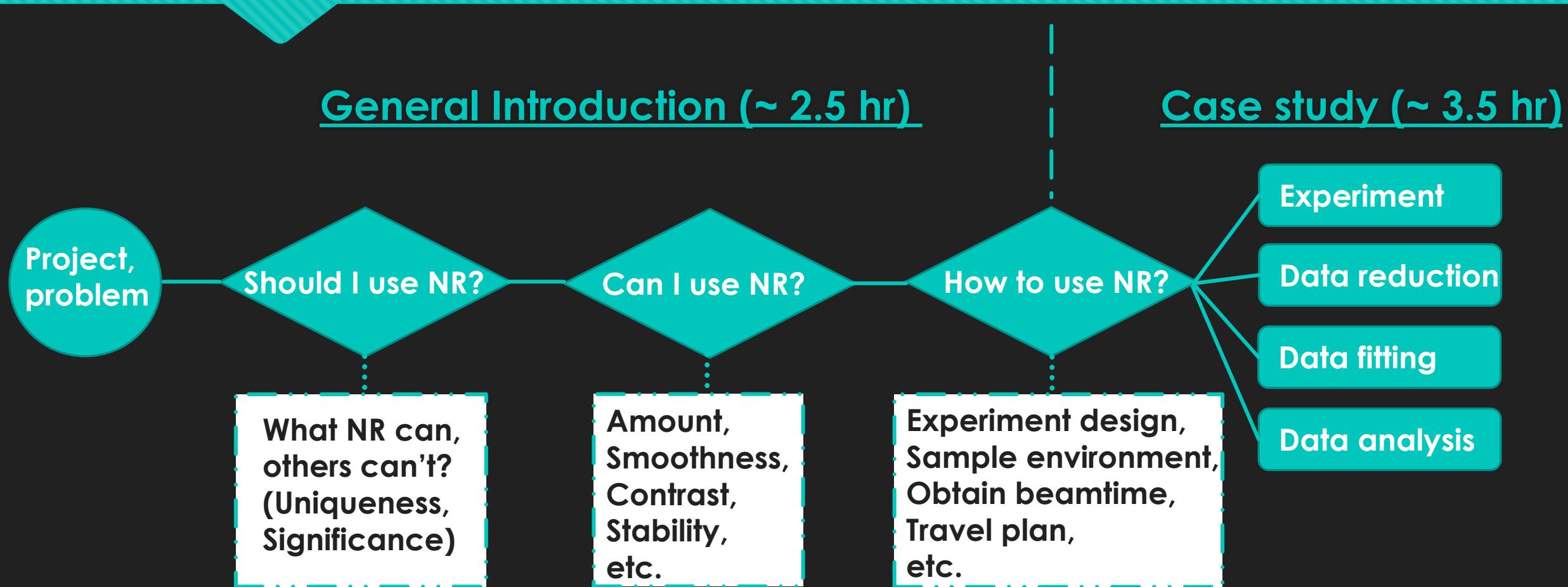


# Neutron Reflectivity Investigation of the Propagation of Melt Polymers across a Glassy Interface

CHRNS School on Methods and Applications of SANS and NR  
NIST Center for Neutron Research

July 2024

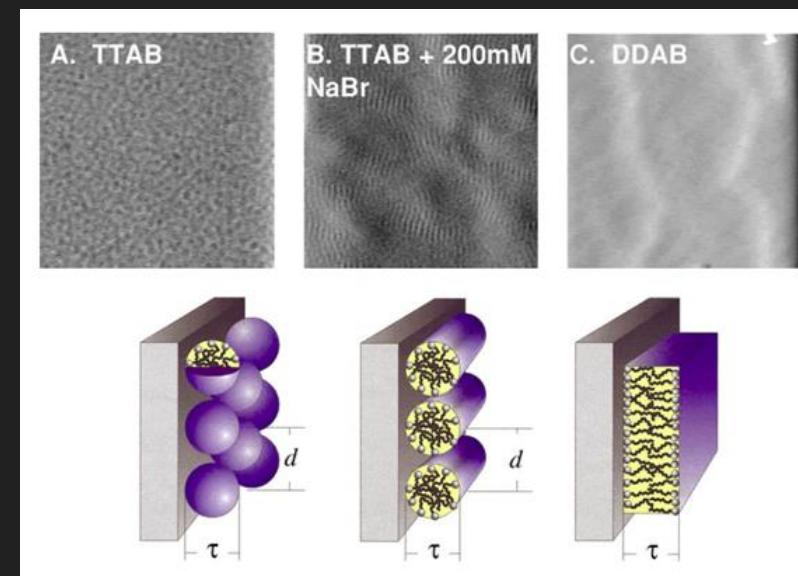
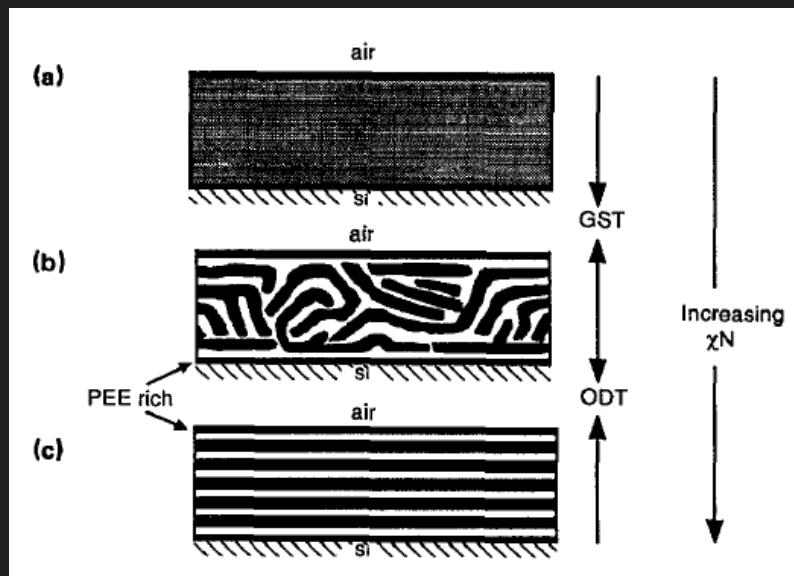
# Schedule & Content



# What NR is for?

Neutron reflectometry is a technique for investigating the thickness and the chemical composition of one or several thin layers at a surface or an interface of many materials.

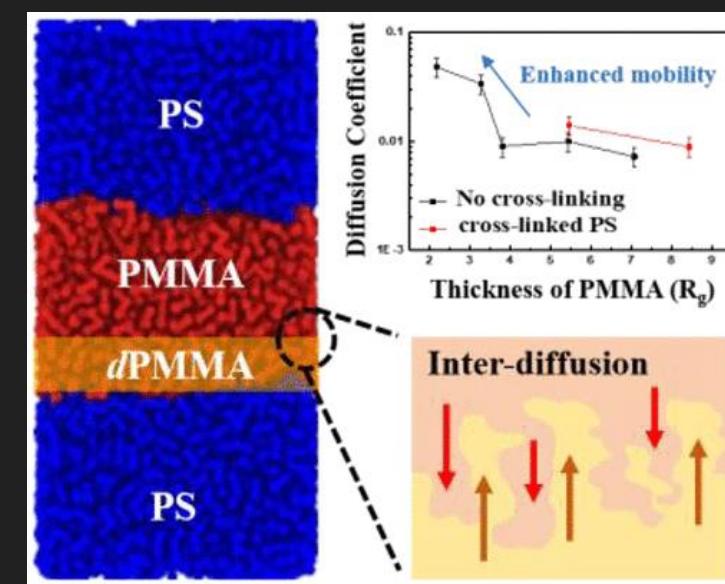
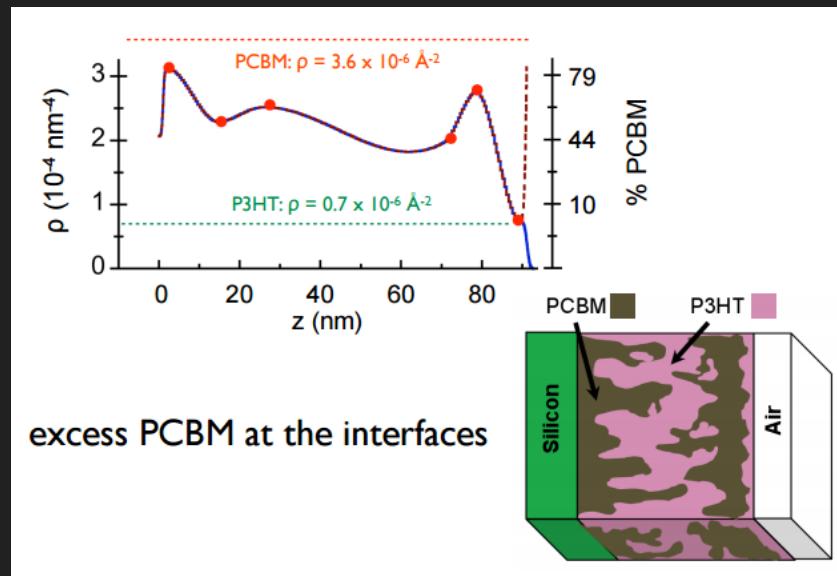
## ○ Application examples (air-solid interface)



# What NR is for?

Neutron reflectometry is a technique for investigating the thickness and the chemical composition of one or several thin layers at a surface or an interface of many materials.

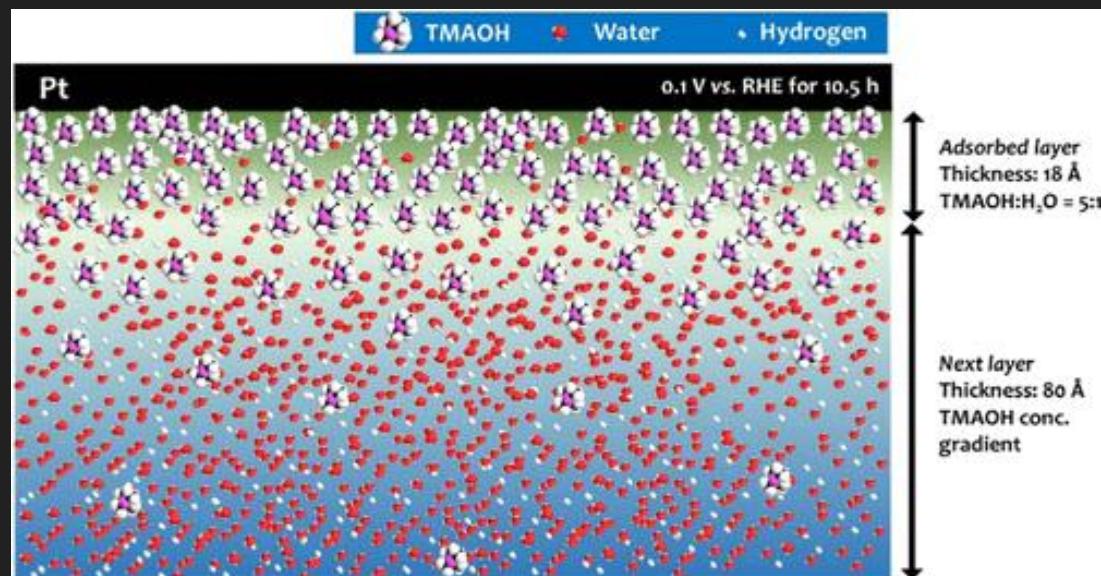
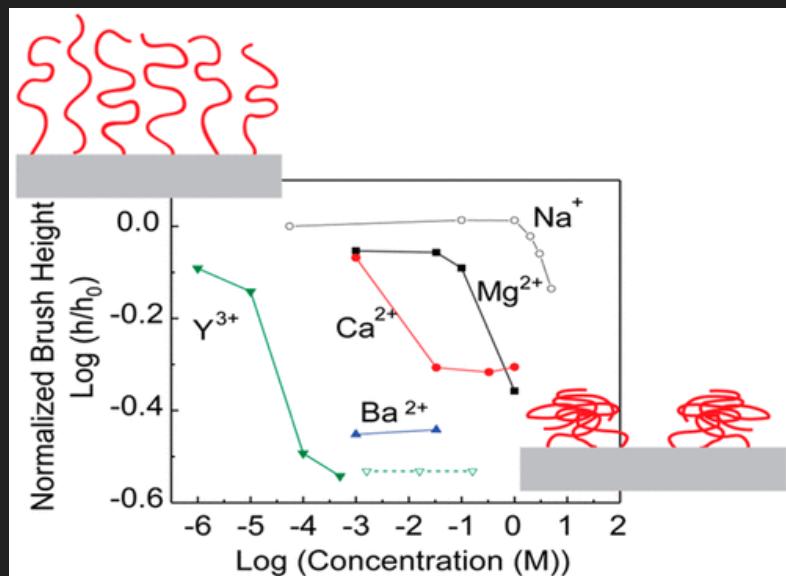
## ○ Application examples (solid-solid interface)



# What NR is for?

Neutron reflectometry is a technique for investigating the thickness and the chemical composition of one or several thin layers at a surface or an interface of many materials.

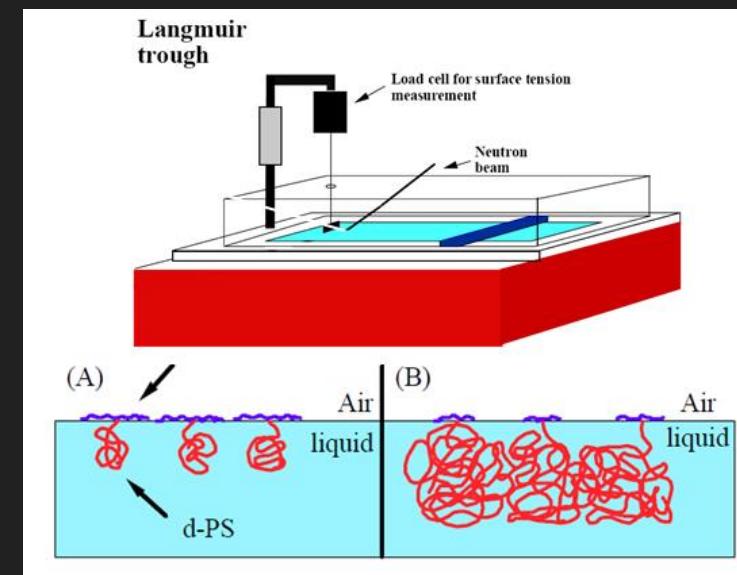
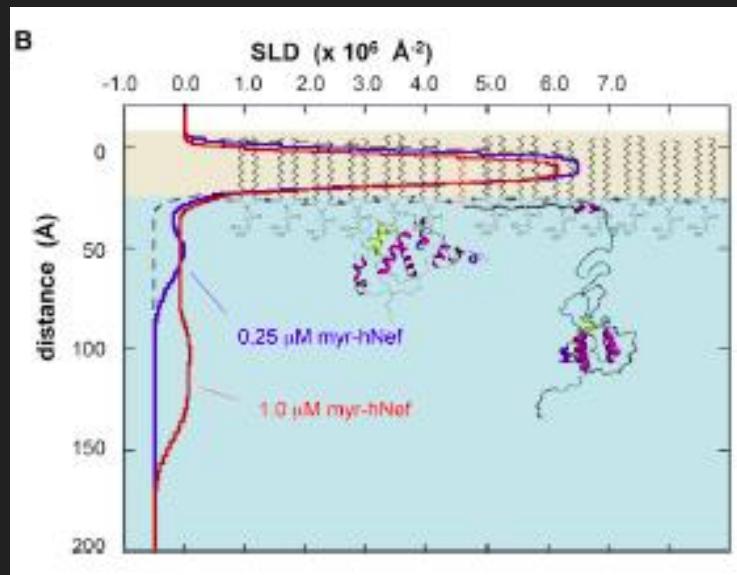
## ○ Application examples (liquid-solid interface)



# What NR is for?

Neutron reflectometry is a technique for investigating the thickness and the chemical composition of one or several thin layers at a surface or an interface of many materials.

## ○ Application examples (air-liquid interface)



# What information NR provides?

- Scattering length density (SLD) vs. depth profile  
(composition vs. depth profile; concentration vs. depth profile; etc.)  
SLD calculator: <http://www.refcalc.appspot.com/sld>

The screenshot shows a web browser window with the URL [refcalc.appspot.com/sld](http://www.refcalc.appspot.com/sld) in the address bar. The page title is "Scattering Length Density Calculator". There are several input fields and calculated results:

- Chemical Formula: Si (highlighted in green)
- e.g. use H[2]2O (or D2O) or deuterated water, H[3]2O (or T2O) for tritiated water
- Calculate using:  density  molecular volume
- Mass density: 2.3300 g.cm<sup>-3</sup>
- Molecular Volume: 20.0159 Å<sup>3</sup>
- X-ray energy: 8.048 keV
- Neutron wavelength: 1.8 Angstrom
- Neutron SLD: (2.07370573668+2.37575233669e-05j) \* 10<sup>-6</sup> Å<sup>-2</sup>
- X-ray SLD: (20.0702465153+0.457434220159j) \* 10<sup>-6</sup> Å<sup>-2</sup>
- Submit button

# What is a SLD vs. depth profile?

## ○ Example

→ H<sub>2</sub>O Density: 0.997 g/cm<sup>3</sup>

SLD (neutron) =  $-0.56 \times 10^{-6}$  Å<sup>-2</sup>

SLD (X-ray) =  $9.44 \times 10^{-6}$  Å<sup>-2</sup>

→ D<sub>2</sub>O Density: 1.10 g/cm<sup>3</sup>

SLD (neutron) =  $6.37 \times 10^{-6}$  Å<sup>-2</sup>

SLD (X-ray) =  $9.43 \times 10^{-6}$  Å<sup>-2</sup>

→ H<sub>2</sub>O:D<sub>2</sub>O = 91.9:8.1 Density: 1.0 g/cm<sup>3</sup>

SLD (neutron) =  $0.00 \times 10^{-6}$  Å<sup>-2</sup>

SLD (X-ray) =  $9.43 \times 10^{-6}$  Å<sup>-2</sup>

→ BSA protein

Density: 2.32 g/cm<sup>3</sup>

## ○ practice

→ PMMA

Formula: (C<sub>5</sub>O<sub>2</sub>H<sub>8</sub>)<sub>n</sub>

Density: 1.18 g/cm<sup>3</sup>

SLD =  $1.06 \times 10^{-6}$  Å<sup>-2</sup>

→ dPC

Formula: (C<sub>16</sub>O<sub>4</sub>H<sub>12</sub>D<sub>6</sub>)<sub>n</sub>

Density: 1.22 g/cm<sup>3</sup>

SLD =  $3.27 \times 10^{-6}$  Å<sup>-2</sup>

→ Si

Formula: Si

Density: 2.32 g/cm<sup>3</sup>

SLD =  $2.07 \times 10^{-6}$  Å<sup>-2</sup>

# Data fitting (R → SLD profile)

<https://ncnr.nist.gov/instruments/magik/calculators/reflectivity-calculator.html>



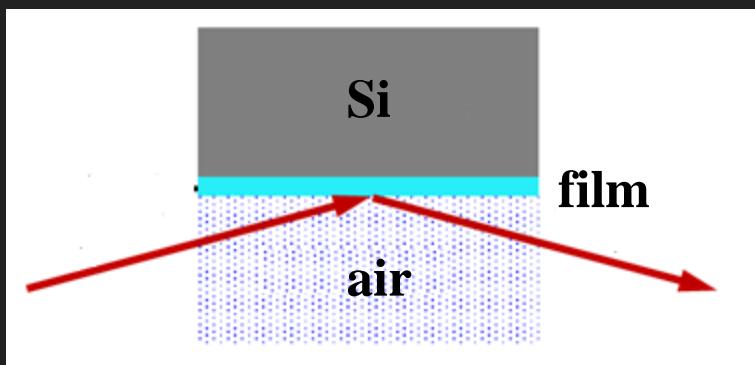
# Thickness & Reflectivity

<https://ncnr.nist.gov/instruments/magik/calculators/reflectivity-calculator.html>

## ○ practice

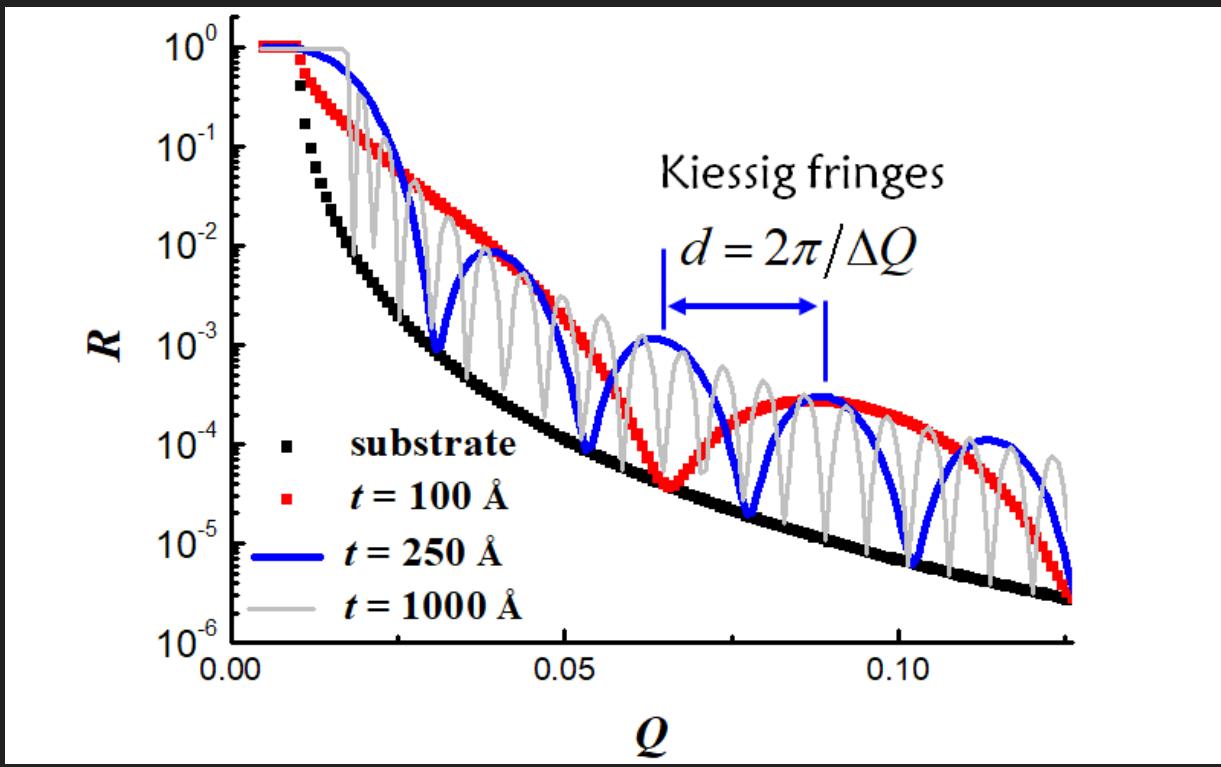
→ Single layer film on Si substrate

Vary film thickness  
(100, 250, 1000)



# Thickness & Reflectivity

thickness      period



at large  $Q$ ,  $R \approx (16\pi^2/Q^4)[\rho^2 + (\rho_s - \rho)^2 + 2\rho(\rho_s - \rho) \cos(Qd)]$

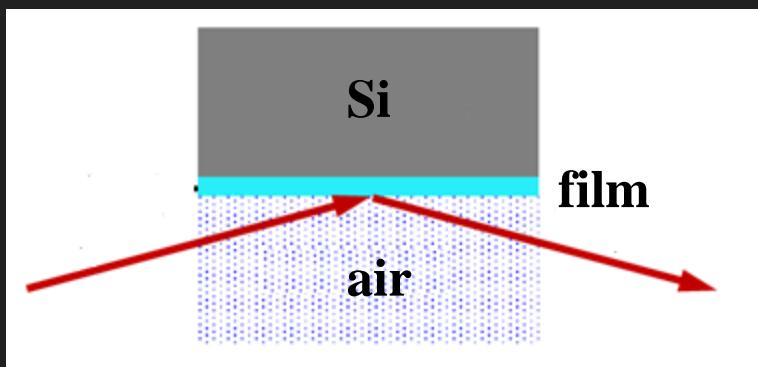
# SLD & Reflectivity

<https://ncnr.nist.gov/instruments/magik/calculators/reflectivity-calculator.html>

## ○ practice

→ Single layer film on Si substrate

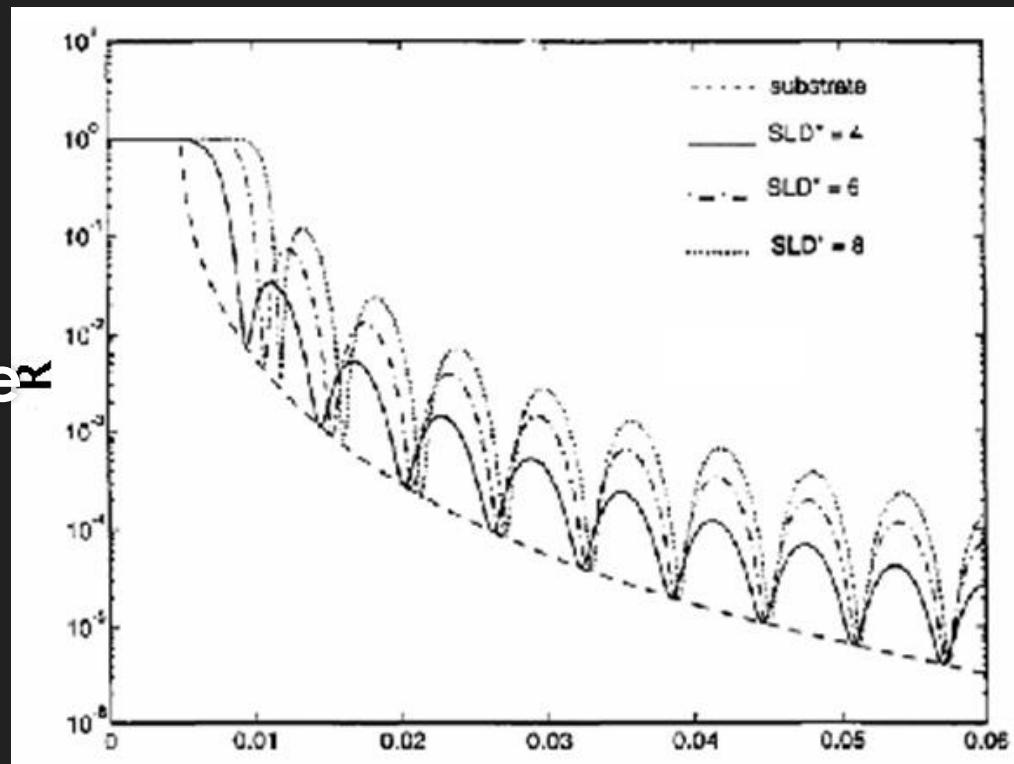
Vary film SLD  
(1.0, 2.07, 3.0, 6.0)



# SLD & Reflectivity

composition (SLD)

amplitude R



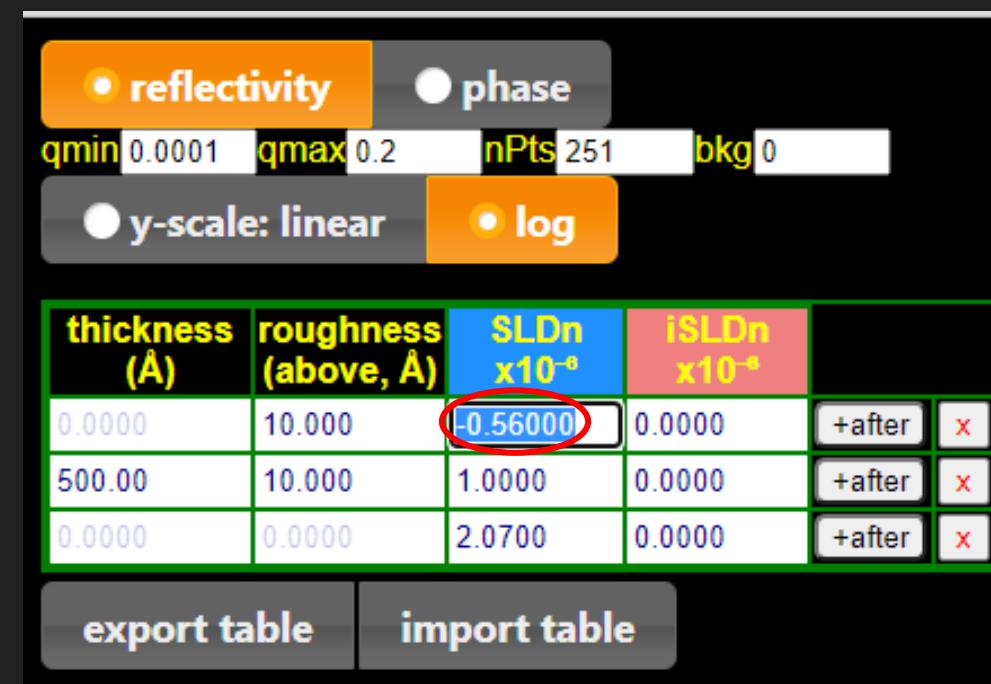
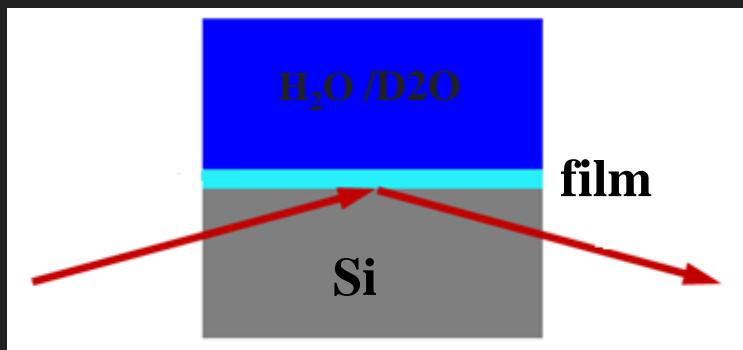
$$\text{at large } Q, \quad R \approx (16\pi^2/Q^4)[\rho^2 + (\rho_s - \rho)^2 + 2\rho(\rho_s - \rho) \cos(Qd)]$$

# SLD & Reflectivity

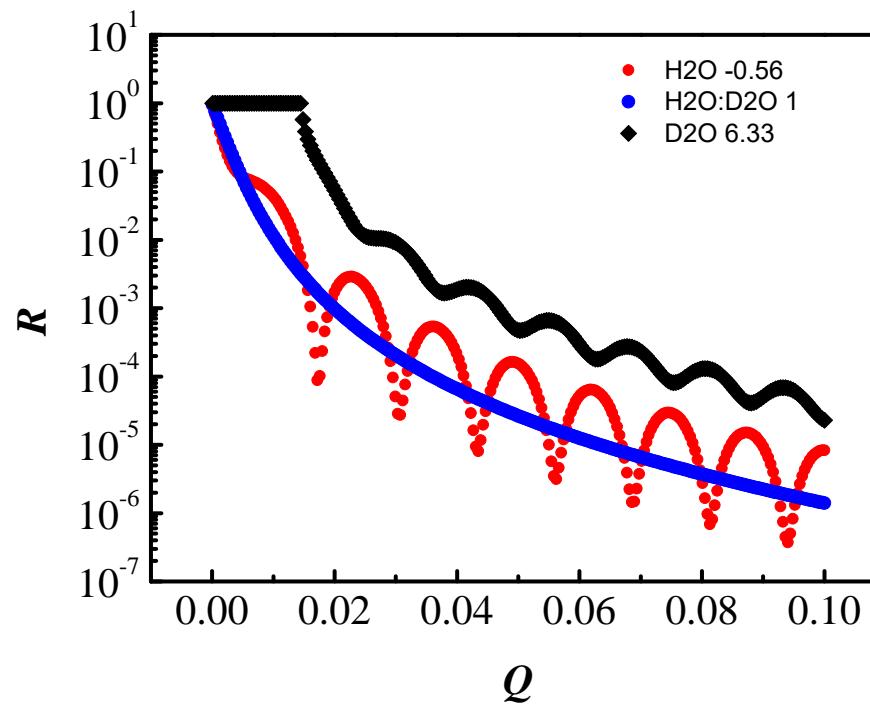
<https://ncnr.nist.gov/instruments/magik/calculators/reflectivity-calculator.html>

## ○ practice

Vary substrate SLD (-0.56; 1; 6.33 )



# SLD & Reflectivity



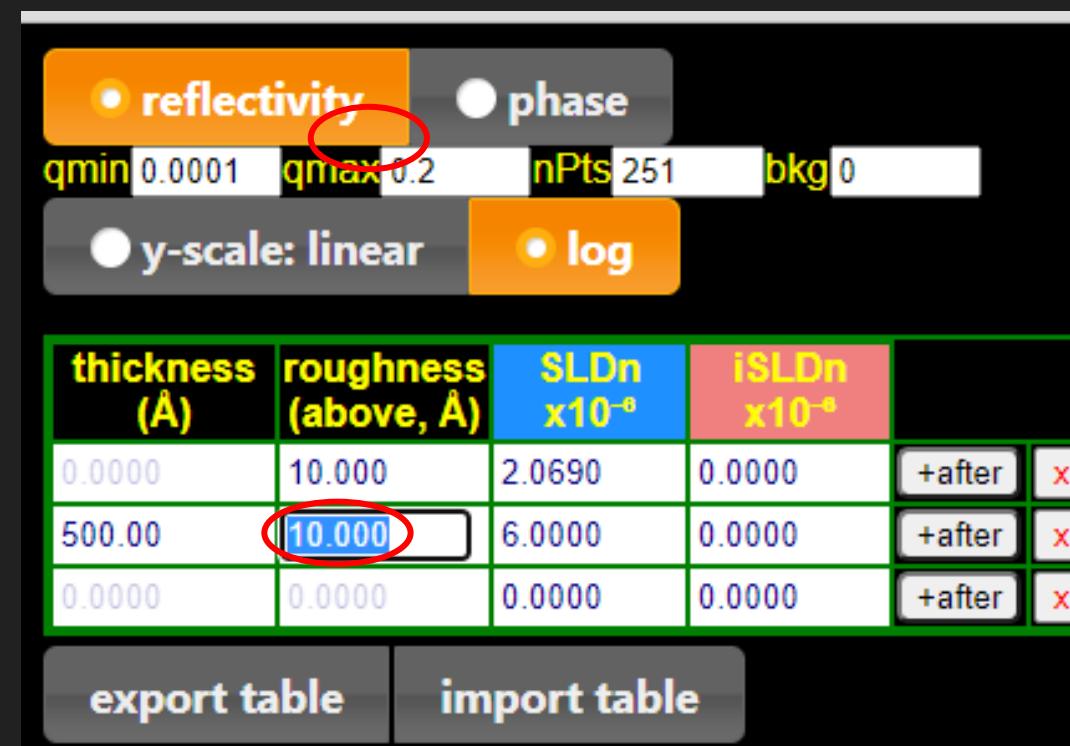
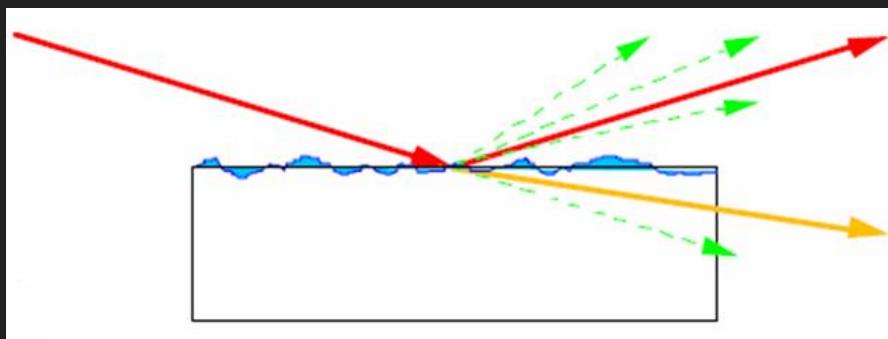
# Roughness & Reflectivity

<https://ncnr.nist.gov/instruments/magik/calculators/reflectivity-calculator.html>

## ○ practice

→ Single layer film on Si substrate

Vary film roughness  
(0, 10, 50, 100 )



# Roughness & Reflectivity

at large  $Q$ , for flat surface and interface,

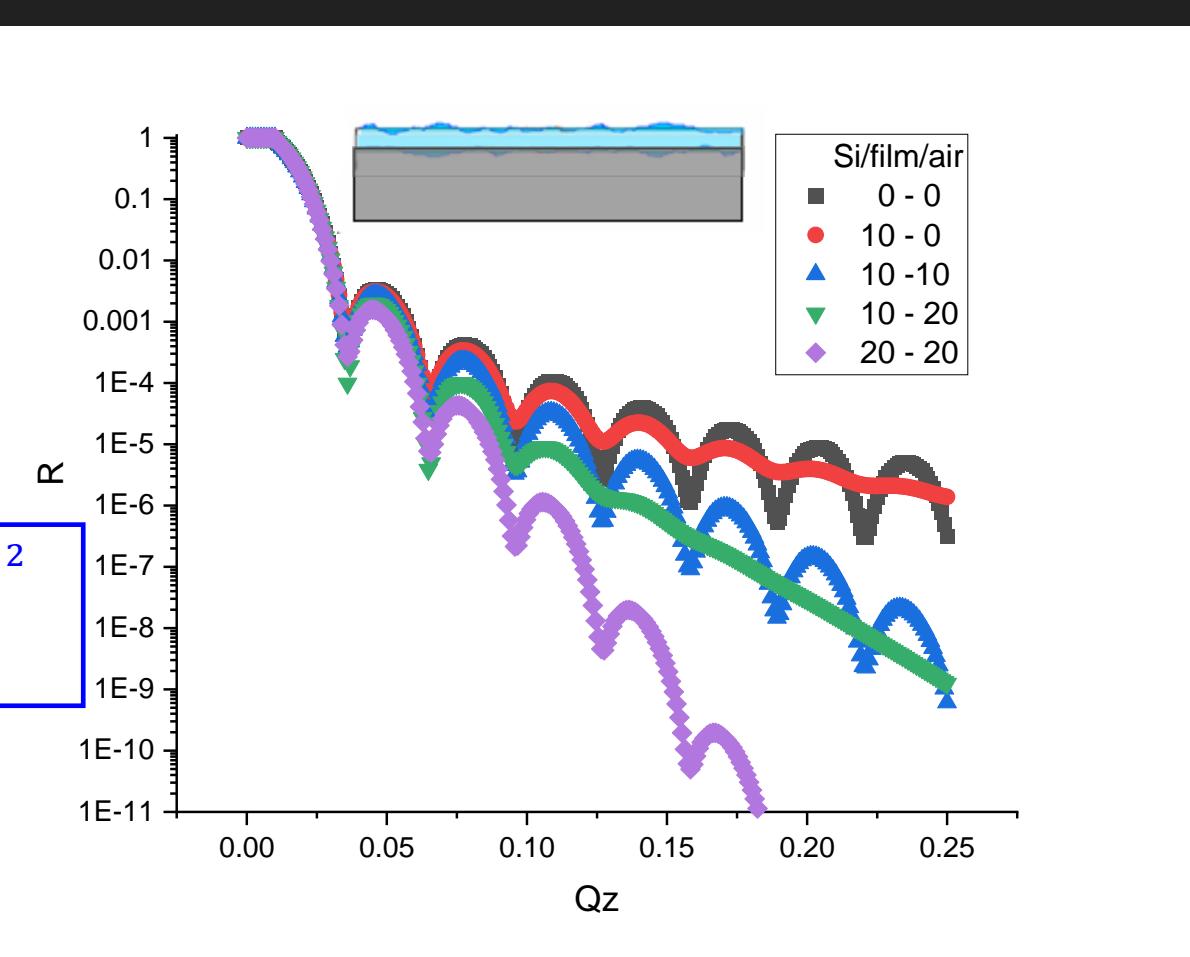
$$R \approx (16\pi^2/Q^4)[\rho^2 + (\rho_s - \rho)^2 + 2\rho(\rho_s - \rho) \cos(Qd)]$$

at large  $Q$ , for diffuse surface and interface,

$$R \approx (16\pi^2/Q^4)\{\rho^2[\exp(-\sigma_1^2 Q^2)]^2 + (\rho_s - \rho)^2[\exp(-\sigma_2^2 Q^2)]^2 + 2\rho(\rho_s - \rho) \exp(-\sigma_1^2 Q^2) \exp(-\sigma_2^2 Q^2) \cos(Qd)\}$$

roughness (interfacial width )

decay



# NR summary

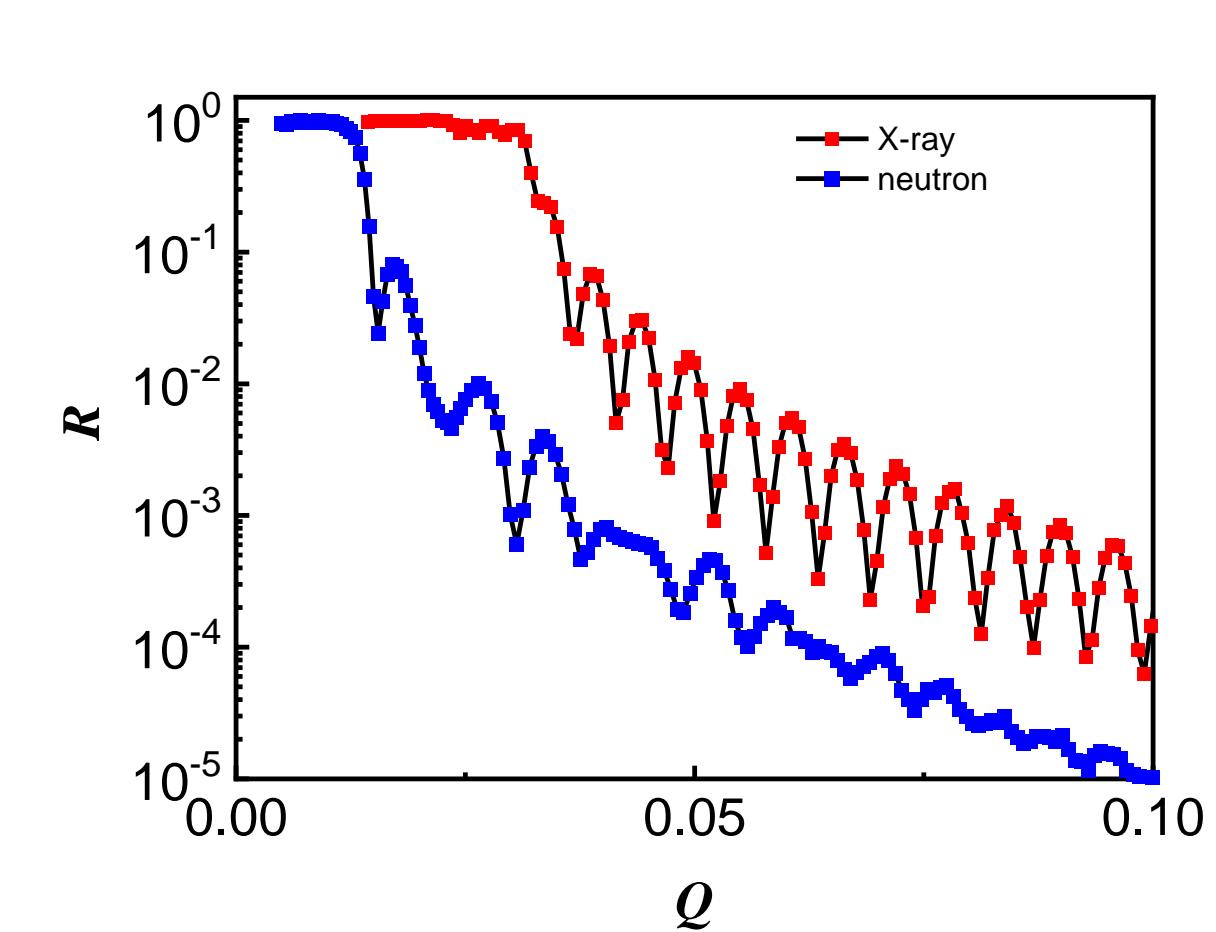
$$R = \frac{I_{\text{reflection}}}{I_{\text{incident}}} = f(Q, \rho, n, d, \sigma \dots)$$

**Substrate:** Si, quartz, sapphire

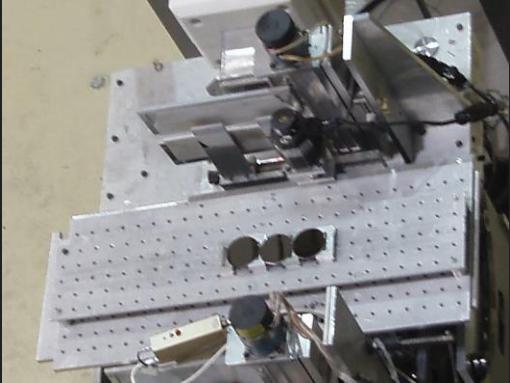
**Sample Size:** 2 ~ 4 inches

**Typical Cases:** diffusion, corrosion, adsorption, segregation, deposition...

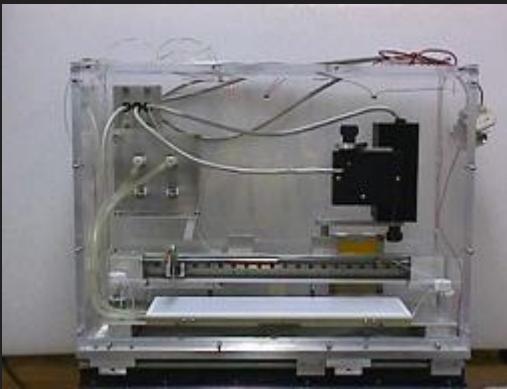
# X-ray & Neutron Comparison



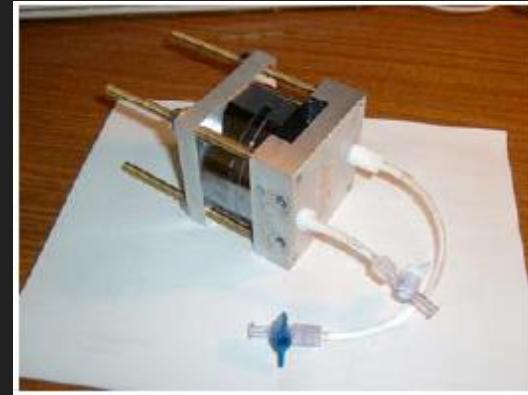
# Sample environments



solid/air



liquid/air



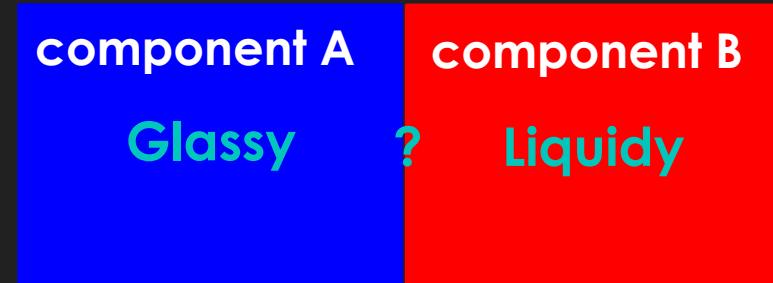
solid/liquid



vacuum, humidity, pressure ...

# Experiment

Neutron Reflectivity Investigation of the **Propagation** (transportation, diffusion, sorption, etc.) of a **Melt Polymer** across a **Glassy polymer Interface**

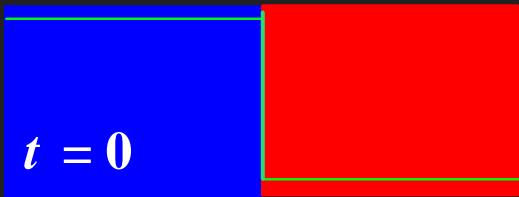


# Background: types of diffusion

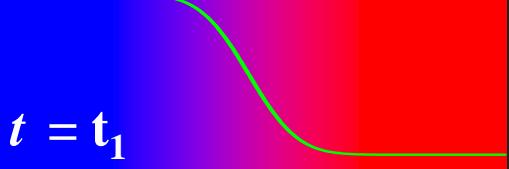
Fick's law of diffusion:  $J = -D\nabla\varphi$  (Adolf Fick in 1855)

## Fickian diffusion

(i.e. Case I diffusion)



$$t = 0$$

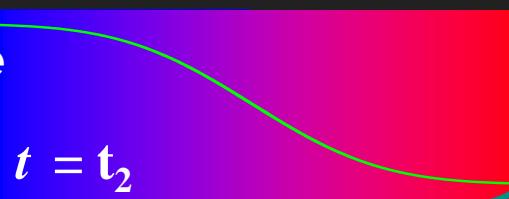


$$t = t_1$$

No clear boundaries

mass uptake

$$M \propto t^{1/2}$$



$$t = t_2$$

## Non-Fickian diffusion

Anomalous diffusion

A combination of Case I and Case II diffusion to different extents

Case II diffusion

$$t = 0$$

$$t = t_1$$

$$t = t_2$$

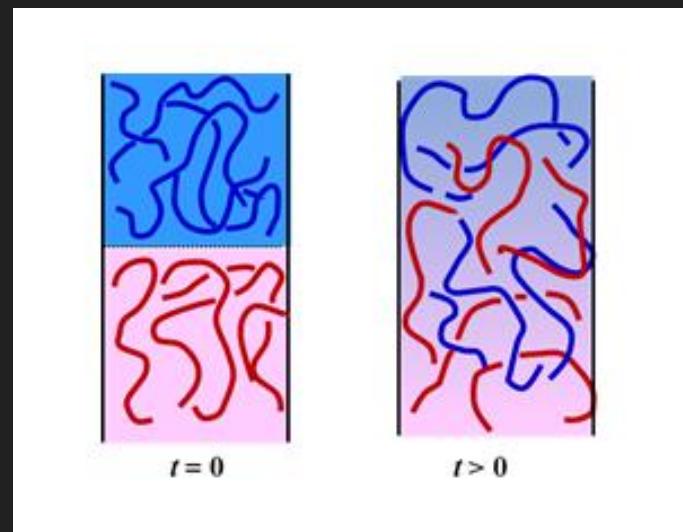
Sharp front

$$\text{mass uptake } M \propto t$$

# What causes different types of diffusion?

**Case I diffusion**  
(e.g. PS/dPS, PMMA/dPMMA)

$$T > T_{gA}, T_{gB}$$



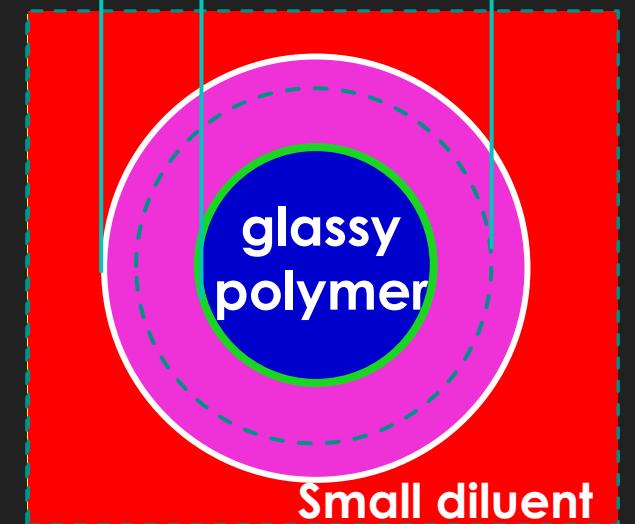
**diffusion control**  
( relaxation negligible)

Anomalous diffusion  
Comparable diffusion  
and relaxation effects

**Case II diffusion**  
(e.g. PMMA rod/methanol)

$$T < T_{gA}, T > T_{gB}$$

penetrating front  
swelling front      initial surface

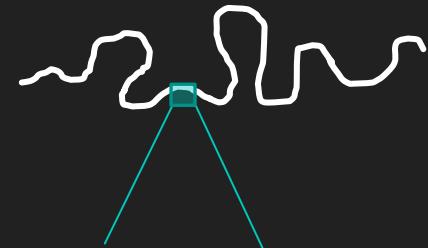


**relaxation control**

# Polymer basics

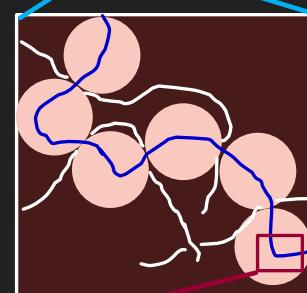
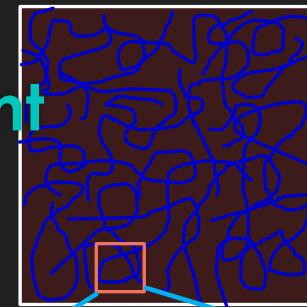
- chain-like structure  
 $M_n, M_w$

→ Repeat units



- Entanglement  
 $M_e$

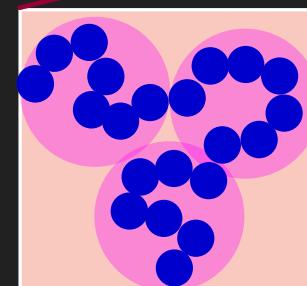
'Rouse blob'



'thermal blob'

$(q, \tau) \downarrow$

- Glass transition  
 $T_g$

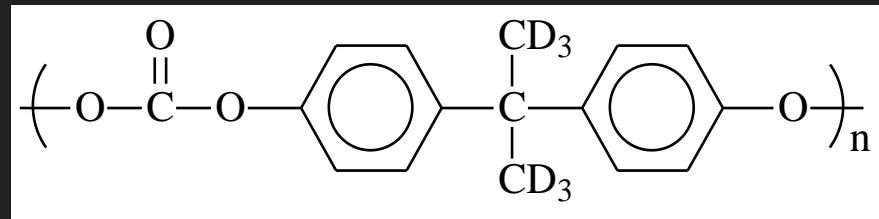


# System investigated

component A

○ deuterated polycarbonate

dPC



$T_g \approx 151 \text{ } ^\circ\text{C}$

$M_n = 8.4 \times 10^4 \text{ g/mol}$

$R_g = 11.0 \text{ nm}$

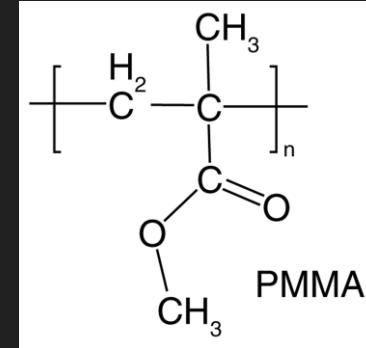
$M_e = 11,60 \text{ g/mol}$

highly entangled

component B

○ poly(methyl methacrylate)

PMMA



$T_g \approx 88 \text{ } ^\circ\text{C}$

$M_n = 4.0 \times 10^3 \text{ g/mol}$

$R_g = 1.6 \text{ nm}$

non-entangled

( $M_e$ : average molecular weight between entanglement points)

# Objective

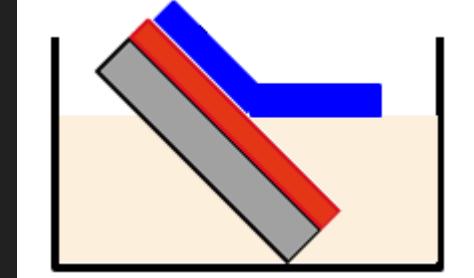
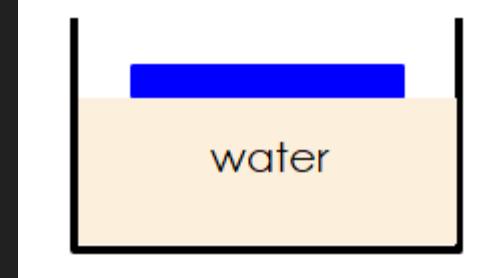
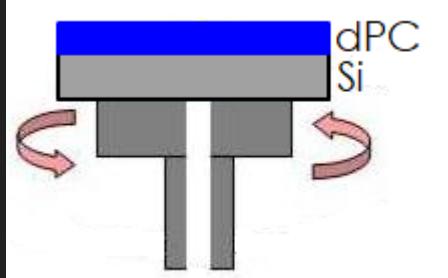
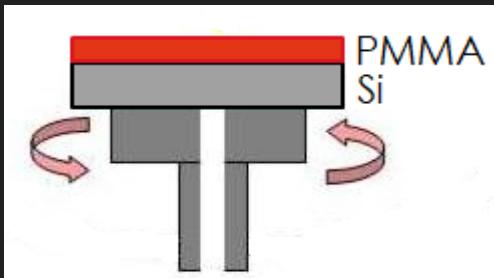


- To learn reflectivity measurements on bilayer polymer thin films.
- To determine the time evolution of interfacial profile.
- To play with the chain-like feature of polymers and understand its effect on interdiffusion.

# Sample preparation

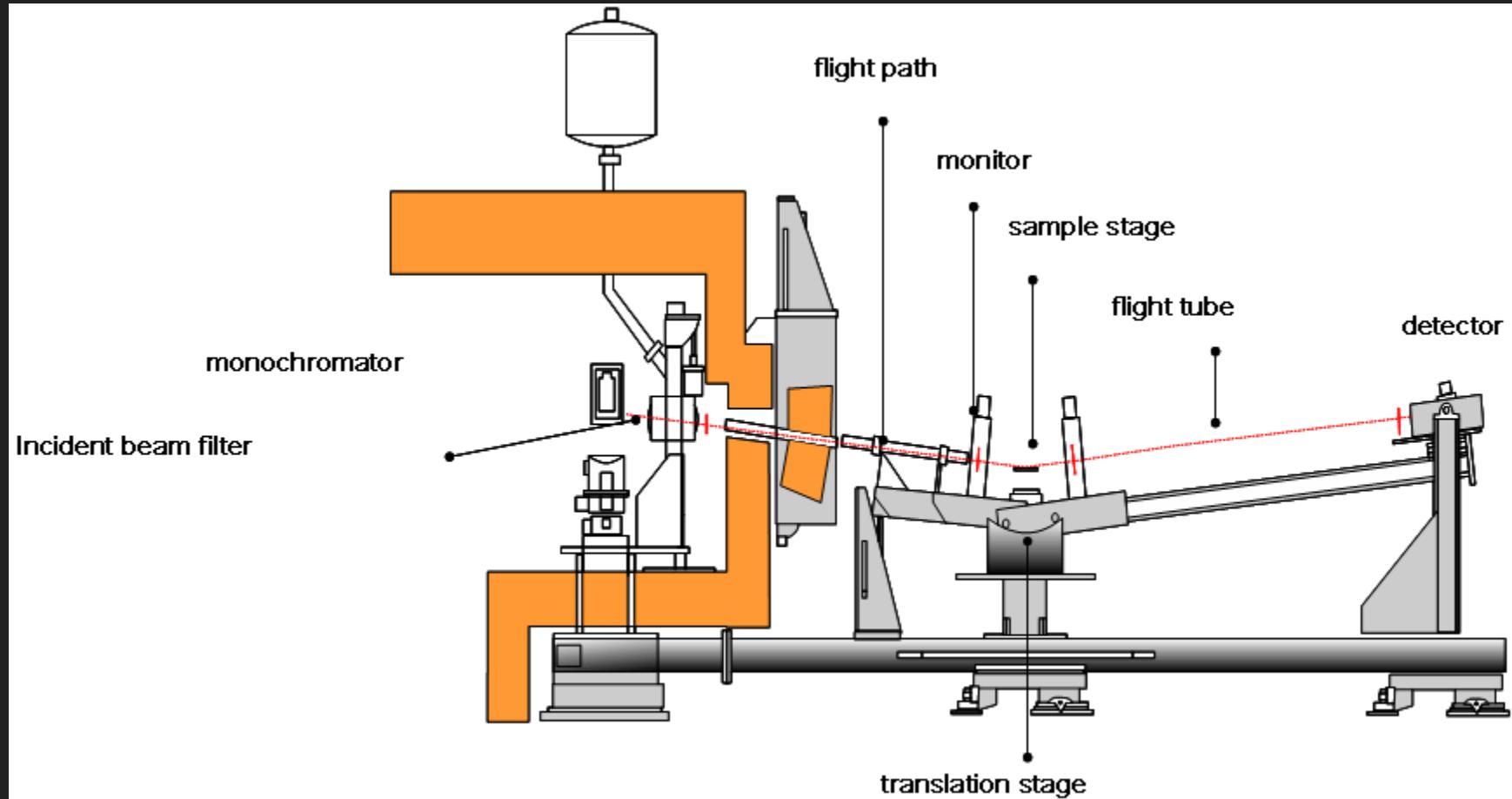
## ○ dPC/PMMA/Si

- Step 1 Remove the silicon oxide layer from the Si substrate  
(First “piranha” solution (70/30 v/v H<sub>2</sub>SO<sub>4</sub> (50%)/ H<sub>2</sub>O<sub>2</sub> (30%)) and then 5 % HF solution)
- Step 2 Spin coat a PMMA layer on the cleaned Si wafer
- Step 3 Spin coat a dPC layer on another Si wafer
- Step 4 Float the dPC film on the water surface then pick it up on the wafer with PMMA layer



# NR measurement

## ○ instrument



# Data reduction

→ <https://reductus.nist.gov/>  
→ Template \_ unpolarized  
→ ncnrdata/ng7/201608/22440/data/1-4E3

## Specular

7204 (as-cast)

7419 (20 min at 135 °C)

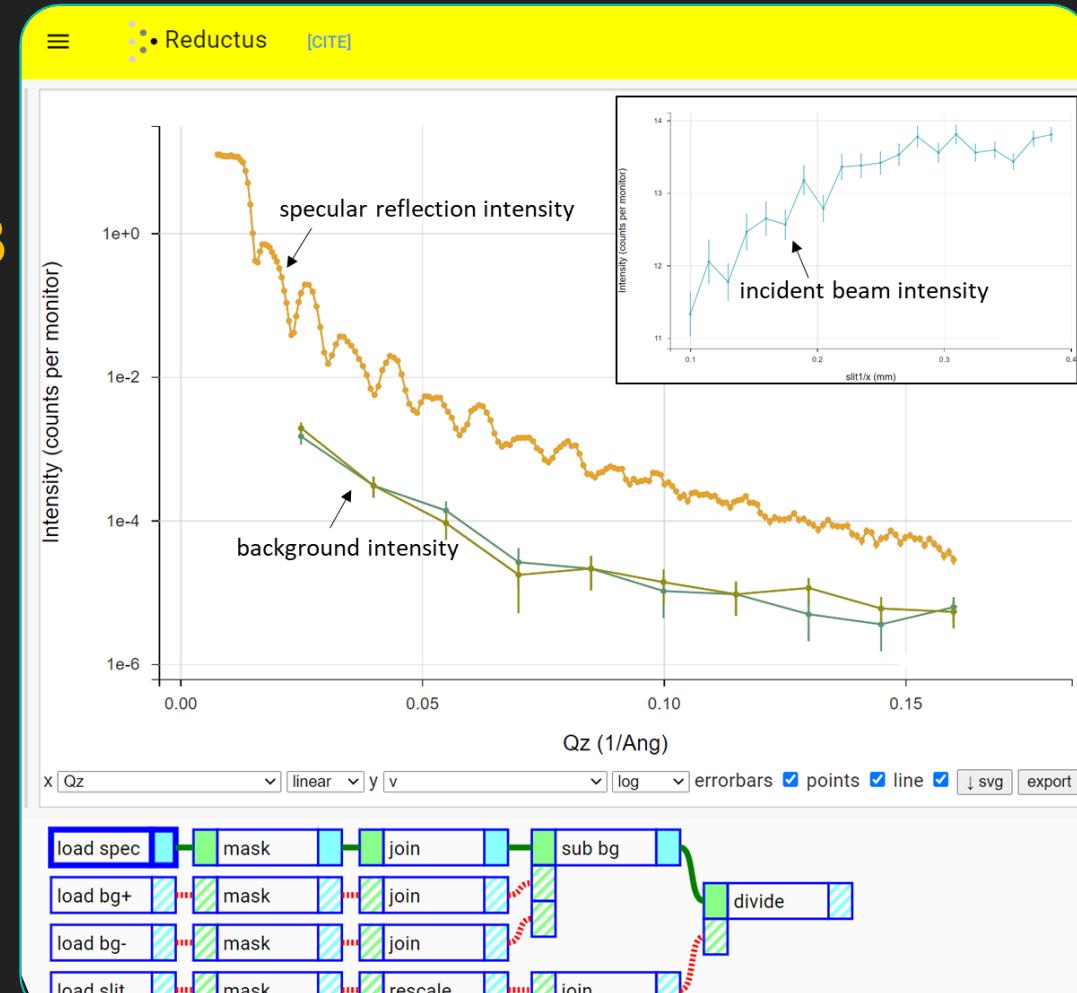
7619 (65 min at 135 °C)

## Background

7205, 7206 (+, -)

## Slits

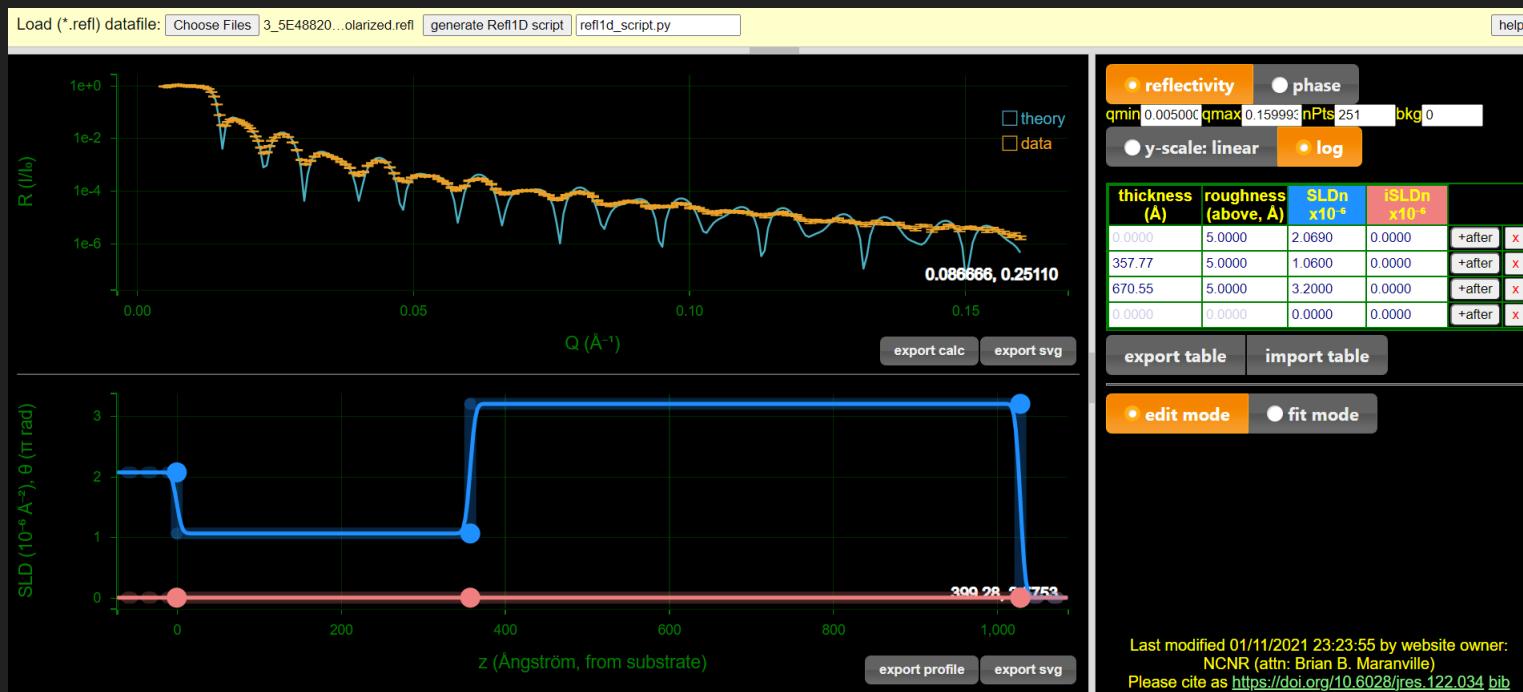
7127 (35 mm beam through air)



# Data fitting

## ○ Generate refl1D script

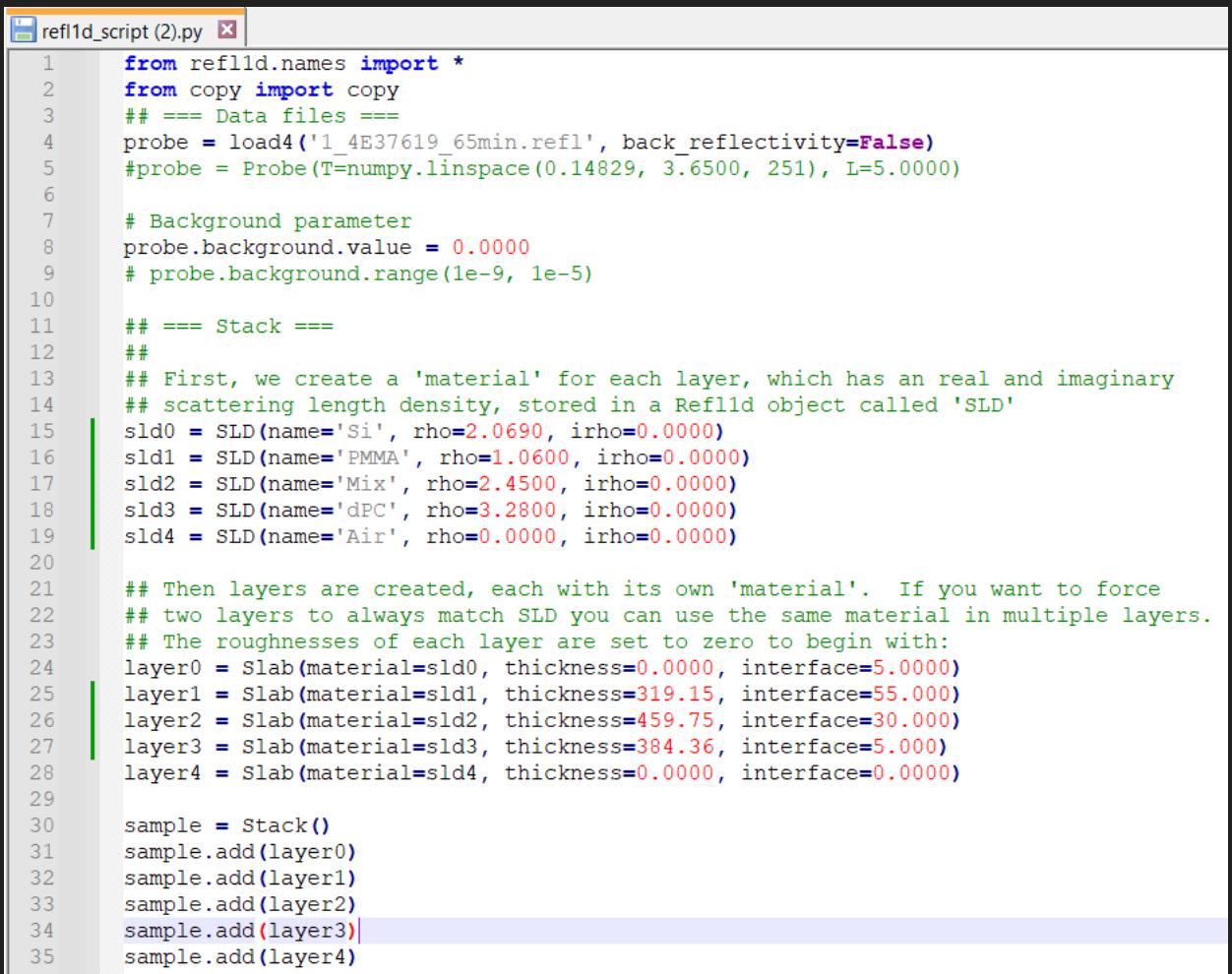
<https://ncnr.nist.gov/instruments/magik/calculators/reflectivity-calculator.html>



# Data fitting

## ○ Edit refl1D script

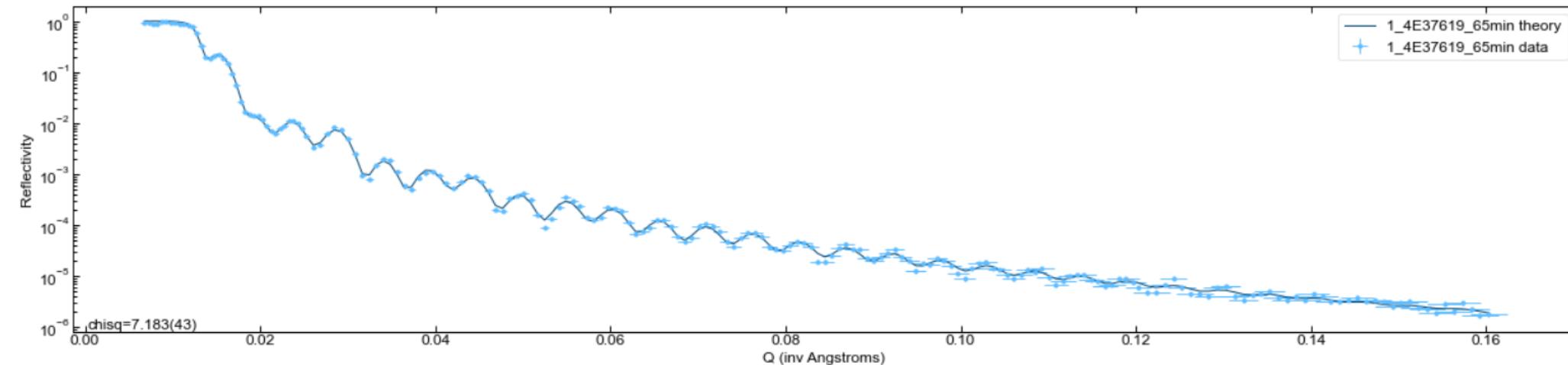
- Load data
- Stack layers
- Set constraints
- Fit parameters



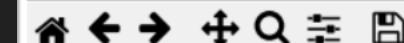
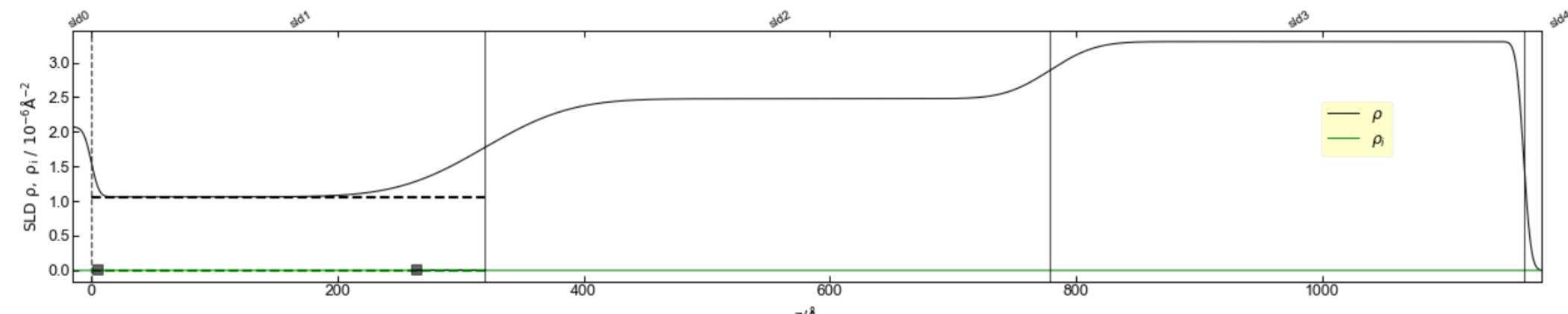
```
refl1d_script (2).py
1  from refl1d.names import *
2  from copy import copy
3  ## === Data files ===
4  probe = load4('1_4E37619_65min.refl', back_reflectivity=False)
#probe = Probe(T=numpy.linspace(0.14829, 3.6500, 251), L=5.0000)
6
7  # Background parameter
8  probe.background.value = 0.0000
# probe.background.range(1e-9, 1e-5)
9
10 ## === Stack ===
11 ##
12 ## First, we create a 'material' for each layer, which has an real and imaginary
13 ## scattering length density, stored in a Refl1d object called 'SLD'
14 sld0 = SLD(name='Si', rho=2.0690, irho=0.0000)
15 sld1 = SLD(name='PMMA', rho=1.0600, irho=0.0000)
16 sld2 = SLD(name='Mix', rho=2.4500, irho=0.0000)
17 sld3 = SLD(name='dPC', rho=3.2800, irho=0.0000)
18 sld4 = SLD(name='Air', rho=0.0000, irho=0.0000)
19
20 ## Then layers are created, each with its own 'material'. If you want to force
21 ## two layers to always match SLD you can use the same material in multiple layers.
22 ## The roughnesses of each layer are set to zero to begin with:
23 layer0 = Slab(material=sld0, thickness=0.0000, interface=5.0000)
24 layer1 = Slab(material=sld1, thickness=319.15, interface=55.000)
25 layer2 = Slab(material=sld2, thickness=459.75, interface=30.000)
26 layer3 = Slab(material=sld3, thickness=384.36, interface=5.000)
27 layer4 = Slab(material=sld4, thickness=0.0000, interface=0.0000)
28
29 sample = Stack()
30 sample.add(layer0)
31 sample.add(layer1)
32 sample.add(layer2)
33 sample.add(layer3)
34 sample.add(layer4)
35 sample.add(layer4)
```



Reflectivity X



Profile X Parameters Summary Log Convergence Uncertainty Correlations Parameter Trace Model Uncertainty



# Conclusion