

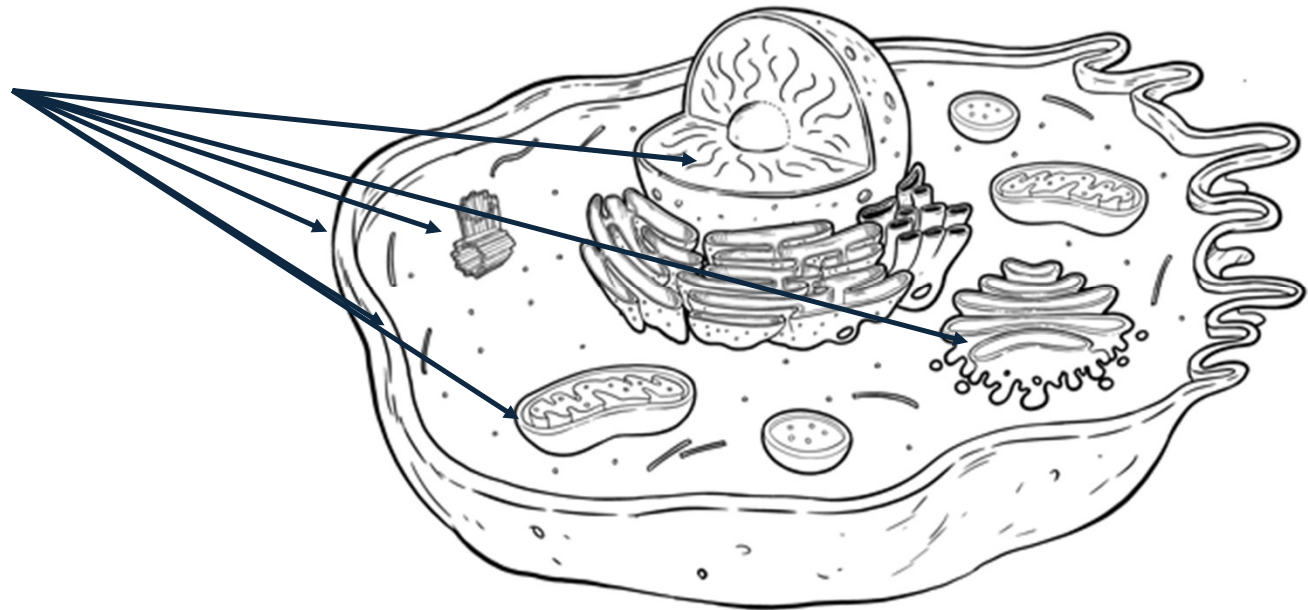
Simulating the effects of charged lipids on bilayer area compressibility

Harrie Ha

Mentors: James “Shea” Fitzgerald and Elizabeth Kelley

Membranes Define Boundaries

Anything you see here that has a boundary has a lipid membrane!



The core purpose of the membrane is to define boundaries and keep the cell functional.

Membranes are vital to cell processes like cell division and diffusion. However, these processes must still occur **while** maintaining a strong boundary EX: Blood cells need to be flexible enough to flow, but not break!

Q: How do membranes achieve this?



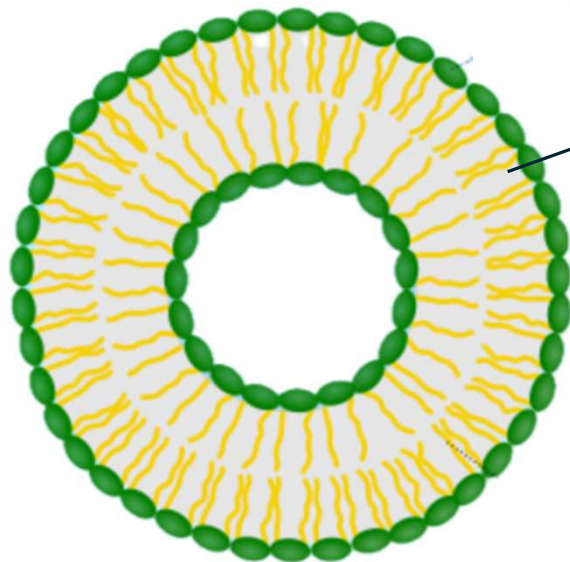
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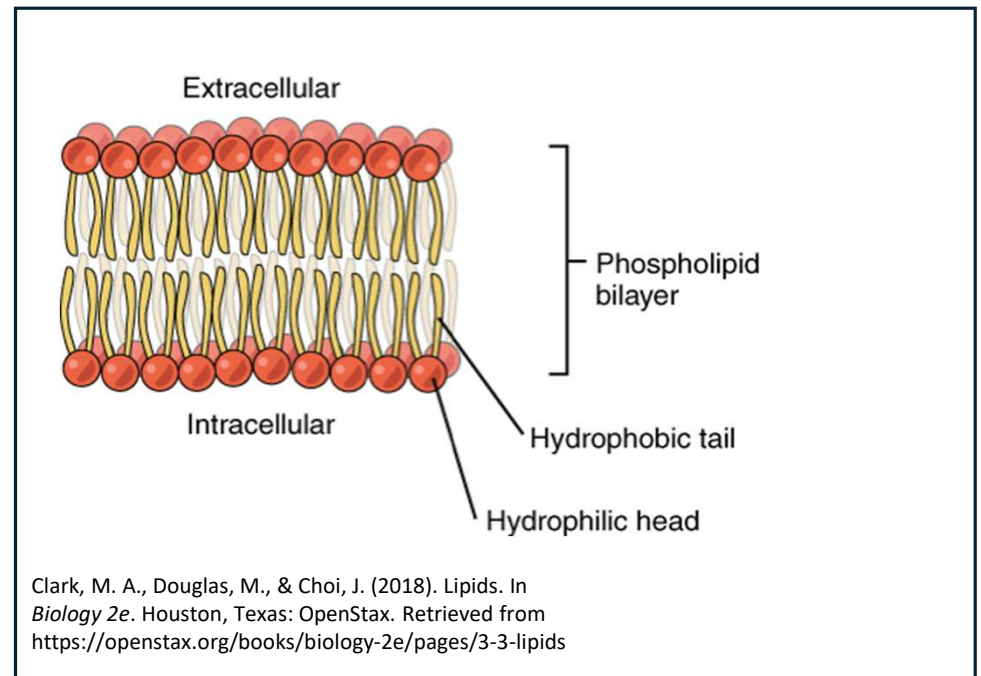
A: Lipids!



Cross Section of a Membrane

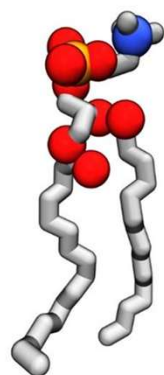


By SuperManu - Own work, CC BY-SA 3.0,
<https://commons.wikimedia.org/w/index.php?curid=2918850>



Biomembranes adjust their mechanical properties by changing their lipid composition

Neutral



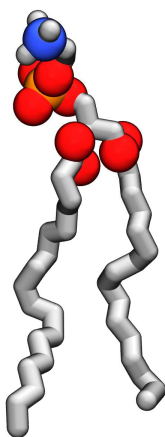
DPPC



Tails

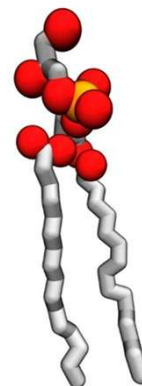


Headgroup

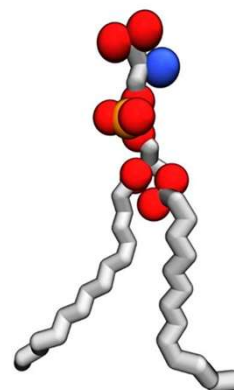


POPC

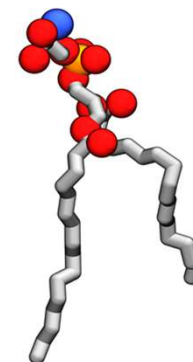
Charged



DPPG



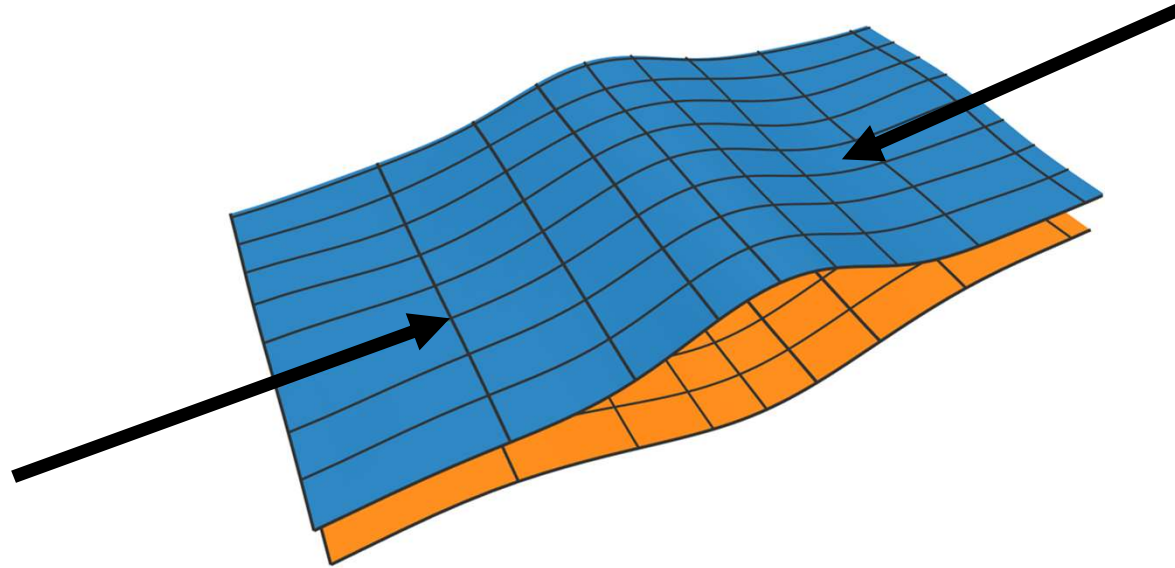
DPPS



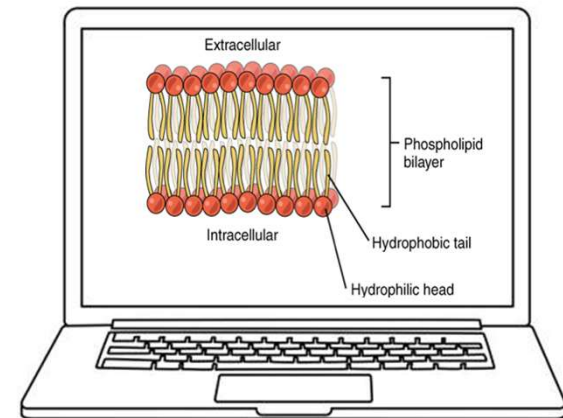
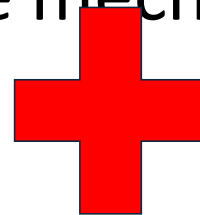
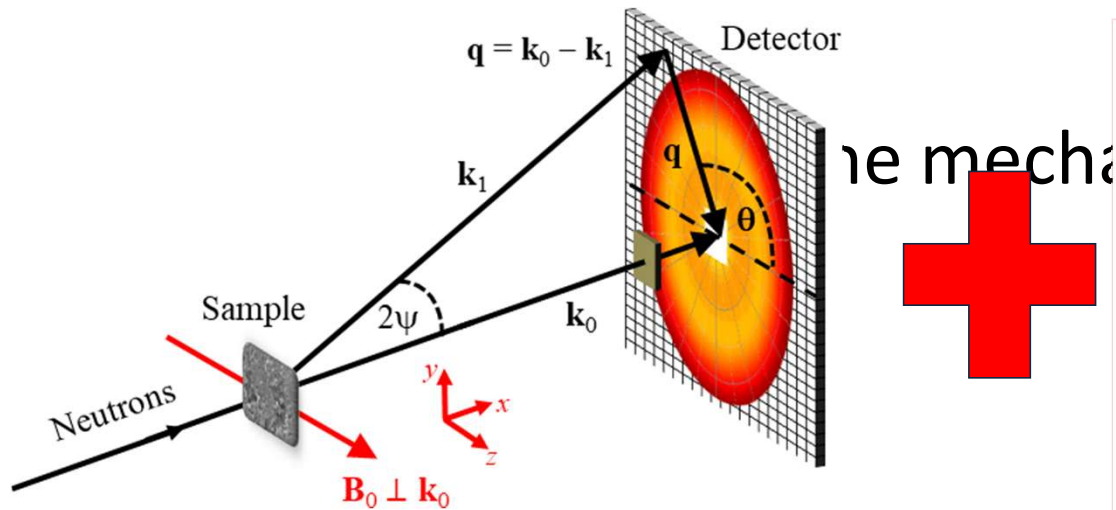
POPS

Area Compressibility (K_A)

The bilayer's resistance to
mechanical compression



Combining Scattering and Simulation



Magnetic neutron scattering from spherical nanoparticles with Neel surface anisotropy: Atomistic simulations - Scientific Figure on ResearchGate. Available from: https://www.researchgate.net/figure/Sketch-of-the-neutron-scattering-geometry-The-applied-magnetic-field-B-0-e-z-is_fig1_360640775

Neutron Scattering Analysis Is Hard!

$$S(q, t) \sim \exp \left[-\frac{k_B T q^2 R^2}{4\pi} \sum_{\ell=2}^{\lfloor \pi R/\delta \rfloor} (2\ell+1) \frac{(1-Q_{11})e^{-\gamma_1 t} + Q_{11}e^{-\gamma_2 t}}{(\ell(\ell+1)-2)(\ell(\ell+1)\kappa)} \right]$$

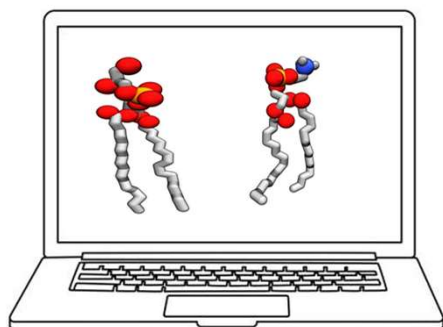
Vlahovska, Petia M., and Rony Granek. "Equilibrium Fluctuations of a Quasi-Spherical Vesicle: Role of the Membrane Dissipation." *Soft Matter*, 2026, 10.1039.D6SM00156D.
<https://doi.org/10.1039/D6SM00156D>.

$$Q_{11} = \frac{1}{2} + 2 \frac{\begin{aligned} &\ell^6(\lambda^2 - \alpha)\chi_s + \ell^5(\lambda^2 - \alpha)(3\chi_s + 2) \\ &+ \ell^4[(\lambda^2 - \alpha)(2\beta + 5) - 2\lambda^2\chi_s] \\ &+ \ell^3[\lambda^2(-9\chi_s + 4\beta - 4) + 4\alpha^2 + \alpha(-4\beta + 5\chi_s)] \\ &+ \ell^2[-\lambda^2(6\beta + 11) + 3\alpha\lambda + \alpha(5 + 6\alpha + 2\beta)] \\ &+ \ell[4\lambda^2(1 - 2\beta) + \alpha(2 + 4\beta + 3\lambda) + \chi_s(8\lambda + 4\alpha^2 - 2\alpha)] \\ &+ 4\lambda^2(2\beta + 1) - 6\lambda\alpha - \alpha^2 - 4\chi_s(2\alpha^2 + \lambda) \end{aligned}}{\begin{aligned} &2\alpha \sqrt{\begin{aligned} &[2\alpha(-4(\ell^2 + \ell - 2)\chi_s - 2(2\ell + 3)\ell^2 + 1) \\ &+ 2(\ell - 1)\ell(\ell + 1)(\ell + 2)(2\beta + (\ell^2 + \ell - 1)\chi_s + 2\ell + 1)]^2 \\ &- 4(1 - \ell)(\ell + 2)(-\lambda + 4\lambda(\ell^2 + \ell - 2)\chi_s + \ell(\ell(\lambda(4\ell + 6) + 3) + 3)) \\ &\cdot (6\alpha + 2\lambda(\ell - 1)(\ell + 2)(2\beta + (\ell^2 + \ell - 1)\chi_s + 2\ell + 1)) \end{aligned}} \end{aligned}}$$

and

$$\gamma_{1,2} = \ell(\ell + 1) \frac{\begin{pmatrix} -(\ell - 1)\ell(\ell + 1)(\ell + 2)(2\beta + (\ell^2 + \ell - 1)\chi_s + 2\ell + 1) + \alpha(-4(\ell^2 + \ell - 2)\chi_s - 4\ell^3 - 6\ell^2 + 1) - 3\lambda(\ell - 1)(\ell + 2) \\ \mp \frac{1}{2} \sqrt{\begin{aligned} &(2(\ell - 1)\ell(\ell + 1)(\ell + 2)(2\beta + (\ell^2 + \ell - 1)\chi_s + 2\ell + 1) + 2\alpha(-4(\ell^2 + \ell - 2)\chi_s - 4\ell^3 - 6\ell^2 + 1))^2 \\ &- 4(1 - \ell)(\ell + 2)(-\lambda + 4\lambda(\ell^2 + \ell - 2)\chi_s + 4\lambda\ell^3 + (6\lambda + 3)\ell^2 + 3\ell) \\ &\cdot 6\alpha + 2\lambda(\ell - 1)(\ell + 2)(2\beta + (\ell^2 + \ell - 1)\chi_s + 2\ell + 1) \end{aligned}} \end{pmatrix}}{9 + (1 - 6\ell^2 - 4\ell^3 - 4(-2 + \ell + \ell^2)\chi_s)(2 + 4\ell + 4\beta + 2(-1 + \ell + \ell^2)\chi_s)}$$

Getting K_A Through Simulation



Select lipid
composition

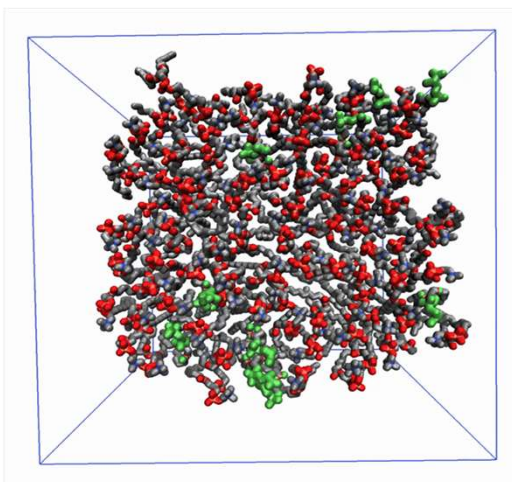


Select temperature &
pressure

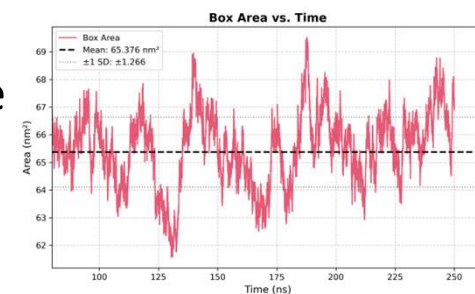


$$K_A = \frac{k_B T \langle A \rangle}{\langle \delta A^2 \rangle}$$

Venable, R. M., Brown, F. L. H., & Pastor, R. W. (2015).
Mechanical properties of lipid bilayers from molecular
dynamics simulation. *Chem. Phys. Lipids*, 192, 60–74.
<https://doi.org/10.1016/j.chemphyslip.2015.07.014>



Extract box size

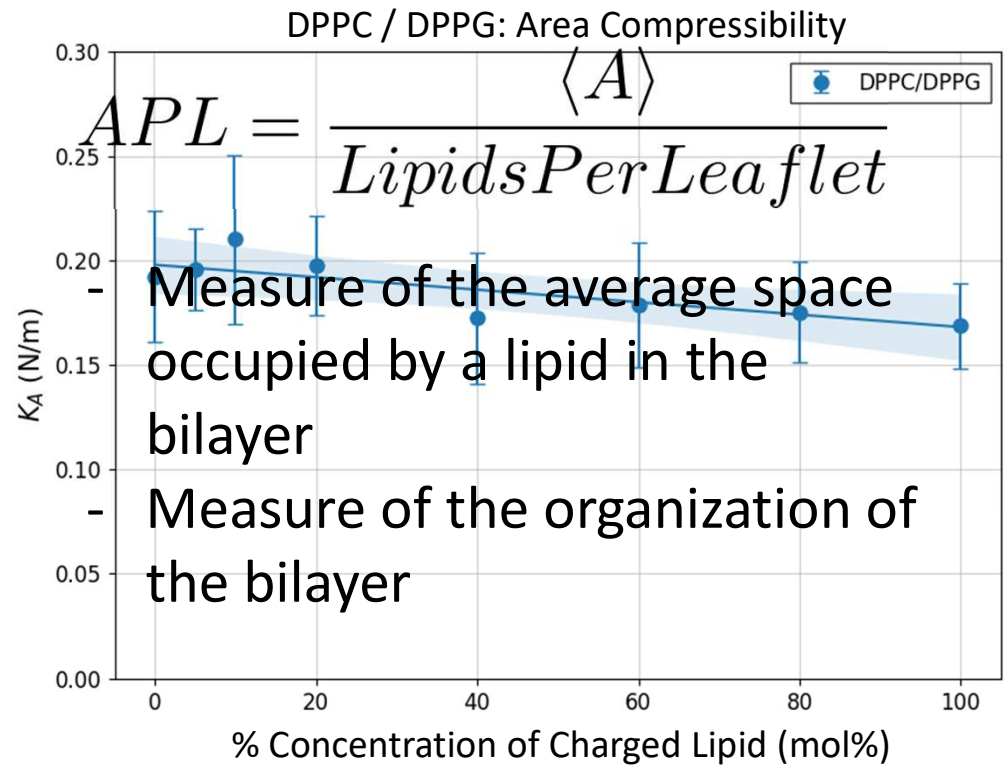
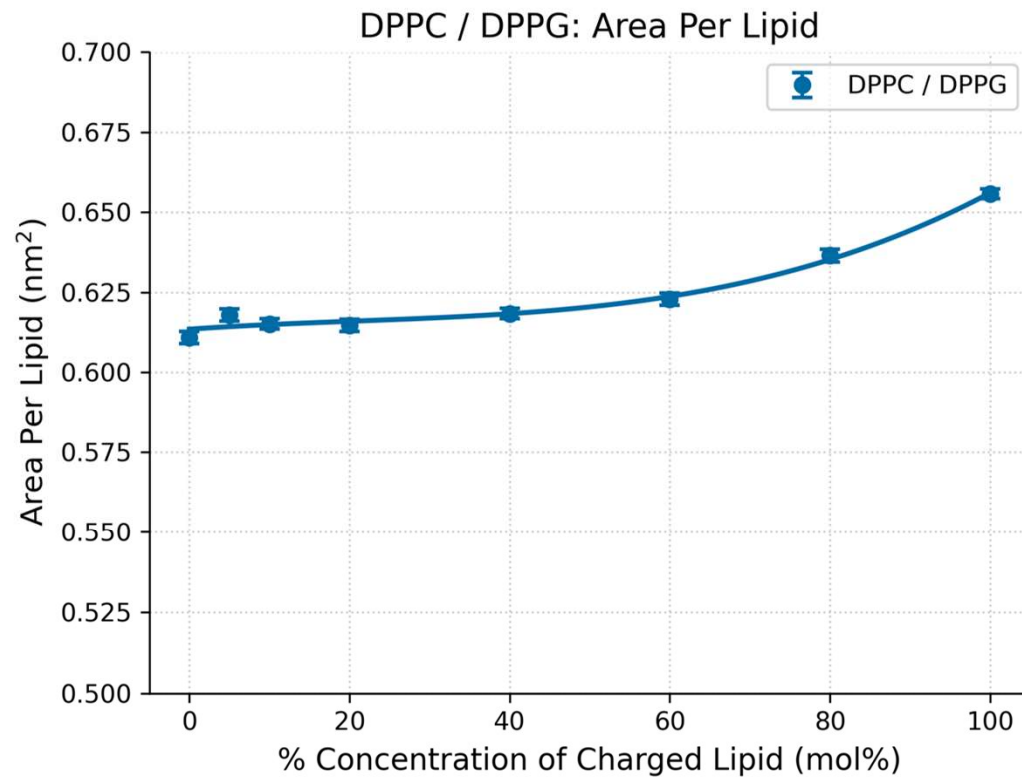


Analyze!

How do charged lipids affect
area compressibility?

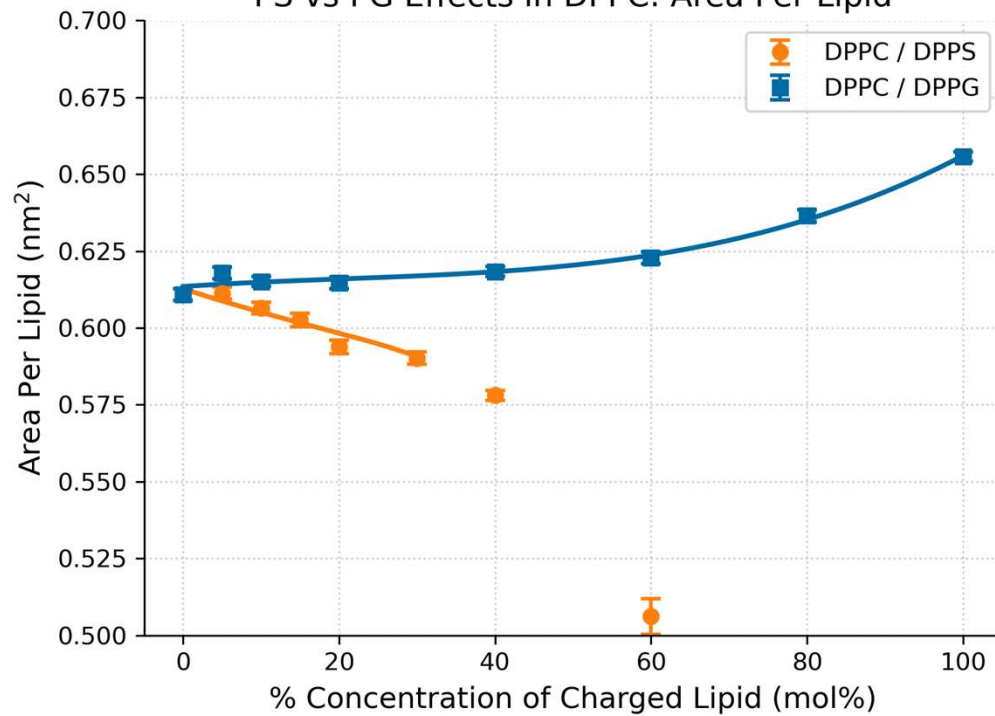


APL Increase, K_A (Nearly) Unchanged

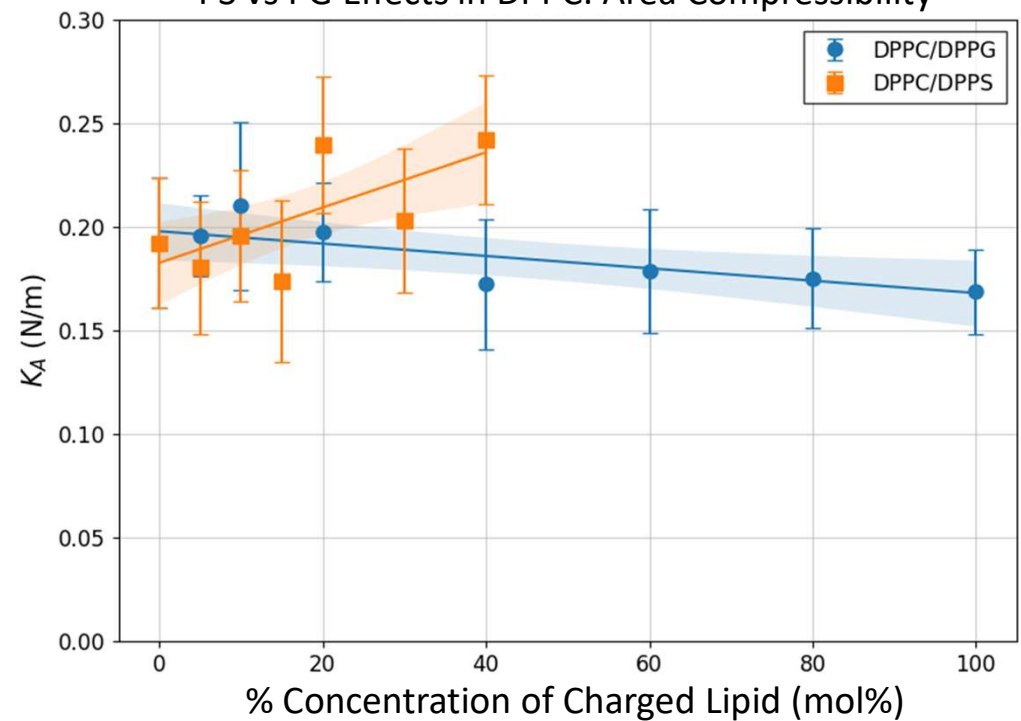


DPPC/DPPS: Very Different Behavior!

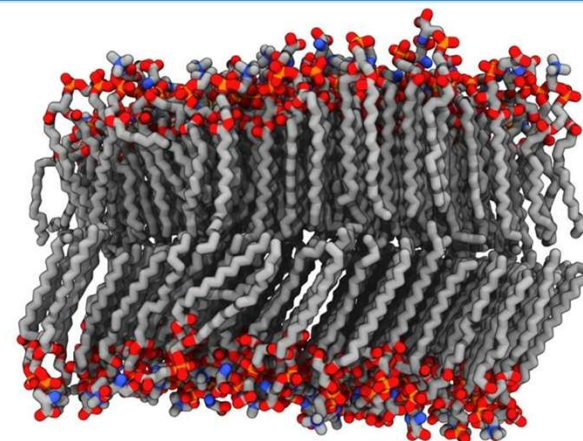
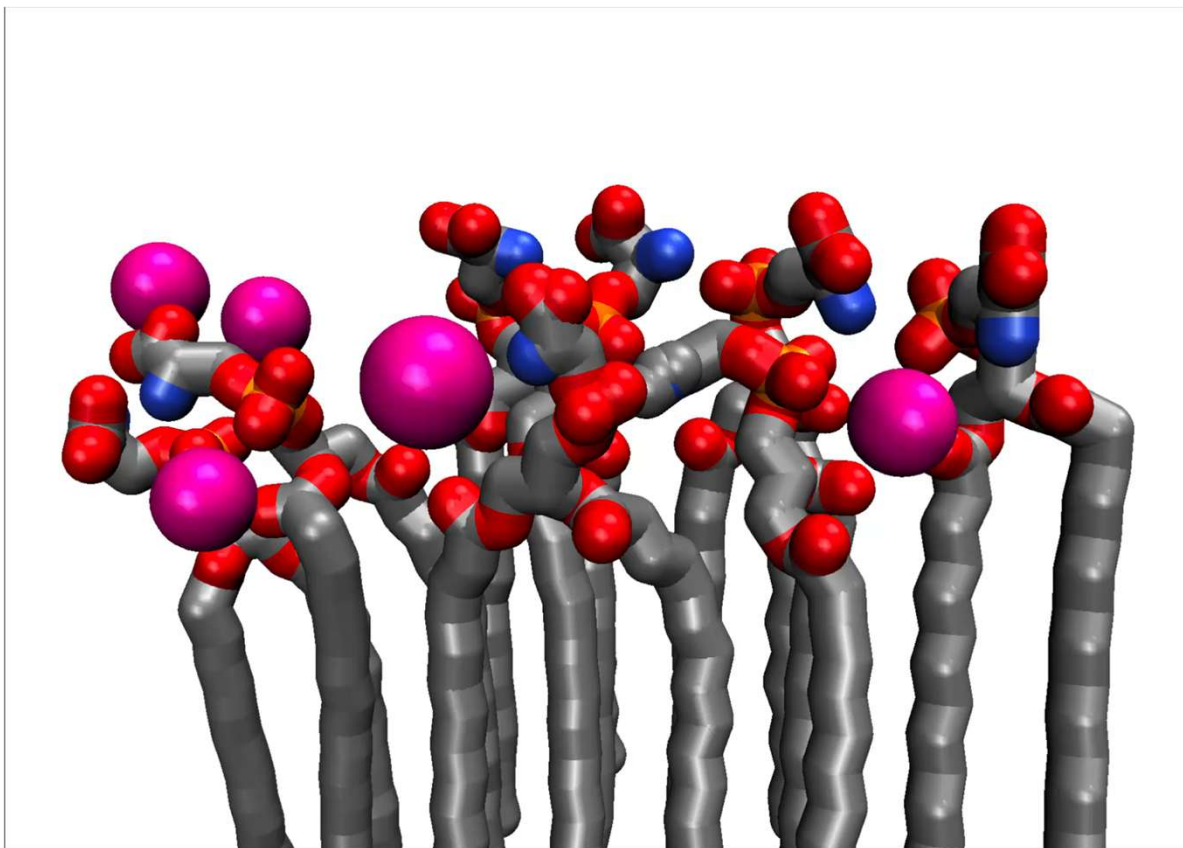
PS vs PG Effects in DPPC: Area Per Lipid



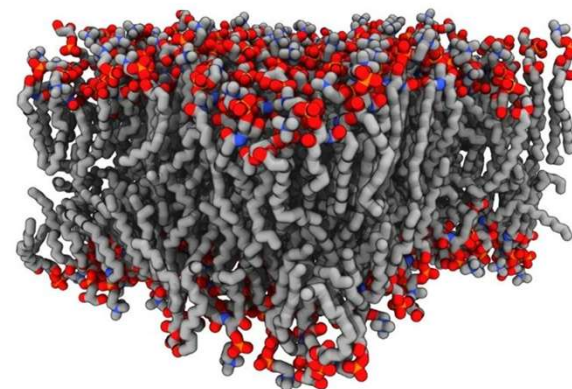
PS vs PG Effects in DPPC: Area Compressibility



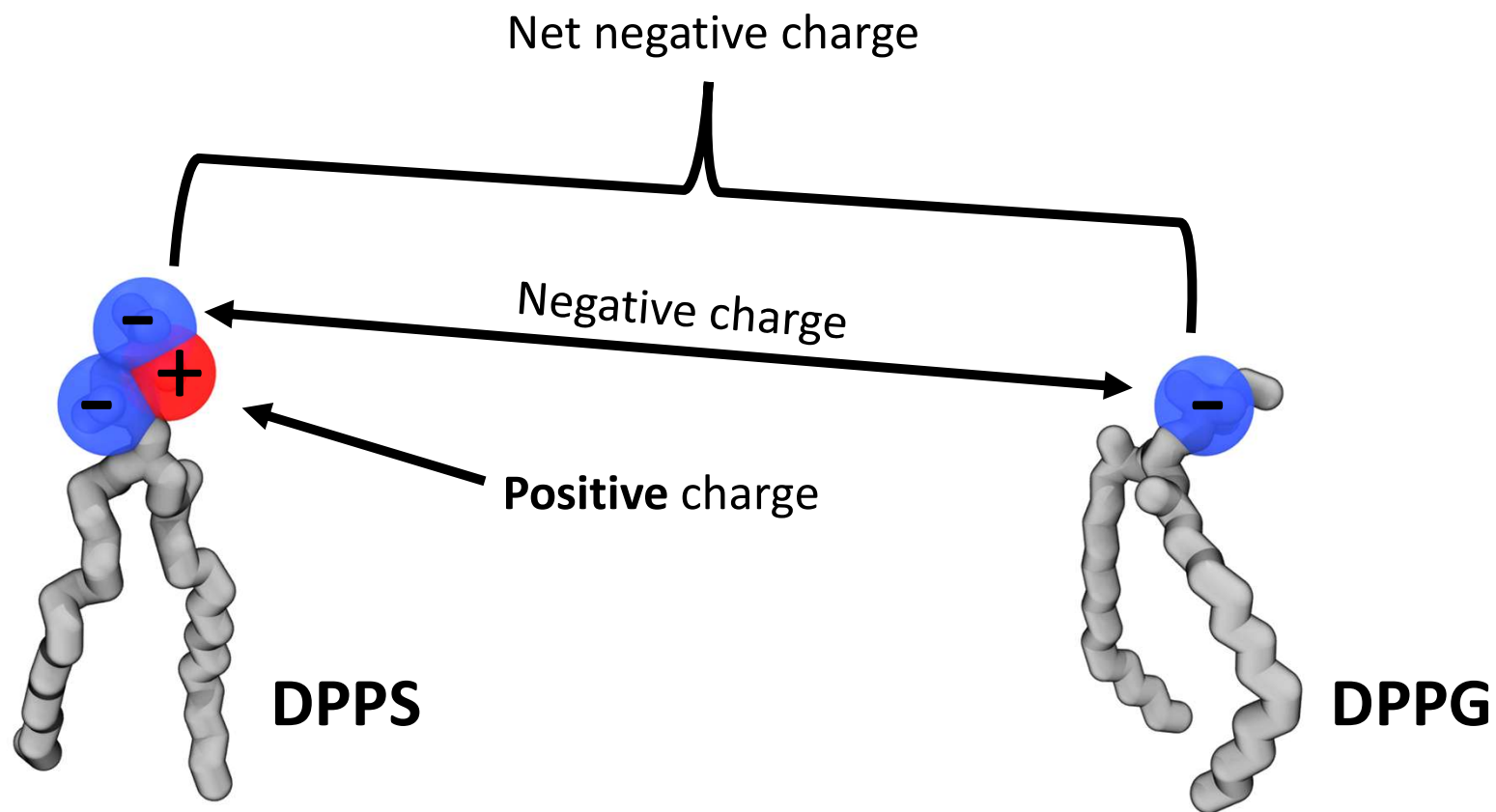
4:6 DPPC:DPPS Becoming Gel



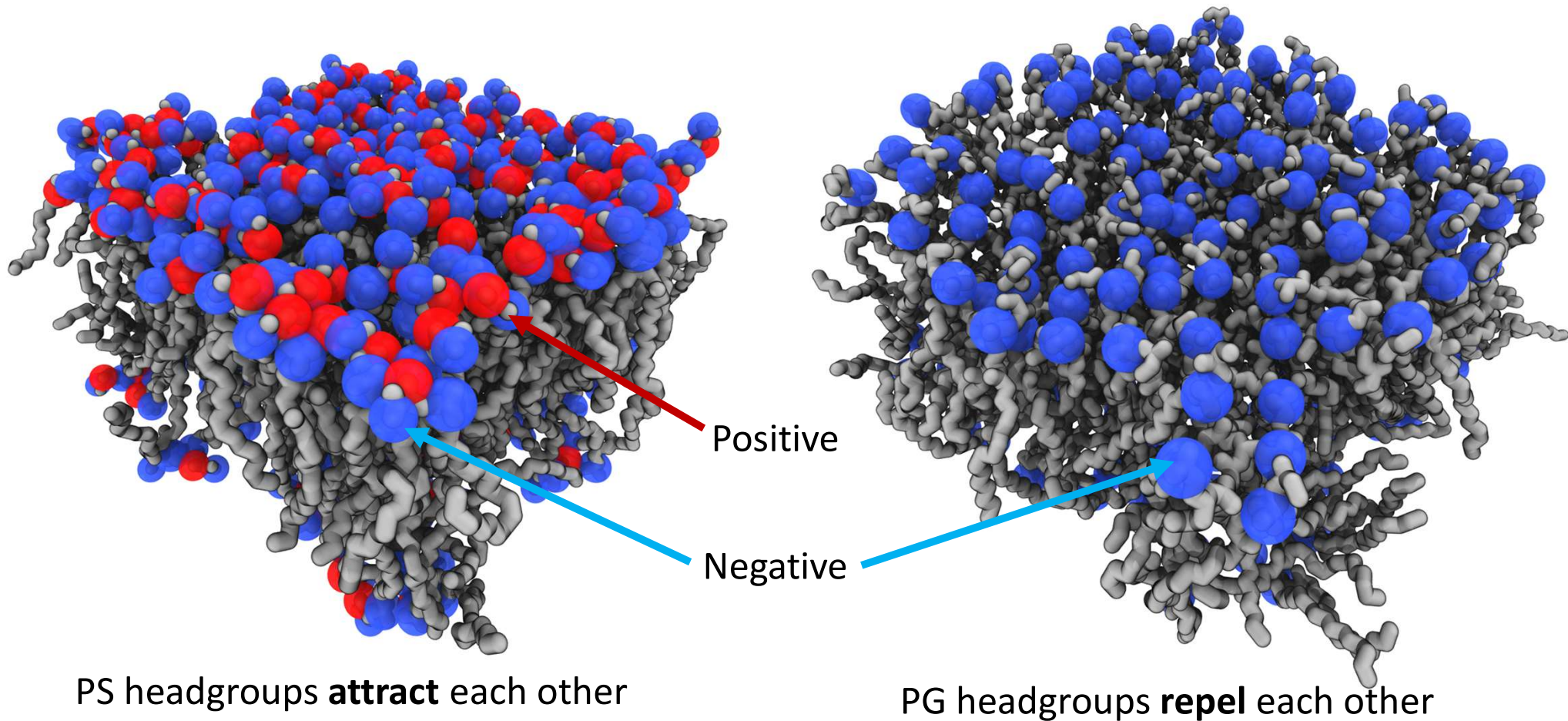
Gel 4:6 DPPC:DPPS



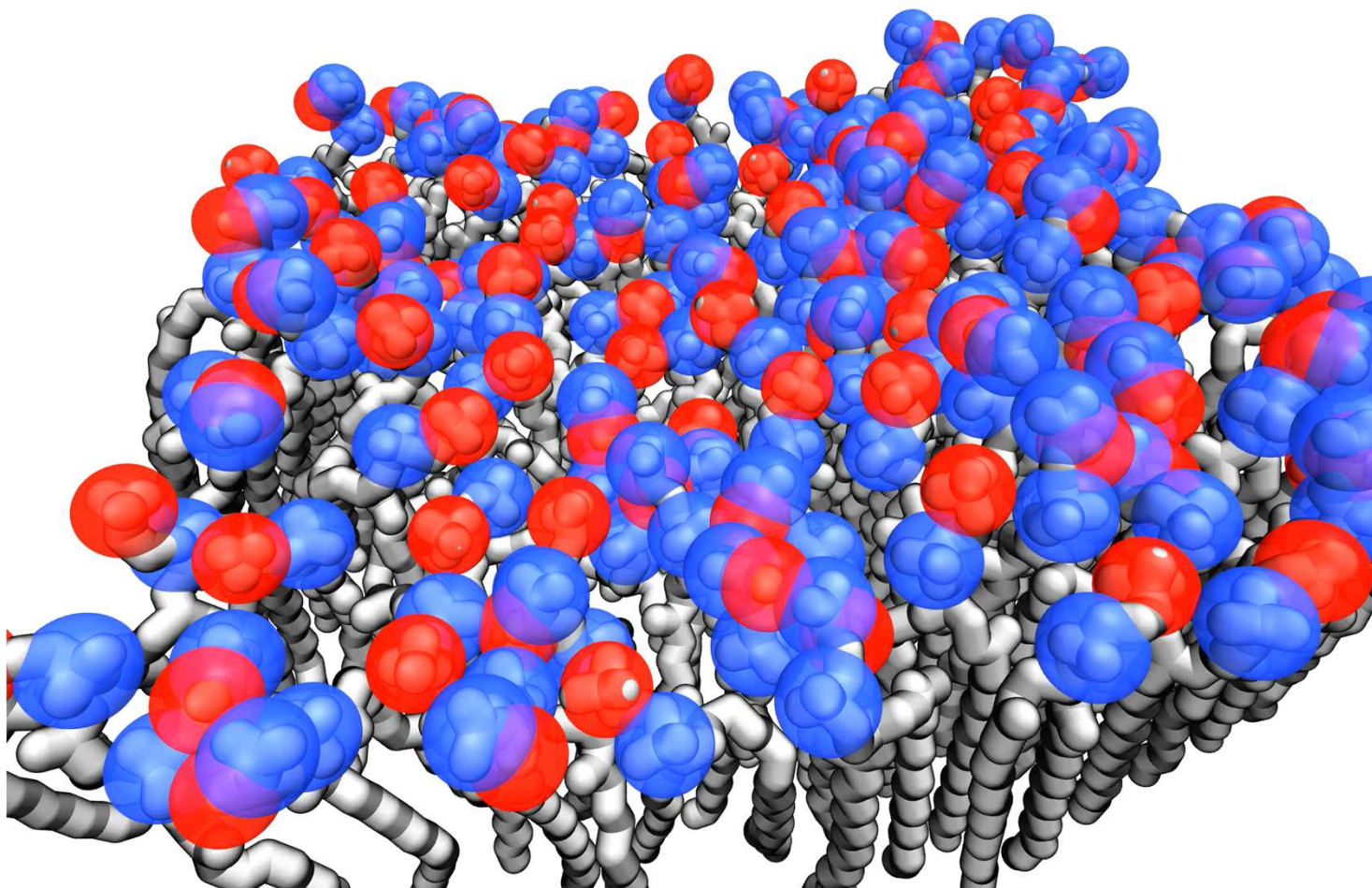
Liquid Bilayer



Charge Distribution of PS vs PG

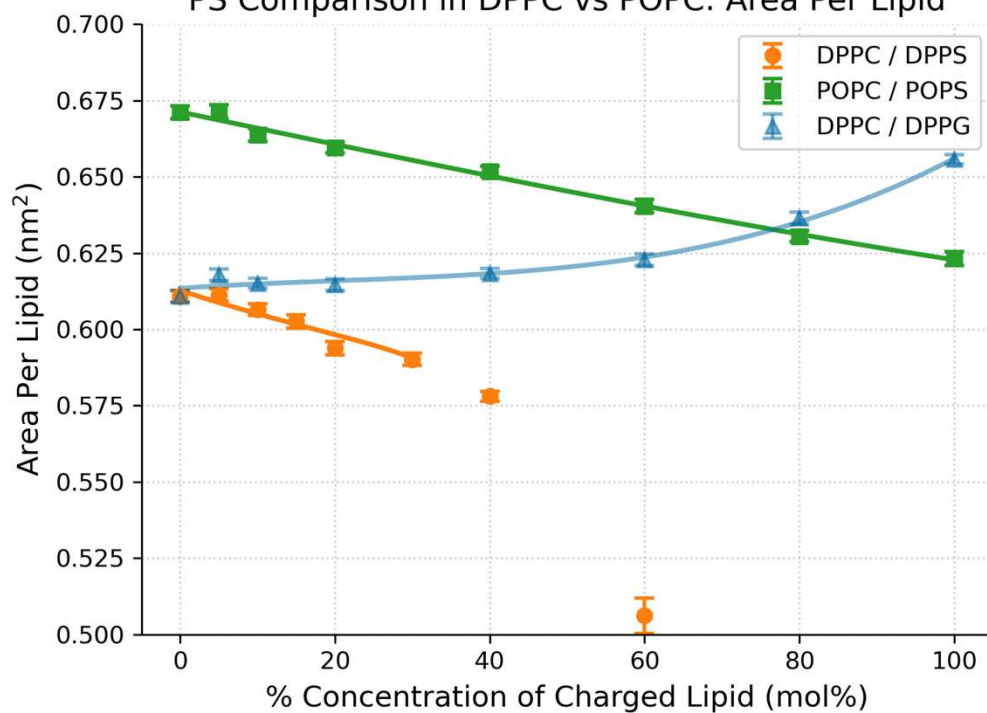


Charge Distribution of DPPG & DPPS

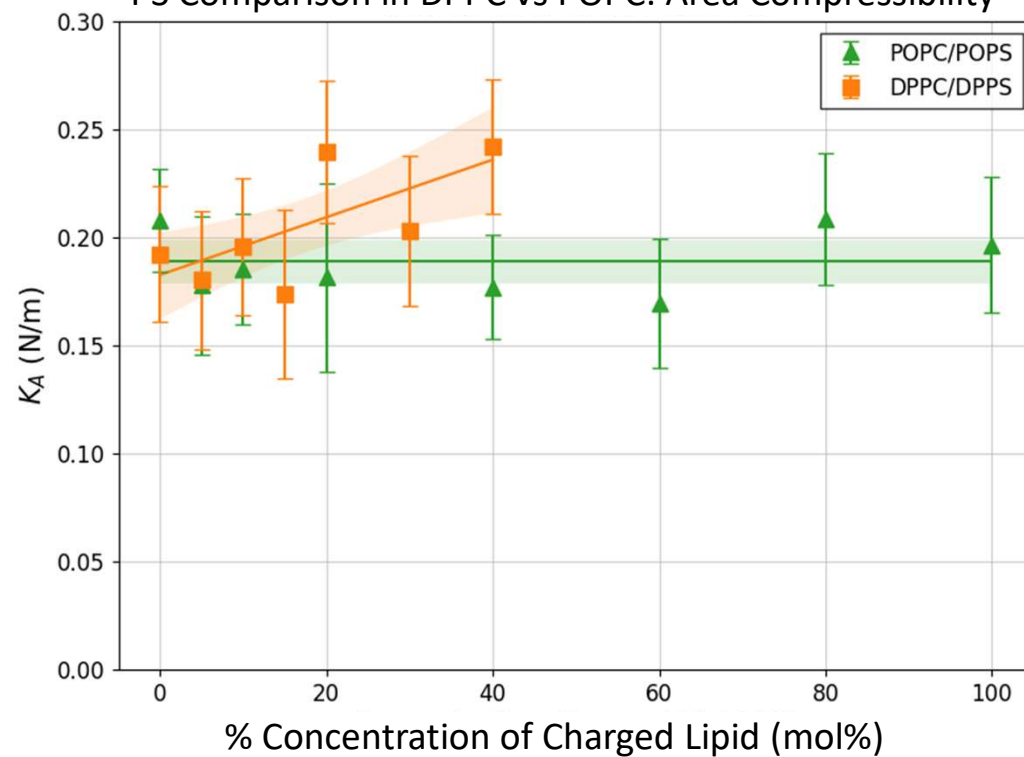


POPS: APL Still Decreases

PS Comparison in DPPC vs POPC: Area Per Lipid



PS Comparison in DPPC vs POPC: Area Compressibility





Summary

- PS and PG lipids have different effects on the membrane despite having the same charge
- Area per lipid is fairly impacted but not the area compressibility

Future Work

- Evaluating Polymer brush model (a well-known theory in bilayer studies)

$$K_A \propto A_L^2 \kappa$$

- Applications to experimental/material design
- Applications to analysis on NSE data of bilayers (recently collected at ILL, soon to be collected at NCNR!)

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I would like to thank my mentors,
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Also to the SURF organizers: Cara
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Rehmann, and Susana Teixeira

RCHPC (Research Computing and
High Performance Computing at
NIST)

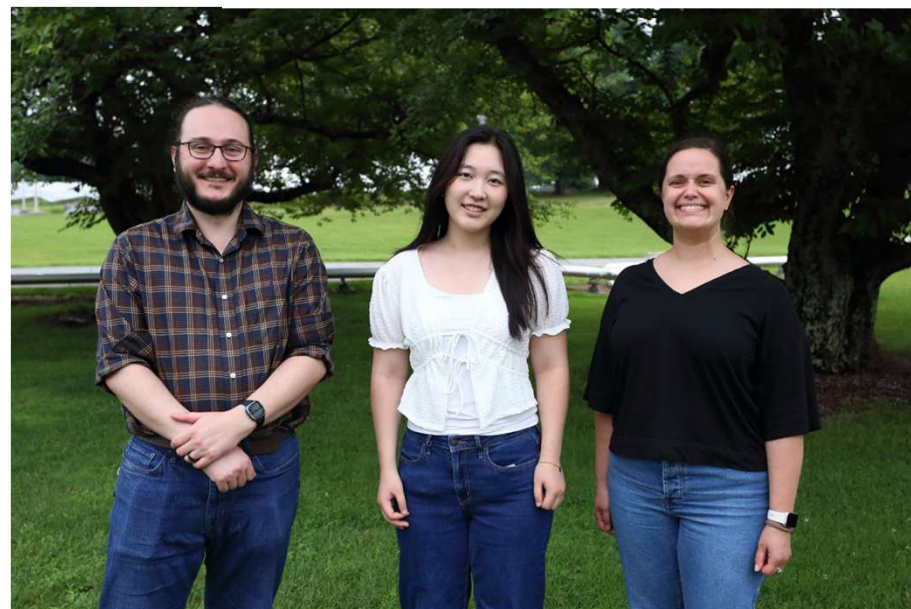


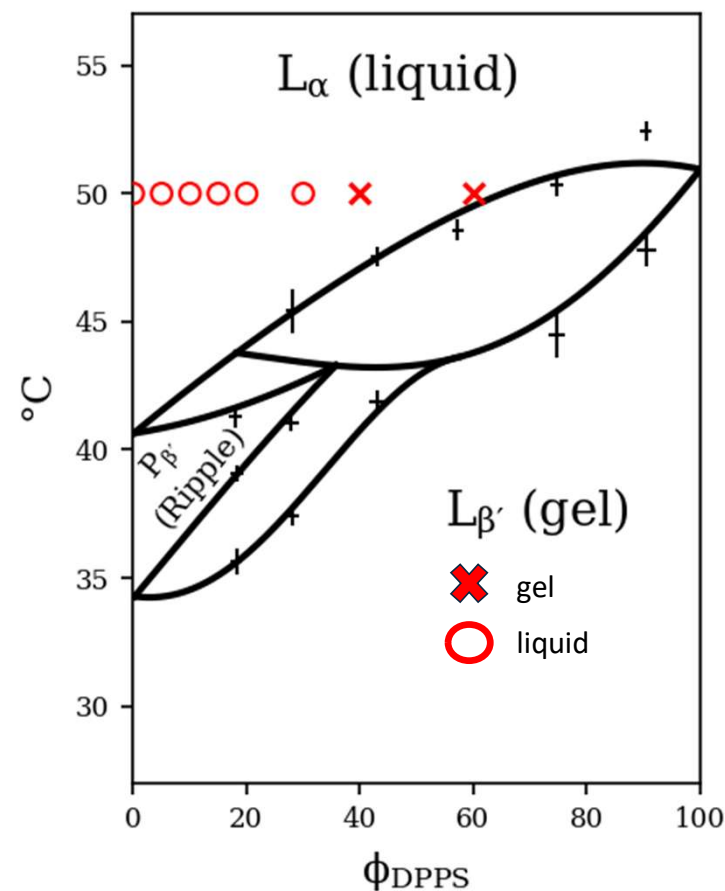
Image by Yiming Qiu



Supplementary: Lipid Phase Transitions

lipid	Tails	T_m (°C)	T_{sim} (°C)
EggSM	16:0	38.3	50
DPPC	16:0	41	50
DPPG (-)	16:0	41	50
DPPS (-)	16:0	54	50
POPC	16:0-18:1	-2	25
POPS (-)	16:0-18:1	14	25

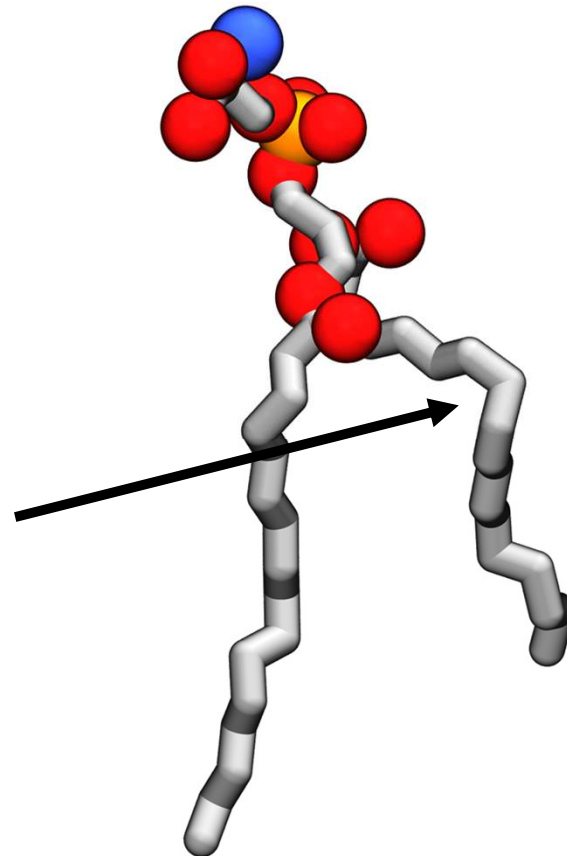
Z., González-Ramírez, E.J., Goñi, F.M., Tristram-Nagle, S., & Nagle, J.F. (2018). Phase behavior of palmitoyl and egg sphingomyelin. *Chemistry and Physics of Lipids*, 213, 102-110. <https://doi.org/10.1016/j.chemphyslip.2018.03>.

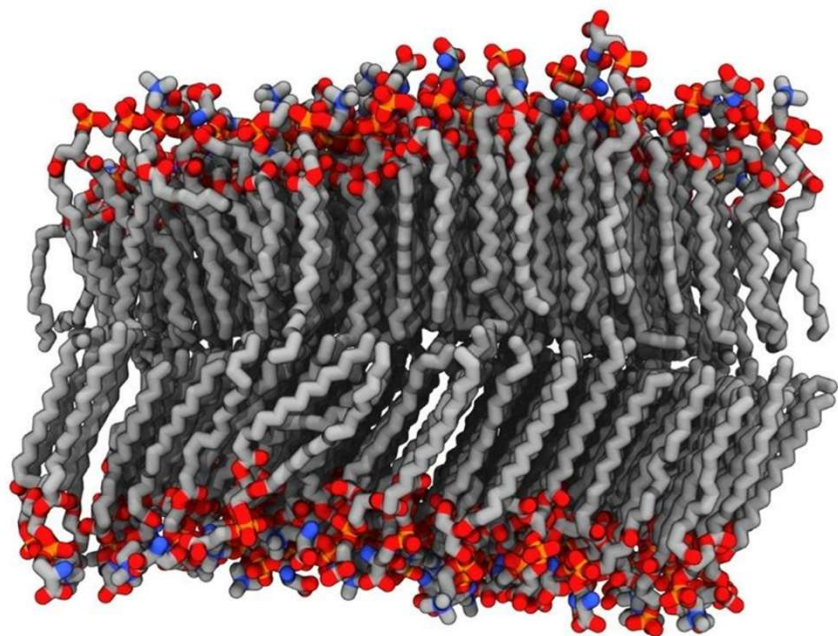


Luna, Elizabeth J., and Harden M. McConnell. "Lateral Phase Separations in Binary Mixtures of Phospholipids Having Different Charges and Different Crystalline Structures." *Biochimica et Biophysica Acta (BBA) - Biomembranes* 470, no. 2 (1977): 303-16. [https://doi.org/10.1016/0005-2736\(77\)90108-0](https://doi.org/10.1016/0005-2736(77)90108-0).

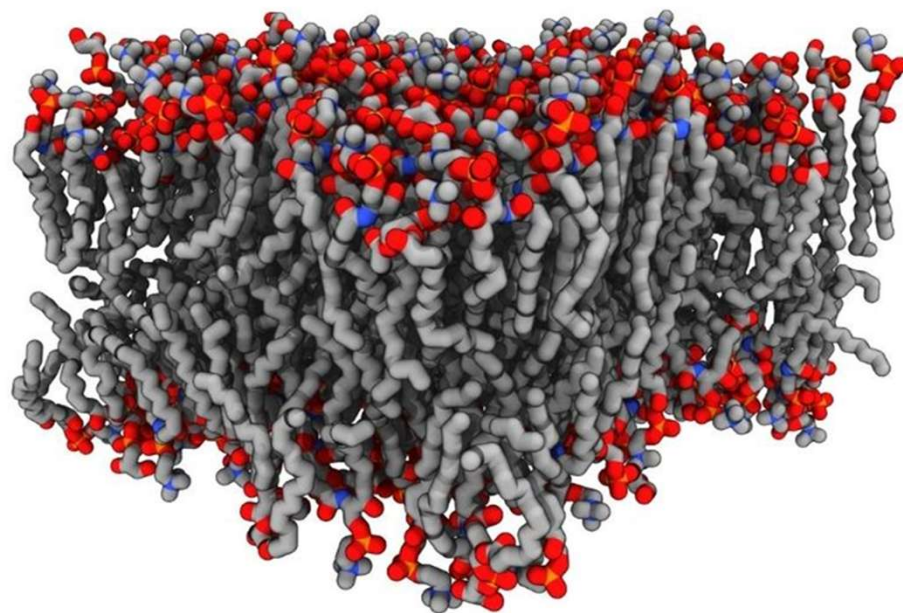
Q: Why does POPC/POPS start at a higher APL than DPPC/DPPS?

A: Due to having an extra bend in the tail, the POPS takes up more space than the DPPS, resulting in more APL.





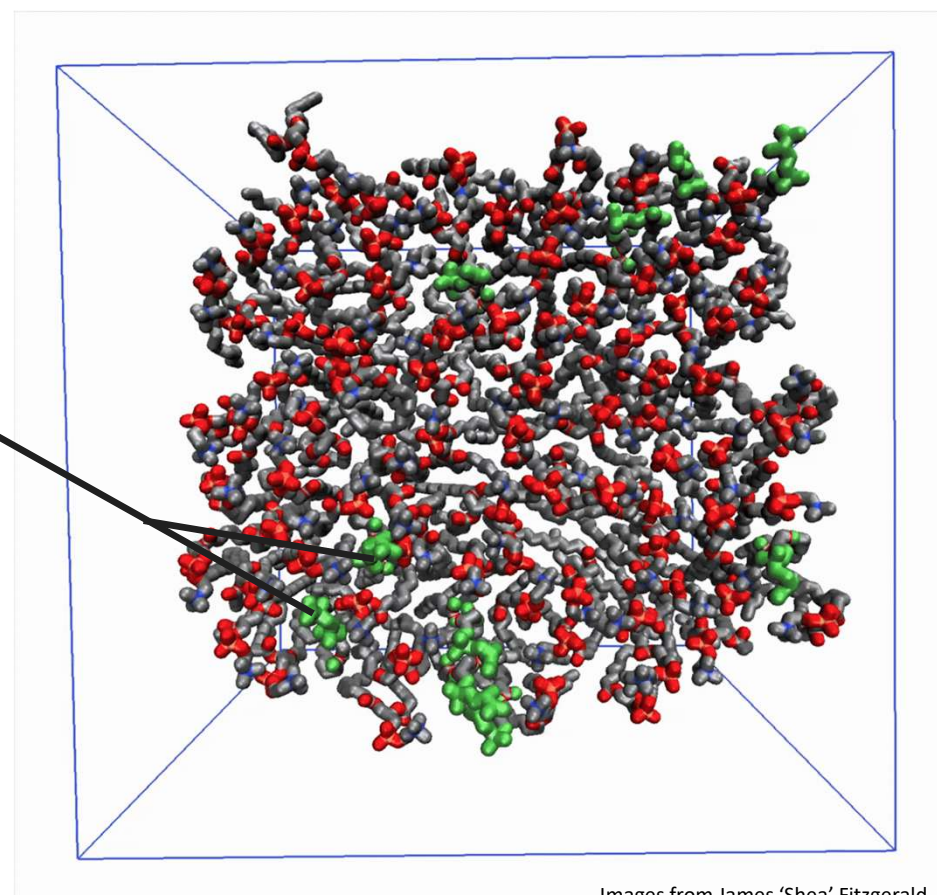
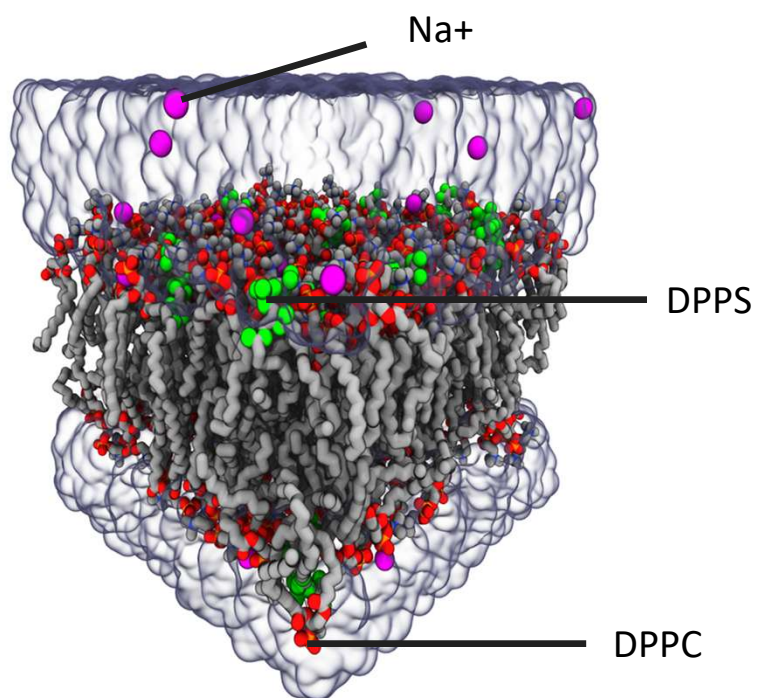
Gel 4:6
DPPC:DPPS



Liquid ESM

1:9 DPPS:DPPC

All-atom MD, CHARMM36 FF



Images from James 'Shea' Fitzgerald

