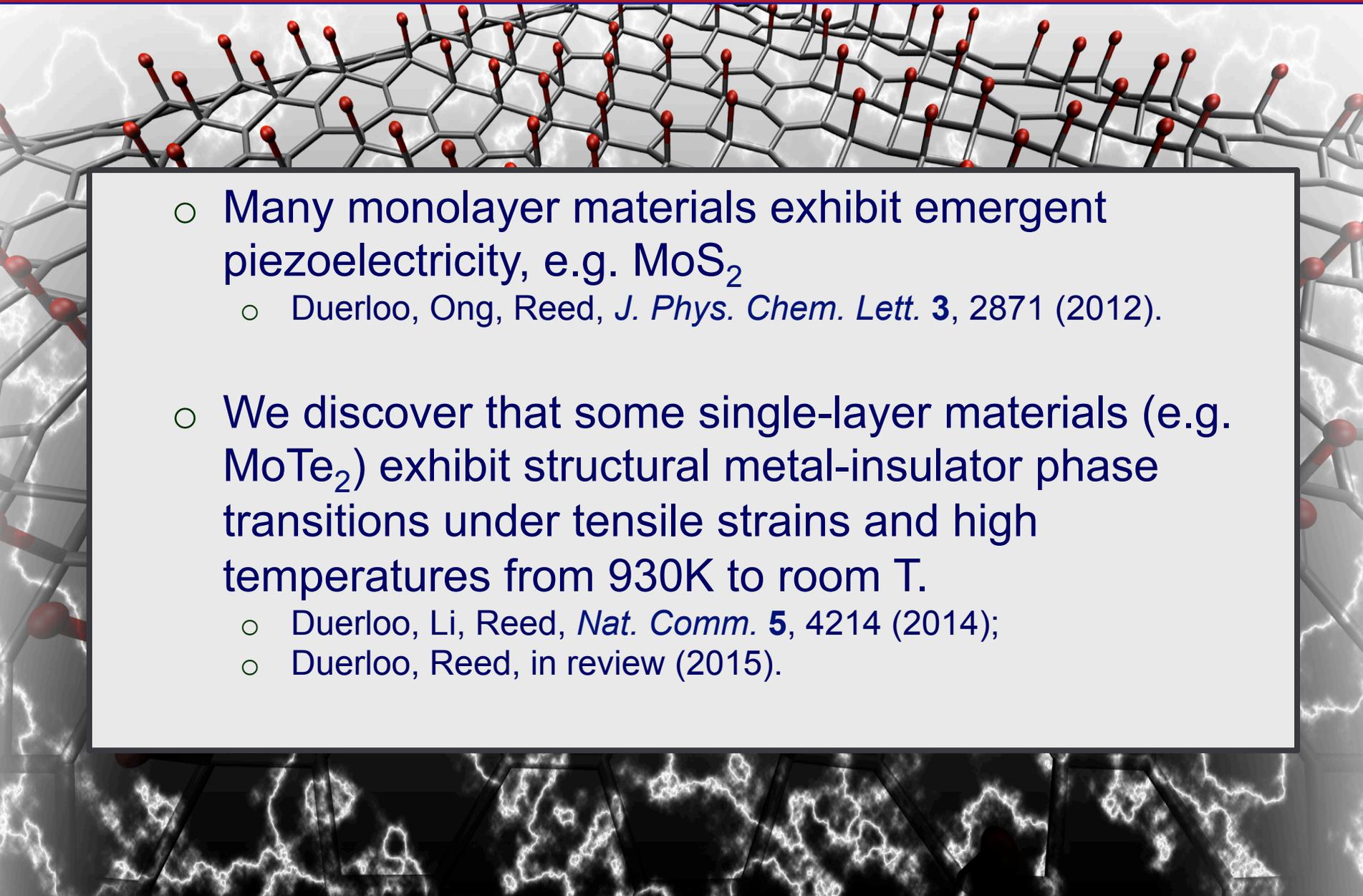


# Phase Change and Piezoelectric Properties of Two-Dimensional Materials

**April 16, 2015**

**Karel-Alexander Duerloo, Yao Li, Yao Zhou, Evan Reed**  
*Department of Materials Science and Engineering*  
*Stanford University*

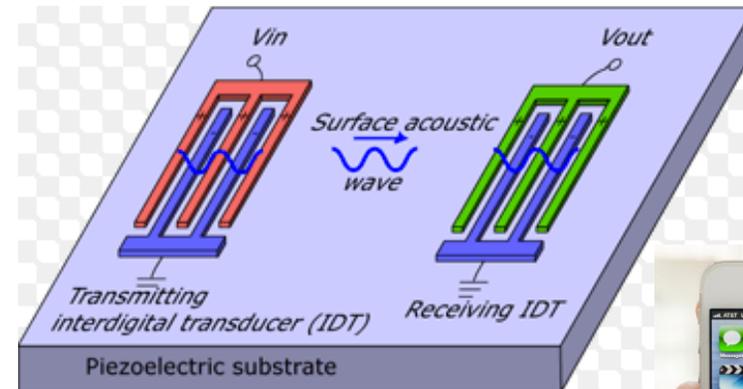


- 
- Many monolayer materials exhibit emergent piezoelectricity, e.g.  $\text{MoS}_2$ 
    - Duerloo, Ong, Reed, *J. Phys. Chem. Lett.* **3**, 2871 (2012).
  - We discover that some single-layer materials (e.g.  $\text{MoTe}_2$ ) exhibit structural metal-insulator phase transitions under tensile strains and high temperatures from 930K to room T.
    - Duerloo, Li, Reed, *Nat. Comm.* **5**, 4214 (2014);
    - Duerloo, Reed, in review (2015).

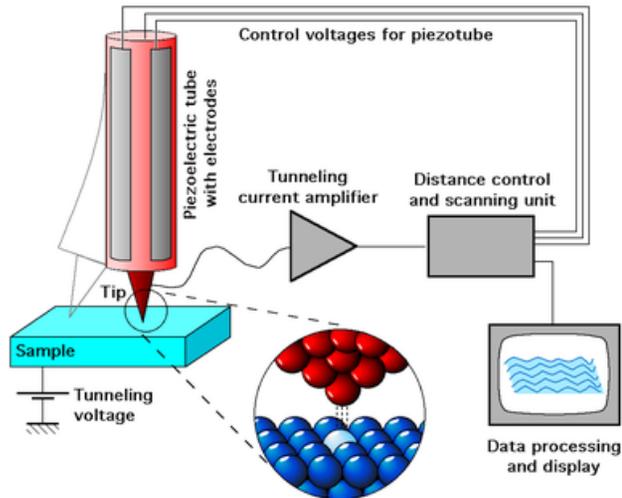
## Stress Sensors



## Acoustic transducers for signal processing



## Scanning Tunneling Microscope (STM)



## Injet Printing



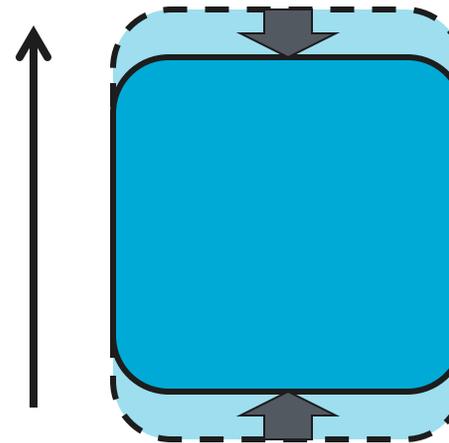
Piezoelectric Effect

$$P_i = e_{ijk} \varepsilon_{jk}$$



Converse Piezoelectric Effect

$$\varepsilon_{ij} = d_{ijk} E_k$$



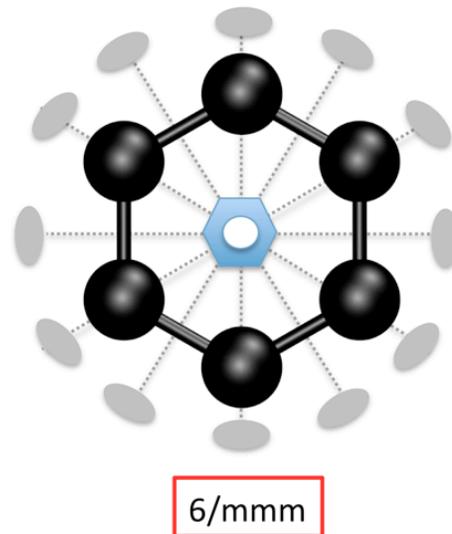
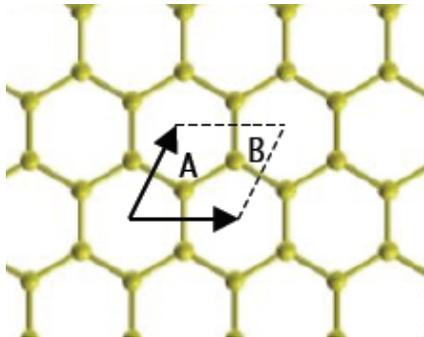
Electric  
Field

Piezoelectric materials must exhibit:

1. An electronic bandgap
2. A lack of centrosymmetry

Inversion symmetry of a crystal  $\Rightarrow d_{ijk} = (-1)^3 d_{ijk} = -d_{ijk}$   
 So  $d_{ijk} = 0$  for crystals with inversion symmetry!

## *graphene*

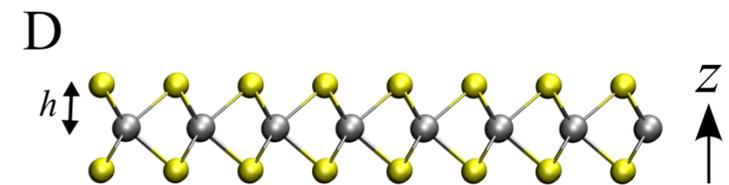
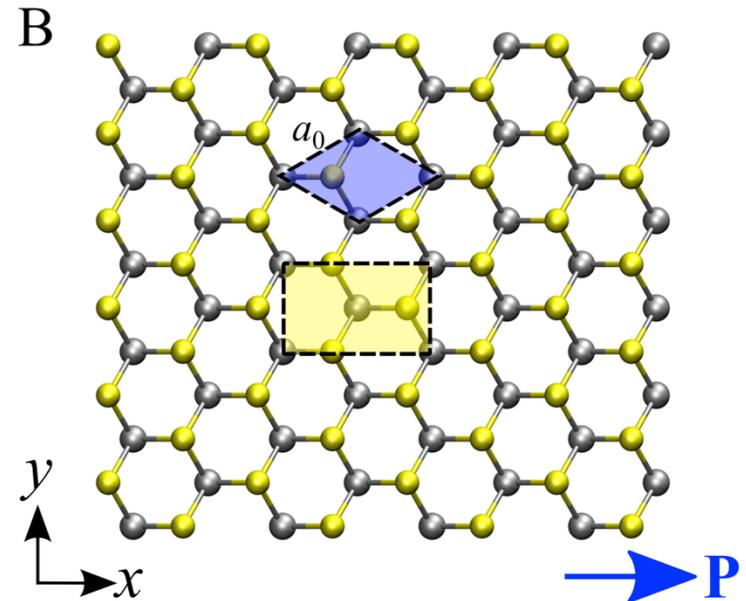


- ***Inversion symmetry => non-piezoelectric***
- ***Semi-metallic character => non-piezoelectric***

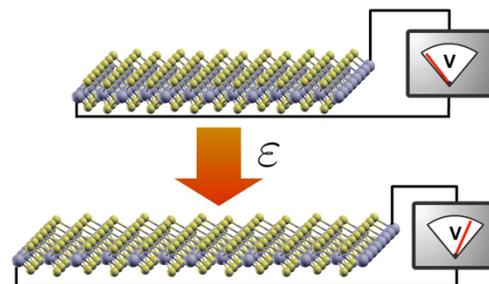
## Transition Metal Dichalcogenides: MoS<sub>2</sub>, MoSe<sub>2</sub>, MoTe<sub>2</sub>, WS<sub>2</sub>, WSe<sub>2</sub>

Trigonal prismatic structure:

- ✓ Semiconducting ( $E_{\text{gap}} \sim 1\text{-}2 \text{ eV}$ )
- ✓ Not centrosymmetric
- ✓ 3m point group leads to non-zero  $d_{11}$  and  $e_{11}$  coefficients



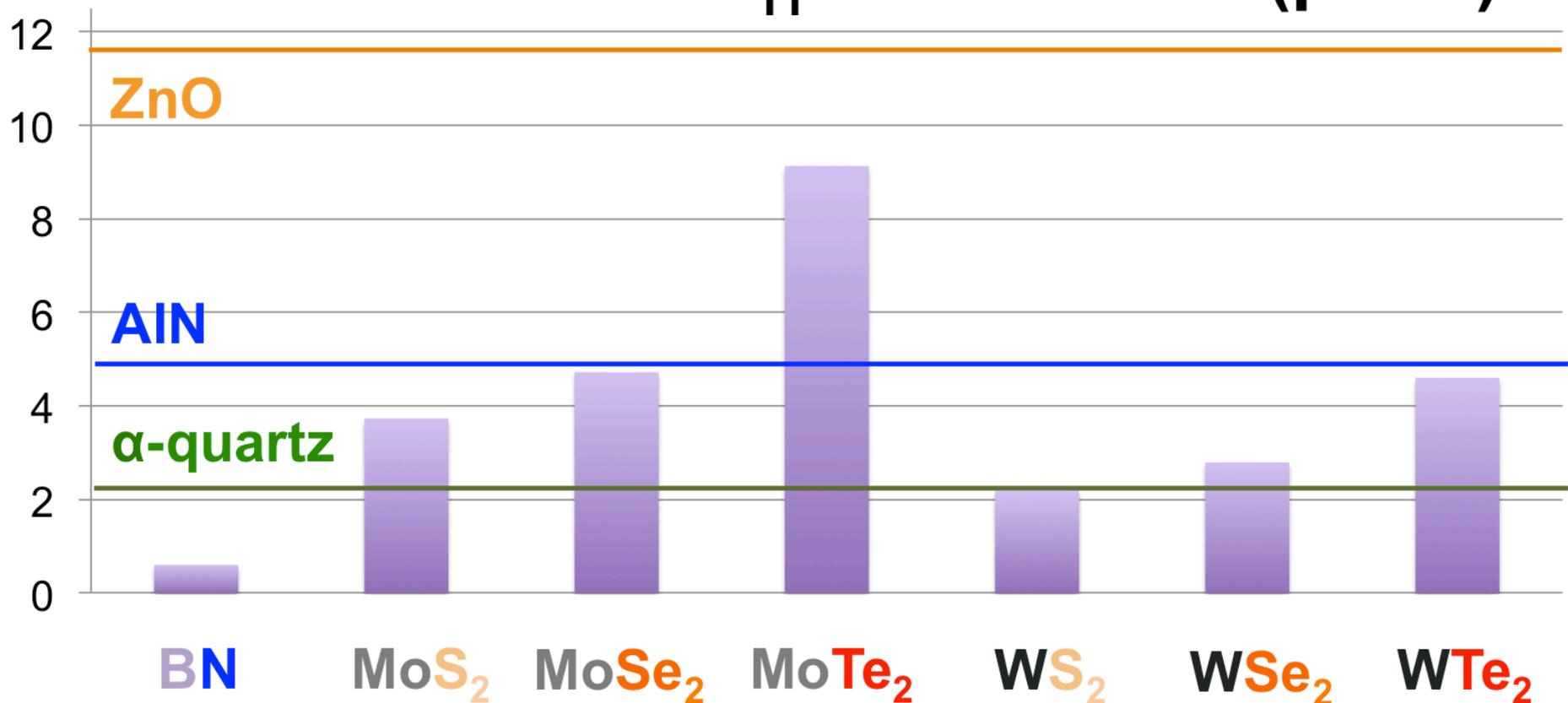
$$\begin{bmatrix} \epsilon_{xx} \\ \epsilon_{yy} \\ \epsilon_{xy} \end{bmatrix} = \begin{bmatrix} d_{11} & 0 & 0 \\ -d_{11} & 0 & 0 \\ 0 & -d_{11} & 0 \end{bmatrix} \begin{bmatrix} E_x \\ E_y \\ E_z \end{bmatrix}$$



# WE DISCOVER THAT A VARIETY OF TMDS HAVE SIGNIFICANT PIEZOELECTRIC EFFECTS



## Calculated $d_{11}$ coefficients (pm/V)



Piezo-coefficients of trigonal prismatic TMD structures are comparable to bulk wurtzite structures

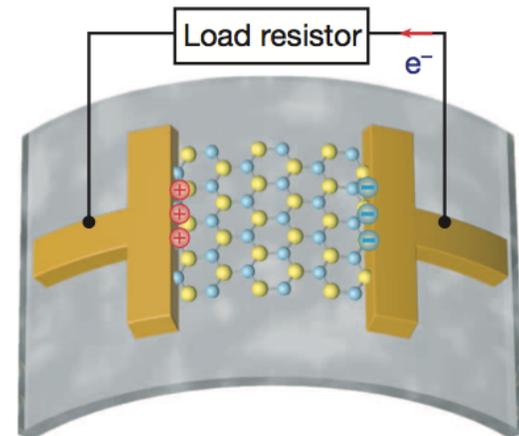
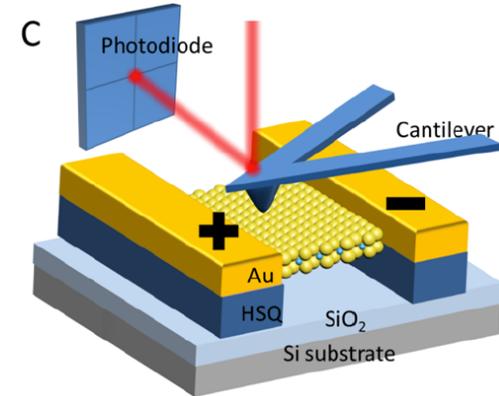
K.-A. Duerloo, M. T. Ong, E. J. Reed.,  
J. Phys. Chem. Lett. 3, 2871 (2012).

# PIEZOELECTRICITY IN 2D MATERIALS HAS RECENTLY BEEN OBSERVED



“**Observation of Piezoelectricity in monolayer MoS<sub>2</sub>**,” Zhu, Wang, Xiao, Liu, Xiong, Wong, Ye, Yin, Zhang, *Nature Nanotechnology* (2014).

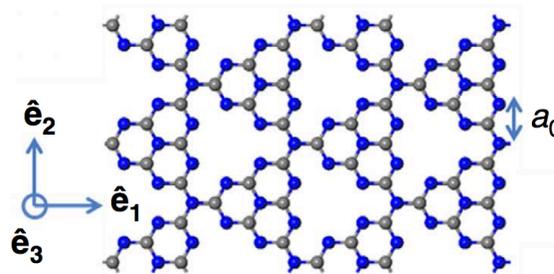
Reported  $e_{11}$  within 20% of predicted.



“**Piezoelectricity of single atomic layer MoS<sub>2</sub>**,” Wu, Wang, Hone, Wang *et al.*, *Nature* (2014).

**Piezoelectricity in C<sub>3</sub>N<sub>4</sub> few layers:**

Zelisko, *et al*, *Nature Communications* (2014).

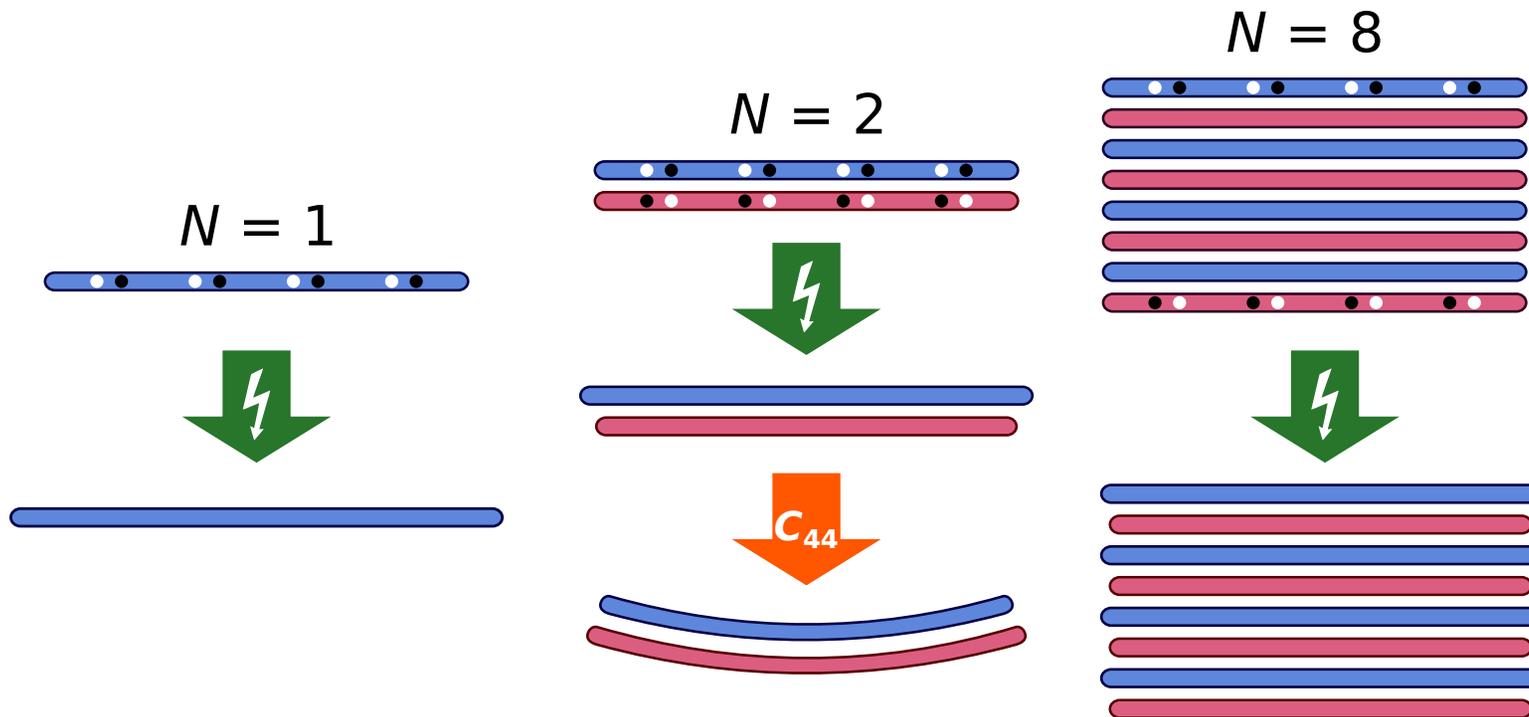




# BILAYER EMERGENT ELECTROMECHANICAL CURVATURE

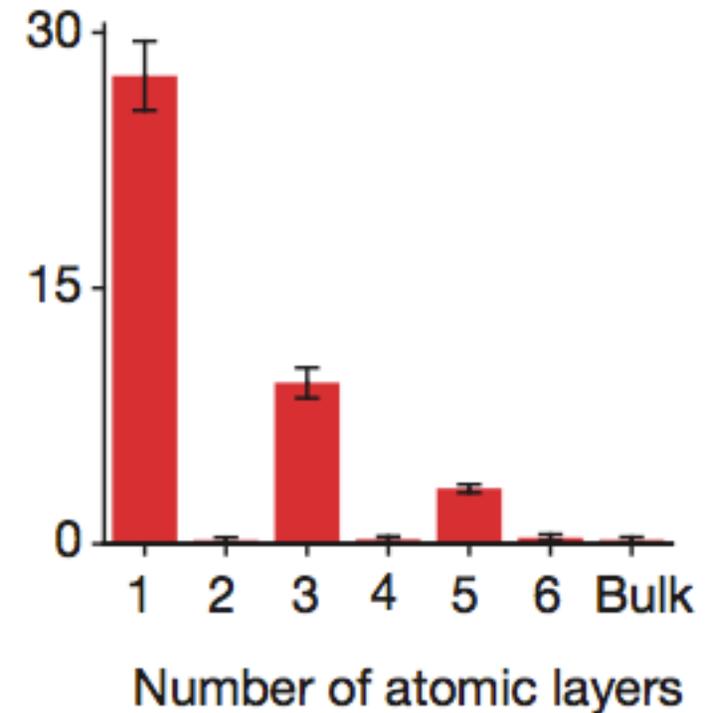
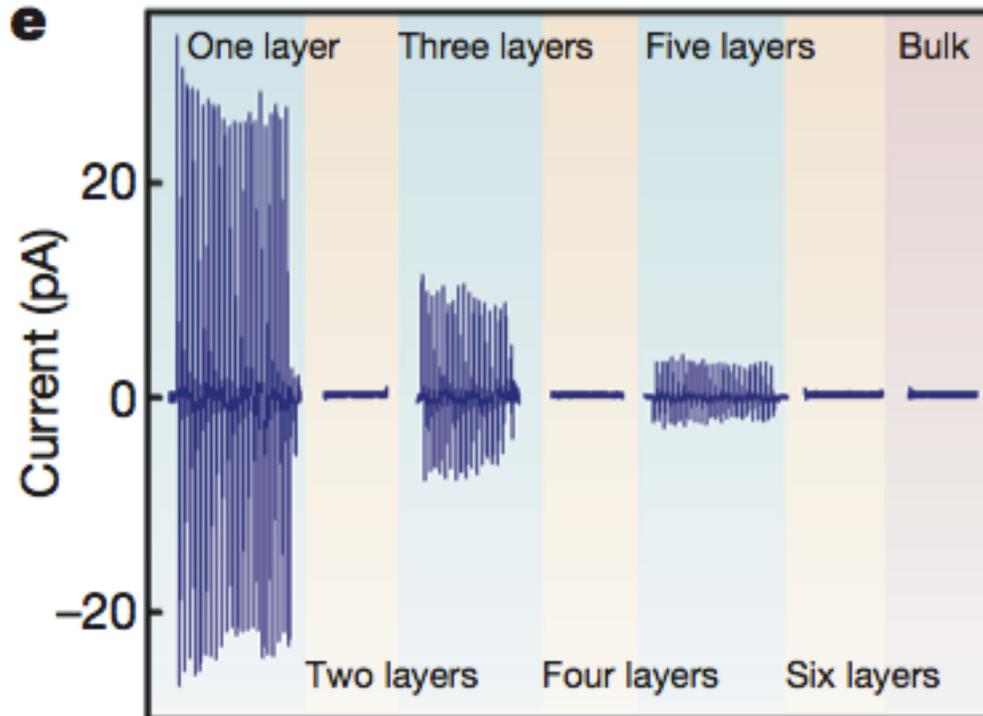


We find that TMDC monolayers are piezoelectric while their bulk host crystals exhibit an inversion center and are therefore not piezoelectric!

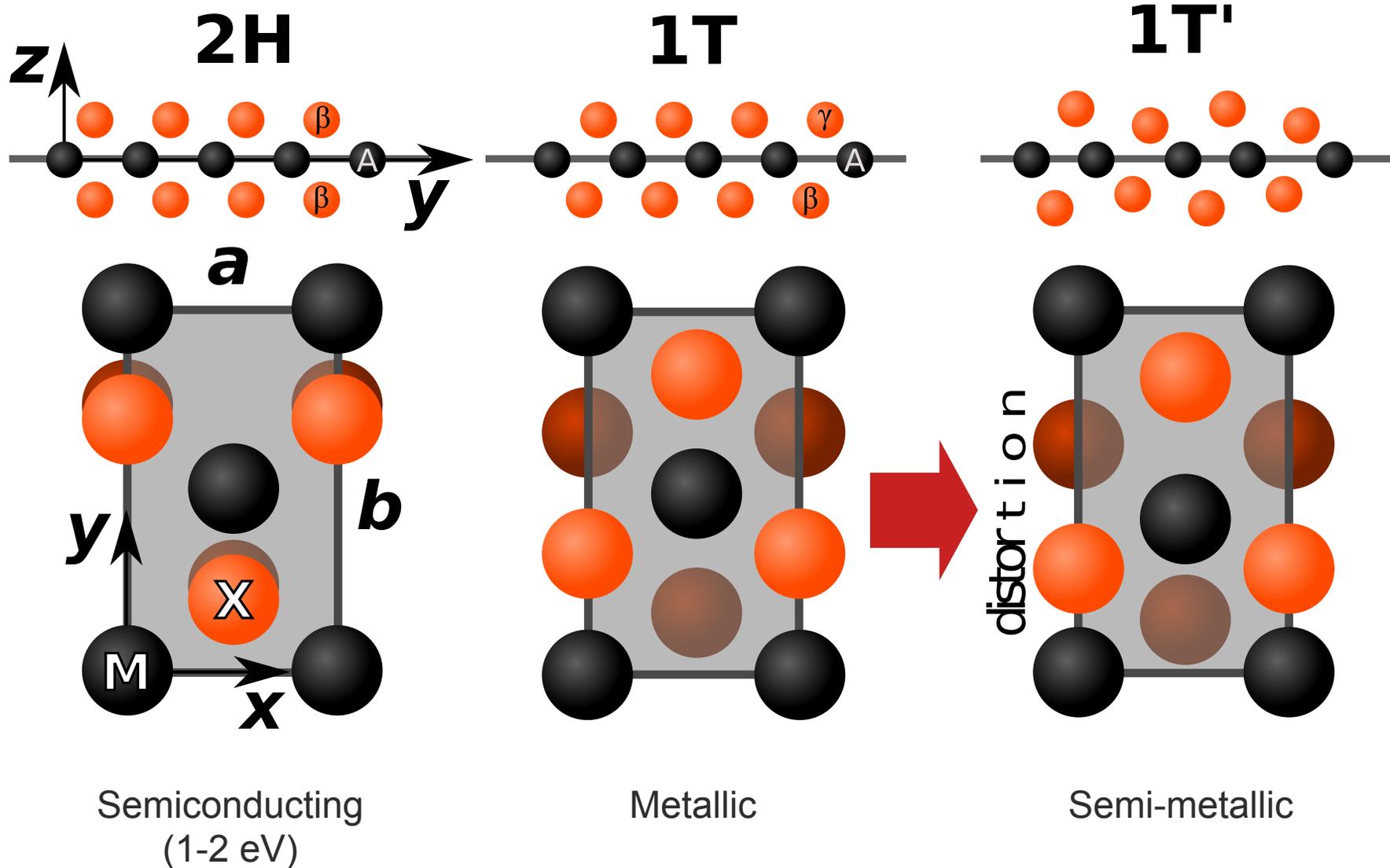


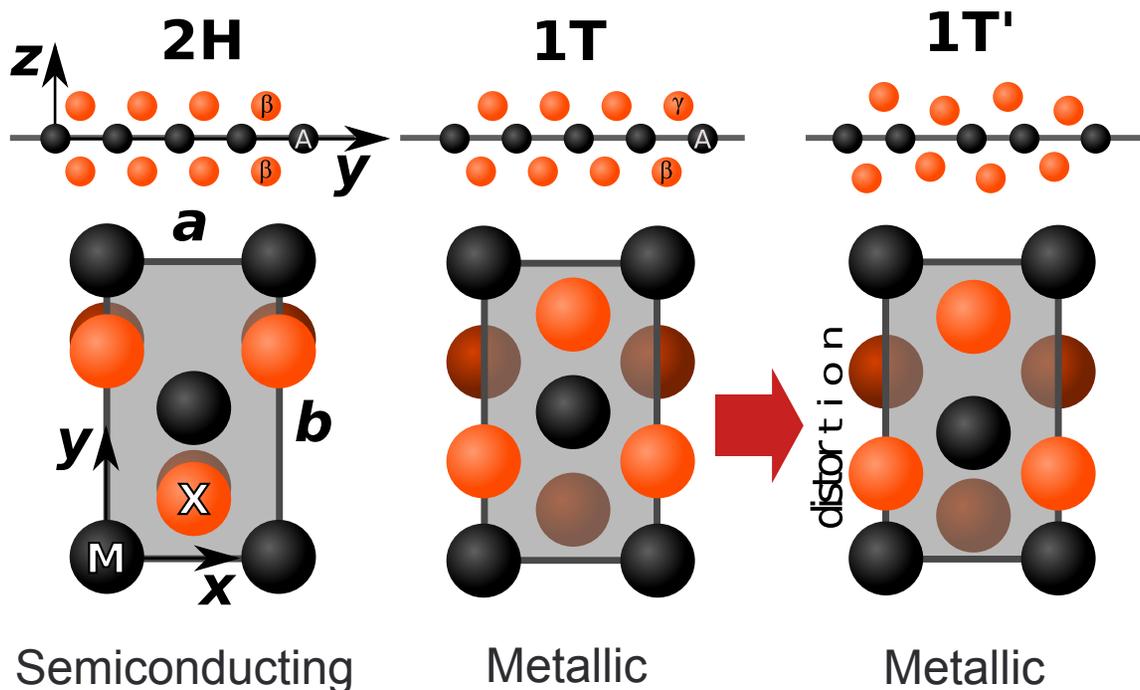
We predict bilayer BN exhibits an electromechanical curvature effect.

# PIEZOELECTRIC EFFECTS OBSERVED ONLY FOR ODD NUMBERS OF LAYERS



**Piezoelectricity of single atomic layer MoS<sub>2</sub>...** Wu, Wang, Hone, Wang *et al.*, *Nature* (2014).

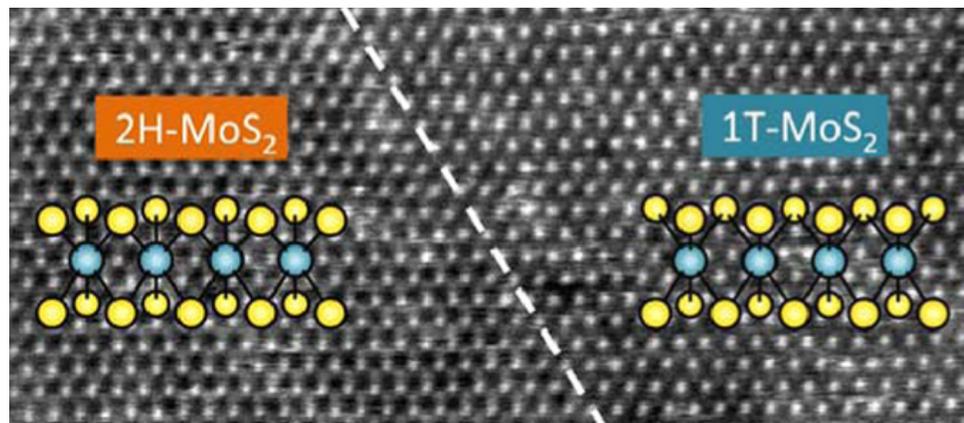


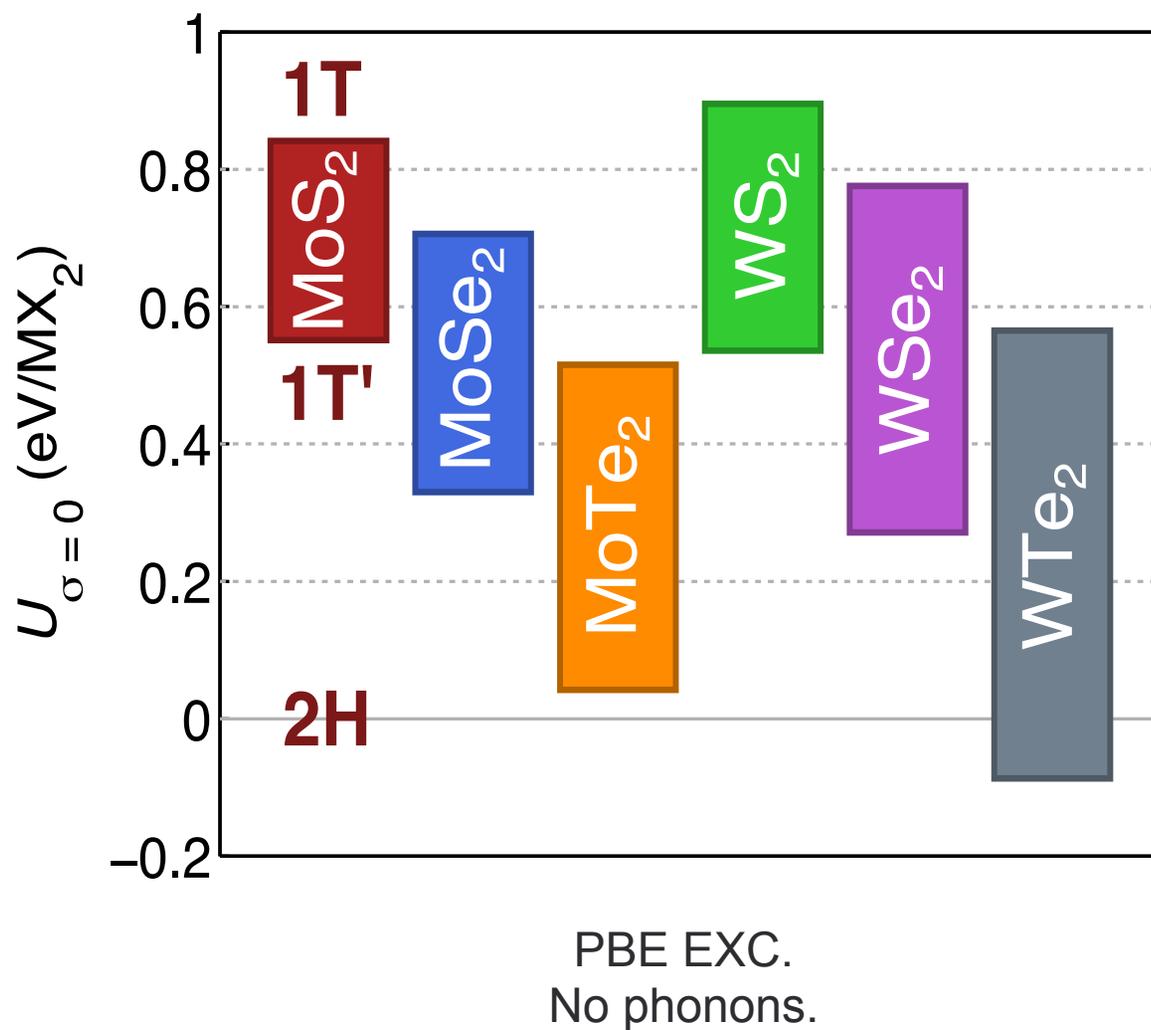


Can the phases of monolayers be engineered and employed in devices?

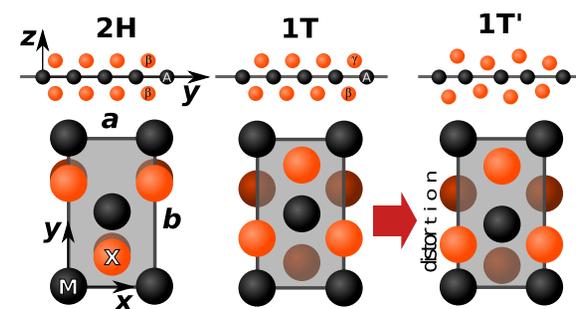
Two phases have been observed in chemically exfoliated  $\text{MoS}_2$  and  $\text{WS}_2$ .

Eda et al, ACS Nano 6, 7311 (2012);  
Voiry et al, Nat. Mat. (2013).



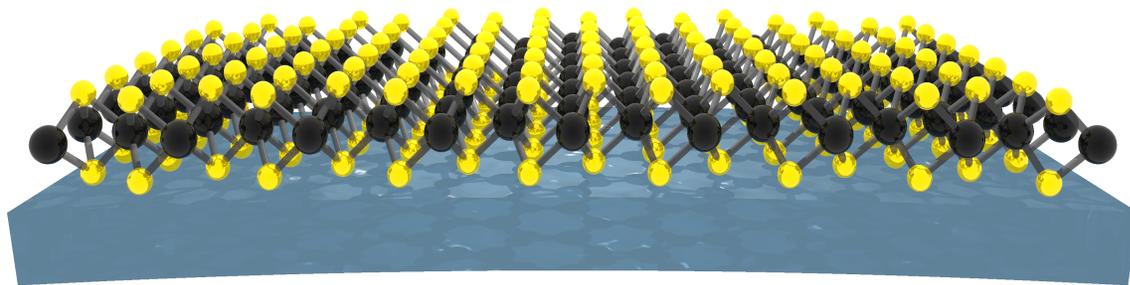


Our semi-local DFT calculations indicate MoTe<sub>2</sub> and WTe<sub>2</sub> exhibit the smallest 2H-1T' energy difference.

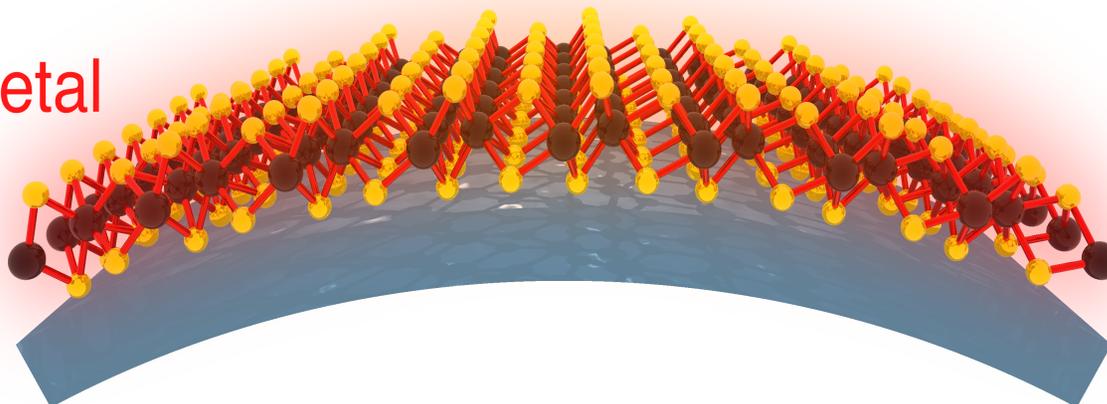


# CAN TENSILE STRAIN CAUSE A STRUCTURAL PHASE TRANSITION?

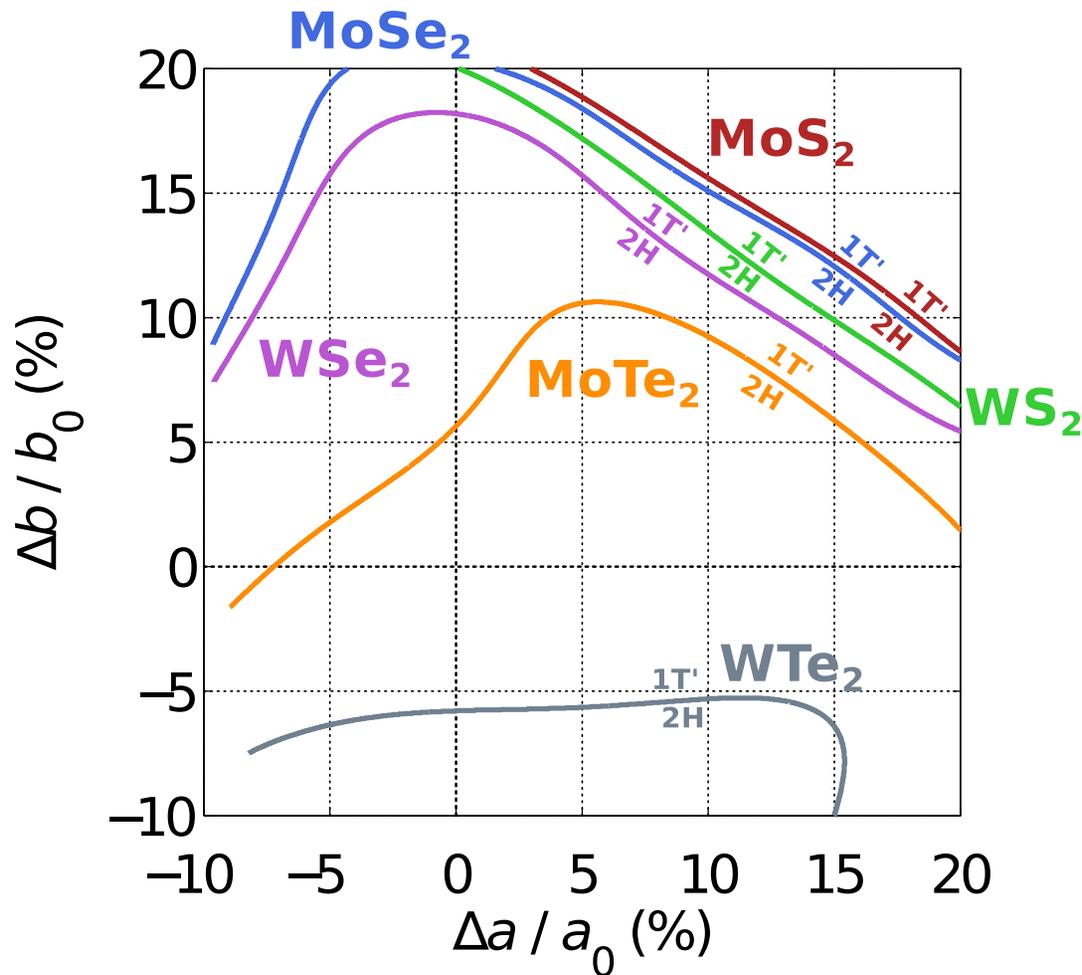
semiconductor



metal

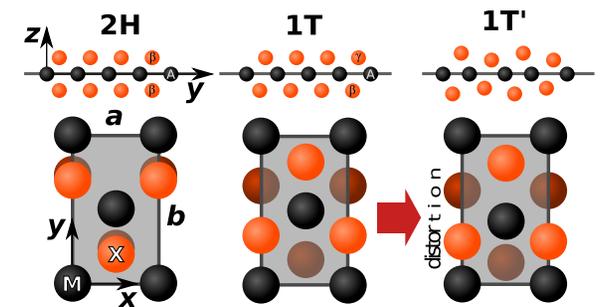


Our DFT/PBE calculations of TMD monolayer phase boundaries in strain.

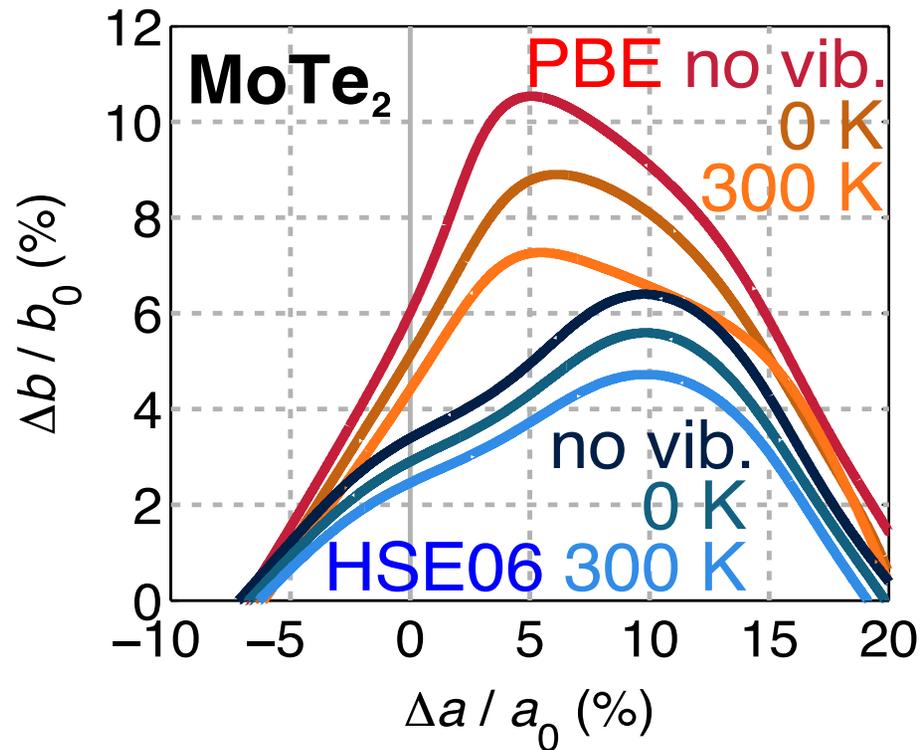


Energy calculations on a 5x5 grid in (a,b) lattice constants. Lagrange interpolation for phase boundaries.

Tensile strain of 6% along b axis crosses phase boundary in MoTe<sub>2</sub>.



Duerloo, Li, Reed, Nature Communications, (2014).

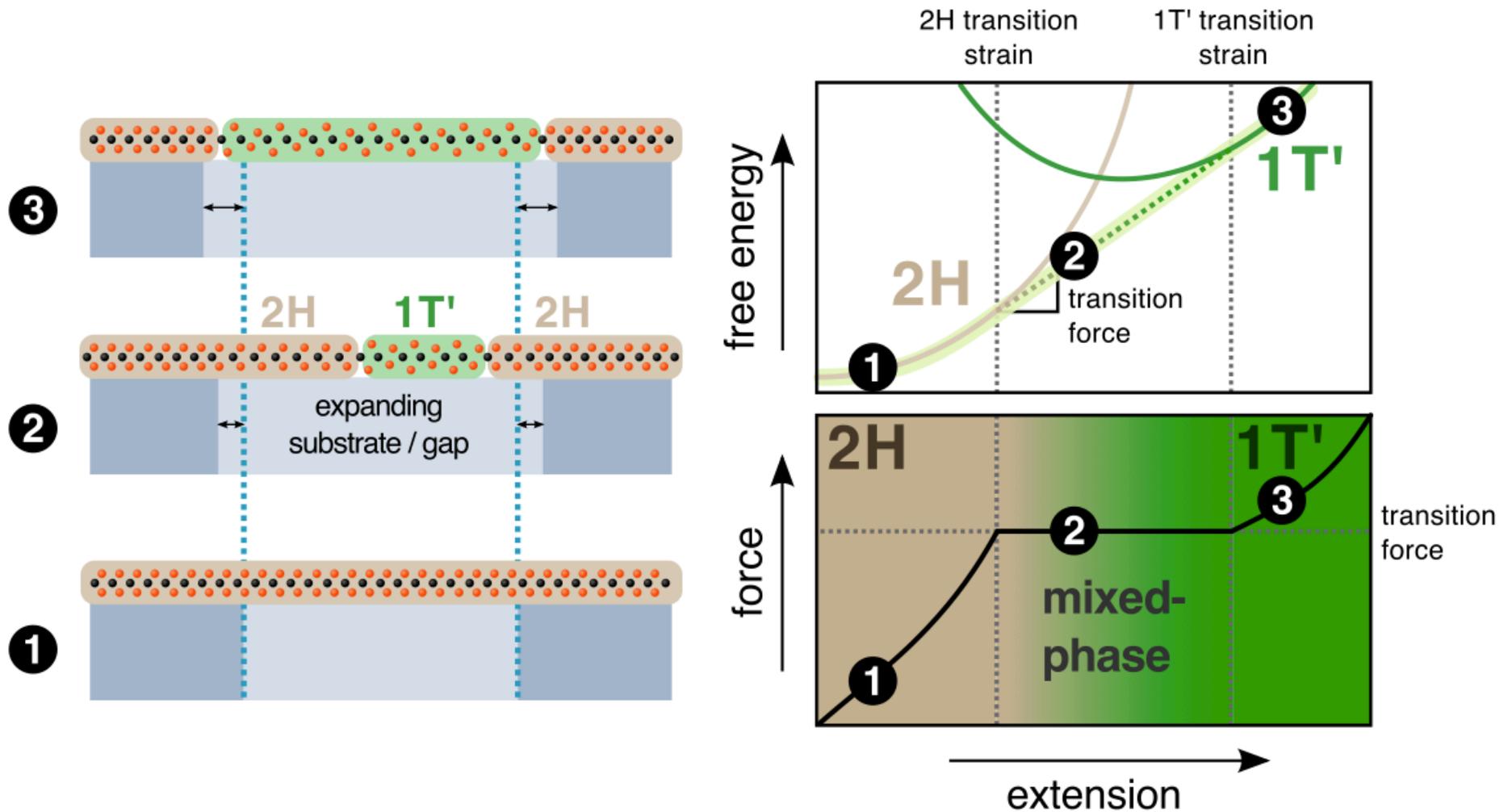


- Hybrid exchange (HSE06) moves phase boundary closer to ambient conditions
- Incorporation of entropic effects ( $F=E-TS$ ) accomplished using quasiharmonic approximation with computed phonon bands

$$F(a, b) \approx U_{\text{crystal}}(a, b) + \sum_i \left[ \frac{1}{2} \hbar \omega_i(a, b) + k_B T \ln(1 - e^{-\hbar \omega_i(a, b) / k_B T}) \right]$$

HSE06 with room T vibrations predict phase boundary within 3% tensile strain in  $\text{MoTe}_2$ .

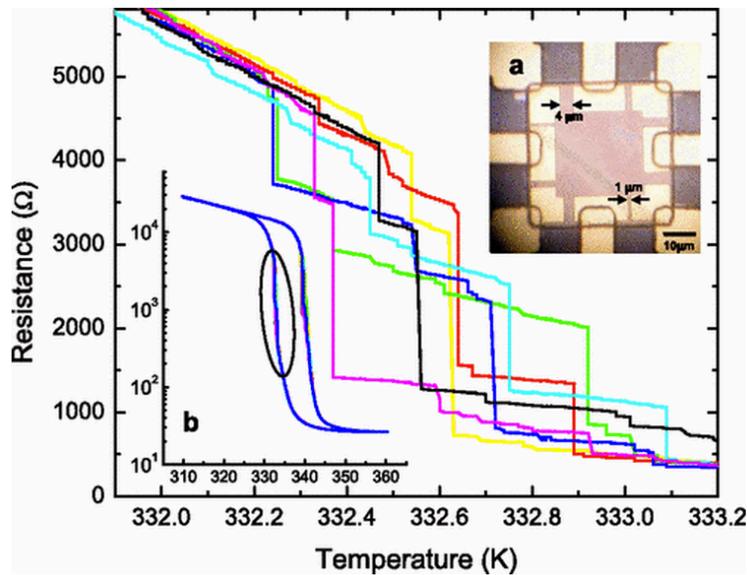
# STRAIN INDUCED STRUCTURAL TRANSITION FROM 2H TO 1T'



Duerloo, Li, Reed, Nature Communications, (2014).

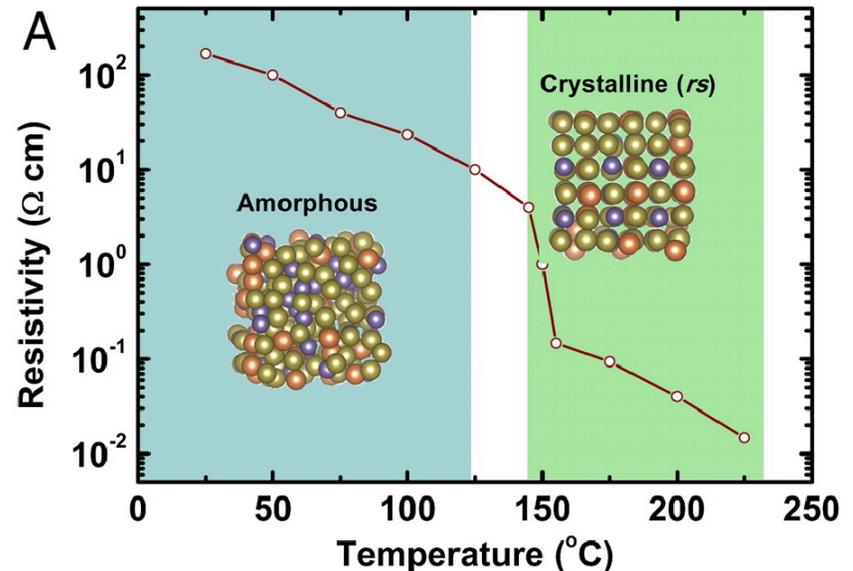
New materials are needed to mitigate escalating power requirements for electronic devices.

Metal-oxides:  $\text{VO}_2$



Sharoni *et al.* *Phys. Rev. Lett.* **101**, 026404 (2008)

Chalcogenide alloys:  
 $\text{Ge}_2\text{Sb}_2\text{Te}_5$  (GST)



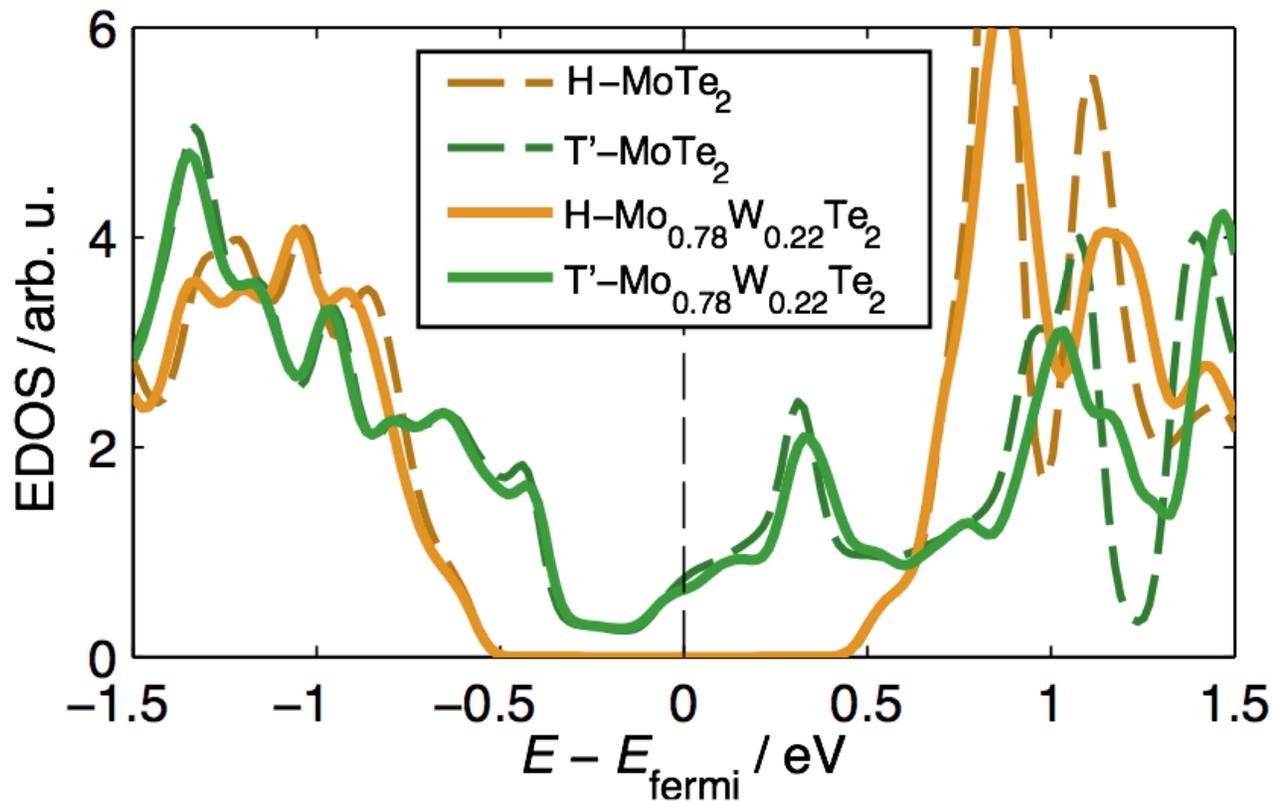
Xu *et al.*, *PNAS.* **109**, 1055 (2012)

Suitable phase change materials are rare animals. We discover a promising new material.

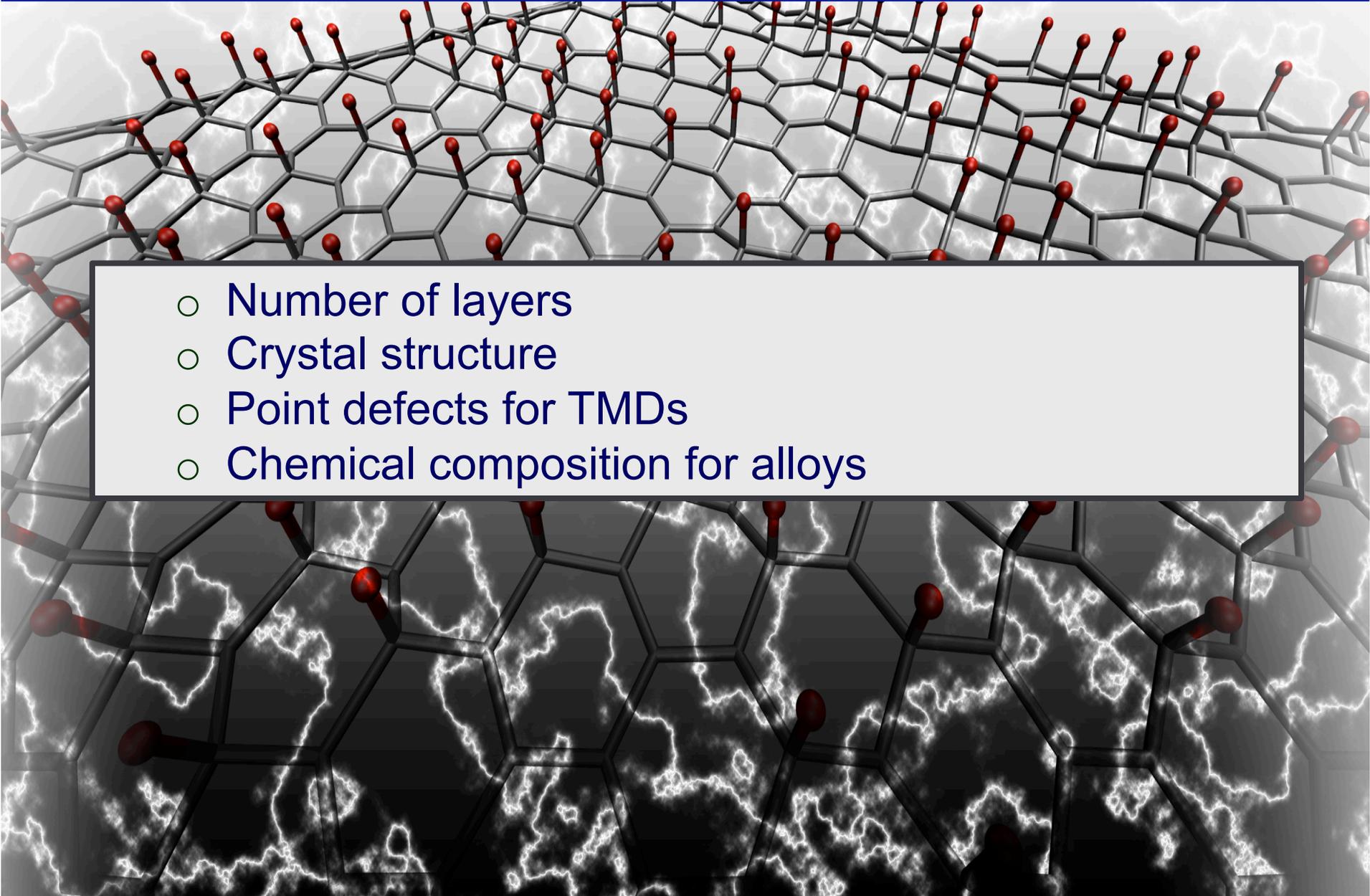
Application spaces:

- Information and energy storage
- Low power electronics
- Infrared technologies

Kohn-Sham (single particle) electronic density of states for H and T' MoTe<sub>2</sub>.

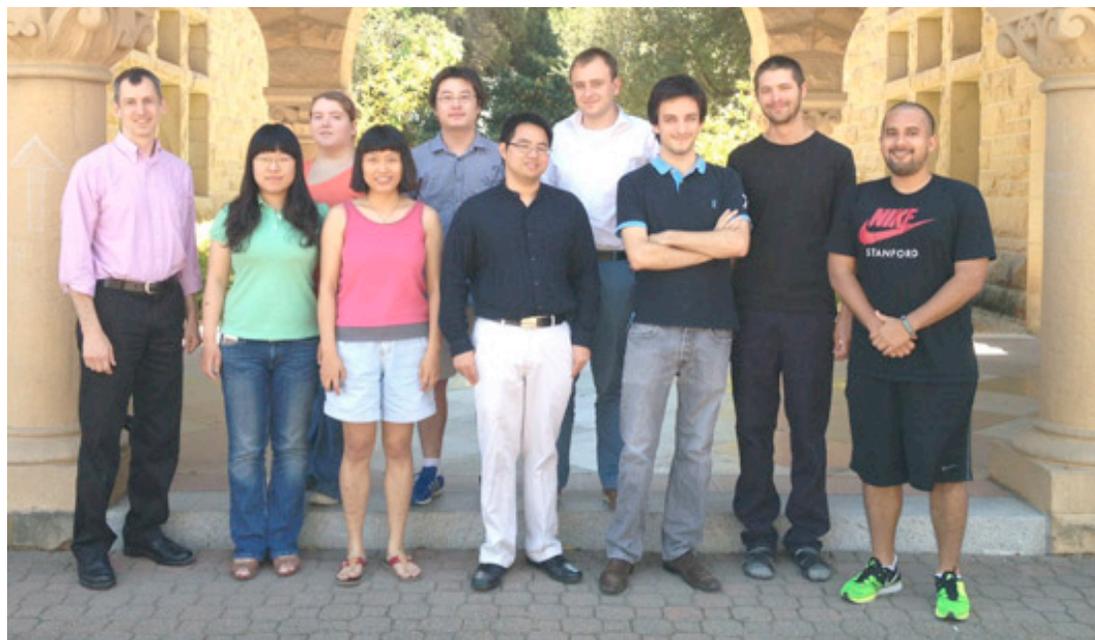


Large predicted electronic changes across the phase transition provide utility for electronic and infrared devices.

- 
- Number of layers
  - Crystal structure
  - Point defects for TMDs
  - Chemical composition for alloys



# ACKNOWLEDGEMENTS



Karel-Alexander Duerloo  
Mitchell Ong  
Yao Li  
Yao Zhou



This work is supported by:

- Army High Performance Computing Research Center (AHPARC)
- DARPA N66001-12-1-4236
- NSF EECS-1436626 and DMR-1455050
- National Energy Research Science Computing Center (NERSC)

- Many monolayer materials exhibit emergent piezoelectricity, e.g.  $\text{MoS}_2$ 
  - Duerloo, Ong, Reed, *J. Phys. Chem. Lett.* **3**, 2871 (2012).
- We discover that some single-layer materials (e.g.  $\text{MoTe}_2$ ) exhibit structural metal-insulator phase transitions under tensile strains and high temperatures from 930K to room T.
  - Duerloo, Li, Reed, *Nat. Comm.* **5**, 4214 (2014);
  - Duerloo, Reed, in review (2015).