

While a city of notable art treasure, architecture also has largest hub of microelectronics in engineering (more than 2000 materia institutes).

The FCMN brings together scientists characterization technology needed for development, and manufacturing.

1998, 2000, 2001 and 2013 1998, 2000, 2001 and 2013

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Dresden and in several

The conference will consist of formal invition presentation sessions and poster sessions for contributed papers. The poster papers will cover new developments in characterization and metrology especially at the nanoscale.

#### The conference series began at NIST in 1995.

# **Welcome in Germany**

#### The country where the first metrology institute was founded





#### 2015 Frontiers of Characterization and Metrology for Nanoelectronics

April 14-16, 2015

**Tuesday, April 14 Conference Opening Keynote Talks** Session Chair: David Seiler, NIST inclination of information processing. New and improved metrology and characterization is required to 9:00 **Characterization Challenges In The 28 nm Technology Node** Hubert Lakner, Executive Director, Fraunhofer Institute for Photonic Microsystems 9:45 Wide Perspective on Today's Semiconductor Industry the semiconductor industry moves to silicon nanoelectronics and Suresh Venkatesan, Senior Vice President, Technology Development, Global Foundries 10:30 **Coffee Break and Poster Viewing** 11:00 **Nanoelectronics for Metrology** Klaus von Klitzing, Max-Planck-Institut FKF

#### 129 years ago

#### Lord Kelvin (William Thomson) 6.May 1886

... I often said that when you can measure what you are speaking about, and can express it in numbers, you know something about it.

...So therefore, if science is measurement, then without metrology there can be no science

#### "Science is Measurement" Henry Marks (1829 – 1898)



With this painting, Henry Marks became member of the Royal Academy, London



## Nanoscience: Dimension → Function







#### The Story of the Egyptian Cubit

It is believed that about 3,000 years B.C., the Egyptian unit of length was established. The Royal Egyptian Cubit was decreed to be equal to the length of the forearm from the bent elbow to the tip of the extended middle finger plus the width of the palm of the hand of the Pharoah ruling at that time. The Royal Cubit Master was carved from a block of black granite to endure for all time. Workers building tombs, temples and pyramids were supplied with cubit sticks made of wood or granite. The Royal Architect or foreman of each construction site was responsible for maintaining and transferring the unit of length to the workers' cubit sticks. It was required that the cubit sticks be brought at each full moon to be compared to the Royal Cubit Master. Failure to do so was punishable by death.

Though the punishment prescribed was severe, the ancient Egyptians had anticipated the spirit of the present day system of legal metrology, standards, traceability and calibration recall. With this standardization and uniformity of length, they achieved amazing accuracy. The Great Pyramid of Giza was constructed to stand roughly 756 feet or 9,069.4 inches. Using cubit sticks, the builders were within 4.5 inches — an accuracy of 0.05%.



stui a or with

This story of the Egyptian cubit was presented to Ed Nemeroff, NCSL Vice President - International Division by Professor, Dr. Mohamed El-Fiki, President of the Egyptian National Institute for Standards in commemoration of the United States – Egypt Bilderal Workshop on Metrology, Standards & Conformity Assessment Jointly sponsored by the United States National Institute of Standards and Technology and the Egyptian National Institute for Standards Alexandria, Egypt 1996

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#### **<u>GLOBAL</u>** UNITS USED TODAY:



#### International System of 7 Base Units

second for time **metre** for length **kilogram** for mass kelvin for temperature ampere for electric current candela for luminous intensity mole for the amount of substance



# **UNIVERSAL SET OF UNITS**

(established at the time of the French revolution)



22.8.1790: Working Group for an UNIVERSAL SET OF UNITS

#### Introduction of "Metric System" by French Academy of Science





#### 1799: Year of birth of Métre et Kilogramme "des Archives"



The metre is equal to one ten millionth part of the quarter of the terrestrial meridian

The kilogram is equal to the mass of a decimetre cube of water at the temperature of melting ice





#### Meter Convention 20.5.1875

#### **METRIC SYSTEM** 1111:11 on severalifice simont lis **Meter Kilogram Second** aluntions achaque clat ; ichangicon Paris dans le delai Son Excellence le Vin sede Prine se prut Colli sona mise signed by 17 countries Francaise, Sa Majos 10 yanmer 11/6. to Himpolentiamorespectifi Sa Majoste l'anjuntar a Mutuch Sa Majiste le Roi des Belges, Sa, Majesté Contrigner chyon apposile rachet de laura Vimperior du Busil, Son Excellence le Wille Juit à Paris; le 20 Mai 1813. 1. Prisident de la Confideration Argentine Sa Majeste le Roi de Danemark, Sa Majeste he Roid bapagne, Son Excellence le Beranel Prisident des Clats Unis d'amerique, Sa P. D. Moneyor Majeste le Roi d'Italie, Sen Excellence allaman le Risident de la Republique du Prione, Sa Majeste le Roi de Portugal es des Alganes, Sa Majeste l'Impereur des tontes les Kussies, Sa Majeste le nei de Suide es de norvege, Son Excellence les Mohentoke Prisident de la Confederation Suisse, Sa Majeste l'hmpiereur des Ollomanico es Son Breellince le Resident delo Republique de Veneruilar desirant afsurer l'unification internationale.

Fig. 3. — La Convention du Mètre (1875).

Première page et premières signatures de l'exemplaire manuscrit déposé dans les Archives du Gouvernement français (Format original : environ 19,5 cm × 31 cm).



**Properties of the Earth were used to introduce a Global Sytem of Units** 





### Don't worry:

The units will be exactly identical with our present units at the time of the introduction of the new International System of Units

(no change at all for length units)



Kilogram Ampere, Ohm, Volt Kelvin Mol

# Development of "METER"-definition





**Official definition of the length unit 1 meter** (since 1983)

# The meter is defined as the length of the path travelled by light in vacuum in 1/299,792,458 of a second.

FIXED VALUE OF A FUNDAMENTAL CONSTANT AS BASIS FOR AN INTERNATIONAL UNIT (original idea of Max Planck)



**1900: Max Planck** (Theory of Black Body Radiation)

Ann.Physik <u>1</u>, 69-122 (1900)

$$E(\lambda,T) = \frac{2hc^2}{\lambda^5} \frac{1}{e^{hc/\lambda kT} - 1}$$

"....with the help of fundamental constants we have the possibility of establishing units of length, time, mass, and temperature, which necessarily retain their <u>significance for all</u> <u>cultures, even unearthly and nonhuman</u>

ones."

even Aliens understand the universal language of science and fundamental constants





#### Max Planck and his Universal Units

Planck length 
$$l_p = \sqrt{\frac{\hbar G}{c^3}} \approx 1.6 \cdot 10^{-35} m$$
  
Planck mass  $m_p = \sqrt{\frac{\hbar c}{G}} \approx 2.18 \cdot 10^{-8} kg$   
Planck time  $t_p = \sqrt{\frac{\hbar G}{c^5}} \approx 5.39 \cdot 10^{-44} s$   
Planck temperature  $T = \sqrt{\frac{\hbar c^5}{Gk_B^2}} = 1.42 \cdot 10^{32} K$ 

Unfortunately, Planck units are useless for practical applications



5 month ago: 25<sup>th</sup> meeting of the Conférence générale des poids et mesures

#### Tuesday 18 November 2014 at 9:30

at the Palais des Congrès de Versailles, 10 rue de la Chancellerie, 78000 Versailles, Yvelines, France.

#### 1<sup>st</sup> General Conference on Weights and Measures: 1889

Constitution of the General Conference on Weights and Measures

Metre Convention (1875): Article 3\*

"The International Bureau<sup>\*\*</sup> shall operate under the exclusive direction and supervision of an *International Committee for Weights and Measures*<sup>\*\*\*</sup>, itself placed under the authority of a *General Conference on Weights and Measures*<sup>\*\*\*\*</sup>, consisting of the delegates of all the contracting Governments."

Regulations annexed to the Metre Convention (1875): Article 7\*

"The General Conference, mentioned in Article 3 of the Convention, shall meet in Paris, on the convocation of the International Committee at least once every six years.



5 month ago: 25<sup>th</sup> meeting of the *Conférence générale des poids et mesures* 

#### List of Draft Resolutions of the General Conference on Weights and Measures (25th meeting)

- A On the future revision of the International System of Units, the SI
- B On the election of the International Committee for Weights and Measures
- C On the Pension and Provident Fund of the BIPM
- D Dotation of the BIPM for the years 2016 to 2019
- E On the importance of the CIPM Mutual Recognition Arrangement

Proposal for a new SI system						
Base Unit		Reference constants used to define the unit         in the current SI       reference constant in the new SI				
second,	S	Δν( <sup>133</sup> Cs) <sub>hfs</sub>	$\Delta v (^{133}Cs)_{hfs}$	Cs hyperfine splitting		
metre,	m	С	с	speed of light in vacuum		
kilogram,	kg	$m(\mathcal{K})$	h	Planck constant		
ampere,	А	$\mu_0$	е	elementary charge		
kelvin,	К	T <sub>TPW</sub>	k	Boltzmann constant		
mole,	mol	<i>M</i> ( <sup>12</sup> C)	N <sub>A</sub>	Avogadro constant		
candela,	cd	$K_{cd}$	K <sub>cd</sub>	luminous efficacy of a 540 THz source		





#### **Roadmap Until Next CGPM Meeting**



Conditions from CCM Recommendation G1 (2013)



## Activities at NIST in 2014 FOR A NEW KILOGRAM





## Physics Today July 2014



#### A makeover for the SI

also: Cold electrons for fast diffraction The ozone hole turns 30 Strategizing for high-energy physics

#### A more fundamental International System of Units

# The kilogram will be replaced by a fixed value of the Planck constant *h*

tem of Units (SI, from the French Système International d'Unités) was officially established in 1960, its origin goes back to the creation of the metric system during the French Revolution. Following an idea proposed a century earlier by John Wilkins,1 the new system of weights and measures took as its starting point a single universal measure-the meter-and used it to define length, volume, and mass. The meter came from a perceived constant of nature: one tenmillionth of the distance along Earth's meridian through Paris from the North Pole to the equator.<sup>2</sup> Definitions for the units of volume and mass followed, with the liter being 0.001 m3 and the kilogram the mass of 1 liter of distilled water at 4 °C. Subsequently, in 1799, two platinum artifact standards for length and mass based on those definitions were deposited in the Archives de la République in Paris. In the words of the Marquis de Condorcet, a new system of measurement "for all time, for all people" was born.

www.physicstoday.org

Convention 1875 established three international organizations: the General Conference on Weights and Measures (CGPM), the International Committee for Weights and Measures (CIPM), and the International Bureau of Weights and Measures (BIPM). They were formally tasked with maintaining the SI and continue to do so.

David B. Newel

The SI is a living, evolving system, changing as new knowledge and measurement needs arise, albeit sometimes slowly when measured against the rapid pace of scientific progress. For example, in the 18th and 19th centuries when natural philosophers and scientists tried to apply the system of length, mass, and time – with time defined by astronomical observations—to quantify newly discovered phenomena such as magnetism and electricity and the concept of energy, they also discovered the need for

David Newell is a physicist at the National Institute of Standards and Technology in Gaithersburg, Maryland, and chair of the CODATA Task Group on Fundamental Constants.





# Basic research on SILICON FIELD EFFECT TRANSISTORS initiated the expected change in the definition of our SI base units





#### The QHE has Initiated the **Development of a New SI System**

#### QHE symposium (MPI Stuttgart, June 2013)

esent kilogral The quantum-Hall effect - the key to -

Invi

Measures, Paris, France Emeritus Director, International

Terry Qui

ional System of Units in which each of The New SI is a revision kitogram, ampere, kelvin, mole and candela, the seven base units will be defined numerical value of a fundamental constant or in as adopted in principle by the 24th General Conference on constar in 2011 to be implemented when certain experimental data Key to the New SI will be the redefinition of the kilogram proved. is of a fixed numerical value for the Planck constant. Such a definition only became possible with the discovery of the quantum-Hall effect.



The kilogram prototype in Sèvre





Technology » Science & Space - Shop for Gadgets

#### Official prototype of kilogram mysteriously losing weight

Posted 9/12/2007 1:27 PM | Comments 🛛 📮 27 | Recommend 🔂 6



🕀 Enlarge

By Jacques Brinon, AP

A copy of a 118-year-old cylinder that has been the international prototype for the metric mass. American physicist Richard Davis said the reference kilo appears to have lost 50 micrograms compared to the average of dozens of copies.

#### By Jamey Keaten, Associated Press

PARIS — A kilogram just isn't what it used to be.

The 118-year-old cylinder that is the international prototype for the metric mass, kept tightly under lock and key outside Paris, is mysteriously losing weight — if ever so slightly. Physicist Richard Davis of the International Bureau of Weights and Measures in Sevres,

southwest of Paris, says the reference kilo appears to have lost 50 micrograms compared with the average of dozens of copies.

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Other ways to share:

"The mystery is that they were all made of the same material, and many were made at the same time and kept under the same conditions, and yet the masses among them are slowly drifting apart," he said. "We don't really have a good hypothesis for it."

The kilogram's uncertainty could affect even countries that don't use the metric system — it is the ultimate weight standard for the U.S. customary system, where it equals 2.2 pounds. For scientists, the inconstant metric constant is a nuisance, threatening calculation of things like

#### electricity generation.

INSTITUTE OF PHYSICS PUBLISHING

Metrologia 42 (2005) 71-80

doi:10.1088/0026-1394/42/2/001

METROLOGIA

# **Redefinition of the kilogram: a decision whose time has come**

Ian M Mills<sup>1</sup>, Peter J Mohr<sup>2</sup>, Terry J Quinn<sup>3</sup>, Barry N Taylor<sup>2</sup> and Edwin R Williams<sup>2</sup>

> My Nobel Prize discovery (Quantum Hall Effect) plays an important role !



My Nobel Prize is connected with basic research on the most important device in electronics: MOS field effect transistor





#### Field Effect Transistor, the Backbone of Electronics





## **Two-Dimensional Electron Gas**





**ELECTRONS** 



## Nobel Prize 2010 Nobel Prize 2000

#### **Graphene: The ideal 2DEG**

#### Modern version of Si MOSFET



Heterostructures for fast electronics: HEMT (2DEG for High Electron Mobility Transistor



### 1879: Discovery of the Hall effect



ellows: Type equation here



The results obtained are as follows:

*			i ype equation here
Current through gold leaf strip.	Strength of Magnetic field.	Current through Thomson galvanometer.	$C \times M$
С.	М.	c.	c
0616	11420 H	0000000232	303000000000
•0249	11240"	0000000085	329000000000
0389	11060 "	0000000135	319000000000
0598	7670 "	0000000147	312000000000
0595	5700 "	*0000000104	326000000000

Edwin Hall (1855-1938)

 $U_{H} \sim B \cdot I$ Proportional constant gives information about electron concentration





Integer Quantum Hall Effect for GaAs/AlGaAs Heterostructure






### Memos from 5.2.1980

The Hall resistance depends (in a certain magnetic field range) only on the fundamental constant h/e<sup>2</sup> ell (1, 7, -1) = M.P. 1. Tota B I tic = surta VE = 25813 L Alte Pinakothek : Deutsches Museum 25763 R : N Montag - Sonntag Täglich außer Montag 10 - 17 Uhr E Donnerstag 10 - 20 Uhr 09.00 Uhr - 17.00 Uhr 2151.08 2146.47 THITESHOUL & DOCTOR Seren a



## First draft of the "NOBEL" publication (submitted 30.5.1980 to PRL)

#### Realization of a resistance standard based on natural constants

K. v. Klitzing, Physikalisches Institut der Universität Würzburg, D-8700 Würzburg, FRG
G. Dorda, Forschungslaboratorien der Siemens AG, D-8000 München and M. Pepper, Cavendish Laboratory, University of Cambridge, Cambridge, U.K.

#### Abstract

Measurements of the Hall voltage of a two dimensional electron gas, realized with a silicon MOS fieldeffect transistor, show, that the Hall resistance at experimentally well defined surface carrier concentrations has a fixed value which depends only on natural constants and which is insensitive to the geometry of the device.



## Reaction from PRL (20.6.1980)

has been reviewed by our referee(s). On the basis of the resulting report(s), we judge that the paper is not suitable for publication in Physical Review Letters in its present form, but might be made so by appropriate revision. Pertinent criticism extracted from the report(s) is enclosed. While we cannot made a definite commitment, the probable course of action if you choose to resubmit is indicated below.

- ) Acceptance, if the editors can judge that all or most of the criticism has been met.
  - ) Return to the original referee(s) for judgement.
  - Submittal to new referee(s) for judgement.

Please accompany your resubmittal by a summary of the changes made, and a brief response to any criticisms you have not attempted to meet. Do not ask us to make changes in the manuscript, but send us either a new copy or revised pages for substitution.

CAUTION! PLEASE STAY WITHIN ALLOWED LENGTH WHENEVER ADDITIONS OR MODIFICATIONS ARE MADE.

Sincerely yours,

Editor (Associate

enc. GB/vm



#### **QUANTIZED HALL RESISTANCE IN SI OHM**

#### (data collected until 1988)

CSIRO, Australia	25 812.809 (2) Ω
NPL, UK	25 812.809 (1) Ω
<b>BNM-LCIE, France</b>	25 812.802 (6) Ω
ETL, Japan	25 812.806 (6) Ω
NIST, USA	25 812.807 (1) Ω
VNIIM, Russia	25 812.806 (8) Ω
VSL, Netherland	25 812.802 (5) Ω
NRC, Canada	25 812.814 (6) Ω
EAM, Switzerland	25 812.809 (4) Ω
PTB, Germany	25 812.802 (3) Ω
NIM, China	25 812.805 (16) Ω
CSIRO/BIPM	25 812.809 (2) Ω
CSIRO/Japan	25 812.813 (2) Ω
<b>BEST VALUE (1990):</b>	$R_{\rm K}$ =25 812.807 (5) $\Omega$

limitations due to calibration of reference resistor



The Comité International des Poids et Mesures,



acting in accordance with instructions given in <u>Resolution 6</u> of the 18th Conférence Générale des Poids et Mesures concerning the forthcoming adjustment of the representations of the volt and the ohm,

#### considering

- that most existing laboratory reference standards of resistance change significantly with time,
- that a laboratory reference standard of resistance based on the quantum Hall effect would be stable and reproducible,
- that a detailed study of the results of the most recent determinations leads to a value of 25 812.807  $\Omega$  for the von Klitzing constant,  $R_{\rm K}$ , that is to say, for the quotient of the Hall potential difference divided by current corresponding to the plateau *i* = 1 in the quantum Hall effect,
- that the quantum Hall effect, together with this value of R<sub>K</sub>, can be used to establish a reference standard of resistance having a one-standard-deviation uncertainty with respect to the ohm estimated to be 2 parts in 10<sup>7</sup>, and a reproducibility which is significantly better,

#### recommends

• that 25.812.807  $\Omega$  exactly be adopted as a conventional value, denoted by  $R_{K-90}$ , for the von Klitzing constant,

 $R_{\mathrm{K}}$ 

 that this value be used from 1 January 1990, and not before, by all laboratories which base their measurements of resistance on the guantum Hall effect,



http://physics.nist.gov/cuu/Constants/index.html

## The NIST Reference on Constants, Units, and Uncertainty

#### fixed value without uncertainty

just for calibrations, outside our present SI system





Quantized Hall Resistance for Different Materials



Using an ultrasensitive, cryogenic, current-comparator bridge the quantized Hall resistance  $R_n(2)$  in a GaAv/AlGaAs heterostructure has been compared directly with  $R_n(4)$  in a ulicon MOSFET. The measurements show that  $R_n(2GaAv)/R_n(4SB) = 211 - 0.22(1.5) \times 10^{-101}$ . Within the 1 $\sigma$  combined uncertainty of 2.5 × 10.1 $^{-101}$  the realizing suggests that the quantized Hall resistance is a universal quantity, independent of the host lattice and Landau-level index, and is probably equivalent to  $h/\sigma^2$ , the relationship predicted theoretically.

T J B M Janssen<sup>1,6</sup>, N E Fletcher<sup>2</sup>, R Goebel<sup>2</sup>, J M Williams A Tzalenchuk<sup>1</sup>, R Yakimova<sup>3</sup>, S Kubatkin<sup>4</sup>, S Lara-Avila<sup>4</sup> and V I Falko<sup>5</sup>

#### Very Wide QHE Plateau for CVD Grown Graphene on SiC http://arxiv.org/abs/1407.3615v1









## The QAH Effect Measured at 30 mK.





### **Room-temperature QHE in Graphene.**



K S Novoselov et al. Science 2007;315:1379





## **Fundamental Constants**

Quantity	Symbol	Numerical value	Unit
electron mass	$m_{\rm e}$	$9.10938291(40)  imes 10^{-31}$	kg
proton mass	$m_{ m p}$	$1.672621777(74) \times 10^{-27}$	kg
proton-electron mass ratio	$m_{ m p}/m_{ m e}$	1836.15267245(75)	
Avogadro constant	$N_{\rm A}, L$	$6.02214129(27) imes10^{23}$	$mol^{-1}$
Faraday constant $N_{\rm A}e$	F	96 485.3365(21)	$C \text{ mol}^{-1}$
molar gas constant	R	8.314 4621(75)	$\rm J~mol^{-1}~K^{-1}$
Boltzmann constant $R/N_A$	k	$1.3806488(13) \times 10^{-23}$	$\rm J~K^{-1}$
Stefan-Boltzmann const. $\pi^2 k^4/60\hbar^3 c^2$	$\sigma$	$5.670373(21)  imes 10^{-8}$	${\rm W}~{\rm m}^{-2}~{\rm K}^{-4}$
magnetic flux quantum $h/2e$	$\Phi_0$	$2.067833758(46)  imes 10^{-15}$	Wb
Josephson constant $2e/h$	$K_{\mathrm{J}}$	$483597.870(11)  imes 10^9$	$\rm Hz~V^{-1}$
von Klitzing constant $h/e^2$	$R_{\rm K}$	25812.8074434(84)	Ω
electron volt $(e/C)$ J	eV	$1.602176565(35)  imes 10^{-19}$	J
(unified) atomic mass unit $\frac{1}{12}m(^{12}C)$	u	$1.660538921(73)\times10^{-27}$	kg

A more extensive listing of constants is available in the references given above and on the NIST Physical Measurement Laboratory Web site: physics.nist.gov/constants.



## **Consistency Check by "Ohms Law"**





### **Semiconductor Quantized Voltage Source**



## An "integrated quantized circuit" (IQC)

Frank Hohls et al., Phys. Rev. Lett. 109, 056802



Metrological triangle confirmed up to Error Correction (Electron Pumps in Series) uncertainty level of ≈1 ppm

island

single electron detector

### Self-Referenced Single-Electron Quantized Current Source

Lukas Fricke, Michael Wulf, Bernd Kaestner, Frank Hohls, Philipp Mirovsky, Brigitte Mackrodt, Ralf Dolata, Thomas Weimann, Klaus Pierz, Uwe Siegner, and Hans W. Schumacher



For practical applications:

## Josephson voltage and quantized Hall resistance are fixed by the fundamental constants *h* and *e*.

Josephson effect: Voltage  $U \leftrightarrow e/h$ 

Quantum Hall effect: Resistance  $R \leftrightarrow h/e^2$ 

All electrical quantities can be measured (with high precision!) in units of h and e

## Electrical Quantum Standards Formed the Basis for the New SI

units based on fundamental constants *h* and *e* and on frequency (atomic clock)





Metrologia 42 (2005) 431-441

## Towards an electronic kilogram: an improved measurement of the Planck constant and electron mass

#### Richard L Steiner, Edwin R Williams, David B Newell and Ruimin Liu

National Institute of Standards and Technology (NIST), 100 Bureau Dr Stop 8171, Gaithersburg, MD 20899-8171, USA

#### Abstract

The electronic kilogram project of NIST has improved the watt balance method to obtain a new determination of the Planck constant *h* by measuring the ratio of the SI unit of power W to the electrical realization unit W<sub>90</sub>, based on the conventional values for the Josephson constant  $K_{J.90}$  and von Klitzing constant  $R_{K.90}$ . The value  $h = 6.62606901(34) \times 10^{-34}$  J s verifies the NIST result from 1998 with a lower combined relative standard uncertainty of 52 nW/W. A value for the electron mass  $m_e = 9.10938214(47) \times 10^{-31}$  kg can also be obtained from this result.



AME

## Final result: $h \leftrightarrow m$



#### A LEGO Watt Balance: An apparatus to demonstrate the definition of mass based on the new SI

L.S. Chao, S. Schlamminger, D.B. Newell, and J.R. Pratt

Physical Measurement Laboratory, National Institute of Standards and Technology, Gaithersburg, MD 20899

G. Sineriz, F. Seifert, A. Cao, and D. Haddad

Joint Quantum Institute, University of Maryland, College Park, MD 20742

X. Zhang

Computational Instrumentation Lab, Massachusetts Institute of Technology, Cambridge, MA 02139 (Dated: December 15, 2014)

A global effort to redefine our International System of Units (SI) is underway and the change to the new system is expected to occur in 2018. Within the newly redefined SI, the present base units will still exist but be derived from fixed numerical values of seven reference constants. More specifically, the unit of mass, the kilogram, will be realized through a fixed value of the Planck constant h. For instance, a watt balance can be used to realize the kilogram unit of mass within a few parts in  $10^8$ . Such a balance has been designed and constructed at the National Institute of Standards and Technology. For educational outreach and to demonstrate the principle, we have constructed a LEGO tabletop watt balance capable of measuring a gram size mass to 1% relative uncertainty. This article presents the design, construction, and performance of the LEGO watt balance and its ability to determine h.

#### MASS $m \rightarrow$ PLANCK CONSTANT h

In the future (new SI): PLANCK CONSTANT  $h \rightarrow MASS m$ 



#### **Summary of Planck Constant Measurements**





 $h \cdot N_A = 3.9903126821(57) \times 10^{-10}$  Js/mol, with relative uncertainty of 1.4×10<sup>-9</sup>

## **IAC** (International Avogadro Coordination)

2003

<sup>28</sup>Si for



## <sup>28</sup>Si: 99,9957%

 $N_A = \frac{M_{Si} \cdot V_{Kugel}}{\sqrt{8} \cdot d_{220}^3 \cdot m_{Kugel}}$ 



IAC 2007/2008





## **Volume: interferometer for spheres**







PTB's sphere interferometer with spherical symmetry

PTB's sphere interferometer enables complete topographies of spheres,  $n_{diameter} \approx 600\ 000$ .

The radius uncertainty is 0.8 nm

Radius topography of <sup>28</sup>Si-sphere S8. Peak to valley deviations from roundness amount to **99 nm**.



## Surface layer characterization for sphere AVO28-8





## **Uncertainty budget**

Quantity	Relative uncertainty 10 <sup>-9</sup>	Contribution %
Molar mass	8	7
Sphere mass	5	3
Surface	16	27
Sphere volume	22	51
Lattice parameter	10	10
Point defects	4	2

## Avogadro project and Watt balances allow high precision measurements of Planck Constant *h*

Watt balances has been built up in many countries and seems to be the best way to realize the unit of mass on the basis of a fixed value for the Planck constant

QUANTUM HALL EFFECT WILL PLAY AN IMPORTANT ROLE IN OUR NEW INTERNATIONAL SYSTEM OF UNITS



Gewichtiges Vorhaben: Das Kilogramm soll neu definiert werden, denn das Urkliogramm ist unpraktisch, und es verändert sich sogar. An der Physikalisch-Technischen Bundesanstalt in Braunschweig soll eine präzise vermessene, hochreine Siliziumkugel benutzt werden, um das Kilogramm auf eine Naturkonstante zu gründen: das Plancksche Wirkungsquantum. Peter Becker hat dieses Projekt 30 Jahre lang geleitet. Inzwischen ist er im Ruhestand. In der rechten Hand hält er eine Kopie des Urkilos, in der linken eine Siliziumkugel.

> silicon sphere Avogadro project

kilogram prototype Watt balance mechanical force ↔ electrical force quantum Hall effect ↔ kilogram



## Photo Gallery of all Watt Balances





## Basic research on a silicon MOSFET opened the possibility of a new system of units based on fundamental constants

## SILICON

not only the most important material in microelectronics but also a very important material in metrology

The size of the new silicon resonator compared to the size of a coin

# The most stable laser in the world

Silicon resonator with length stability unachieved so far – for improved optical atomic clocks

