Capillary µRheoSANS for High Shear Rate, Low Volume Studies

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Applications in industry







~1,000,000 s⁻¹



Shear rate and traditional RheoSANS

$$h \int v = v/h$$
Shear Rate: $\dot{\gamma} = v/h$
Shear Thickening
Newtonian
Shear Thinning





~5000 s⁻¹ 7-20 mL Sample

Applications in industry

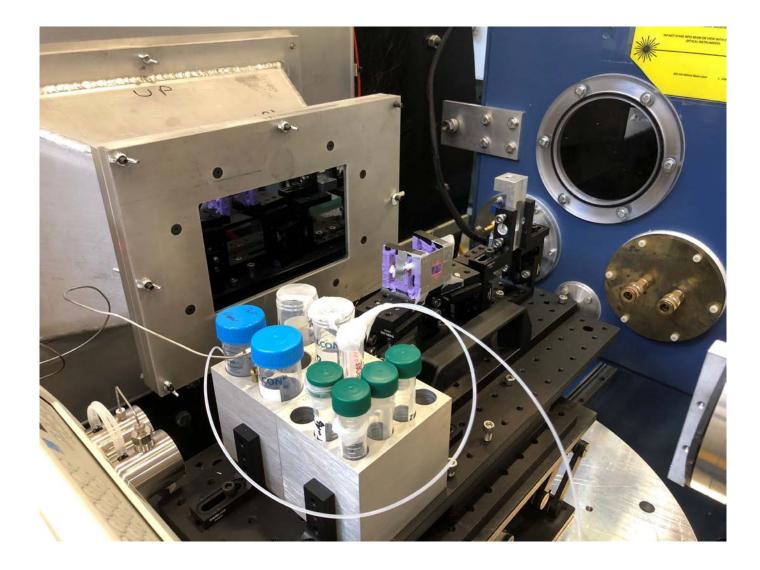




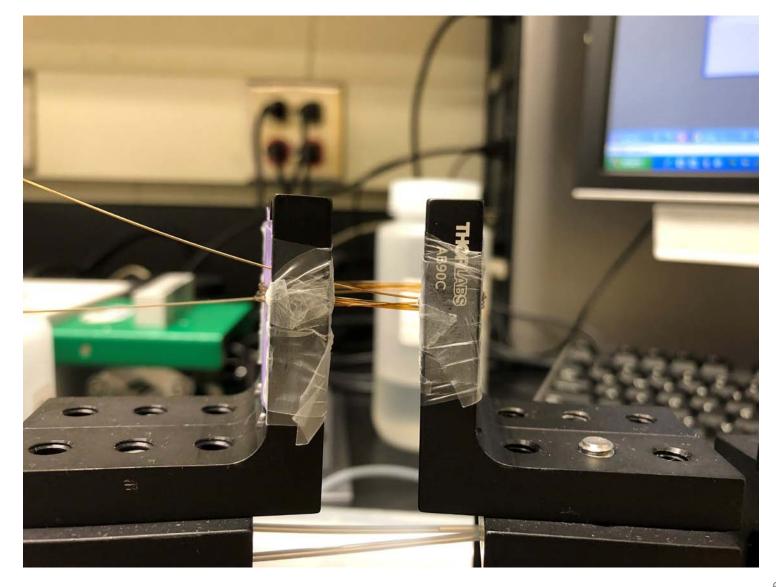


~1,000,000 s⁻¹

Capillary µRheoSANS

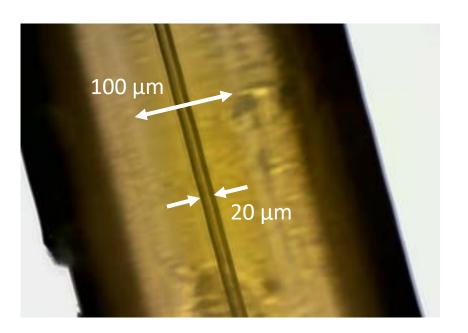


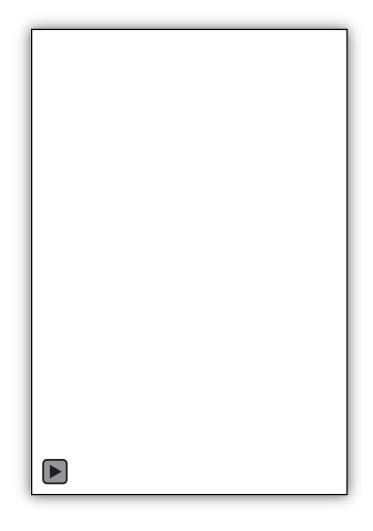
Capillary µRheoSANS





Capillary size and velocity



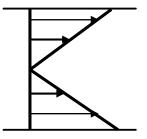


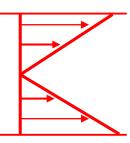


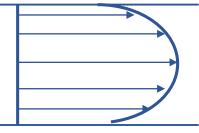
Capillary fluid flow

Laminar Poiseuille Flow (Newtonian)

 $\tau = \mu \dot{\gamma}$







Shear Stress (τ)

Shear Rate ($\dot{\gamma}$)

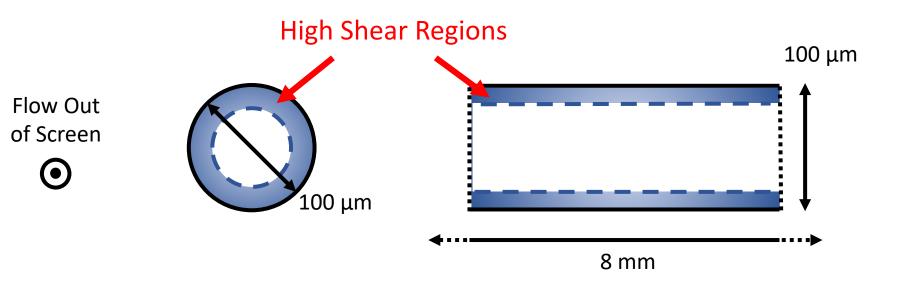
Velocity

Non-Newtonian

$$\tau = \mu(\dot{\gamma}) \cdot \dot{\gamma}$$

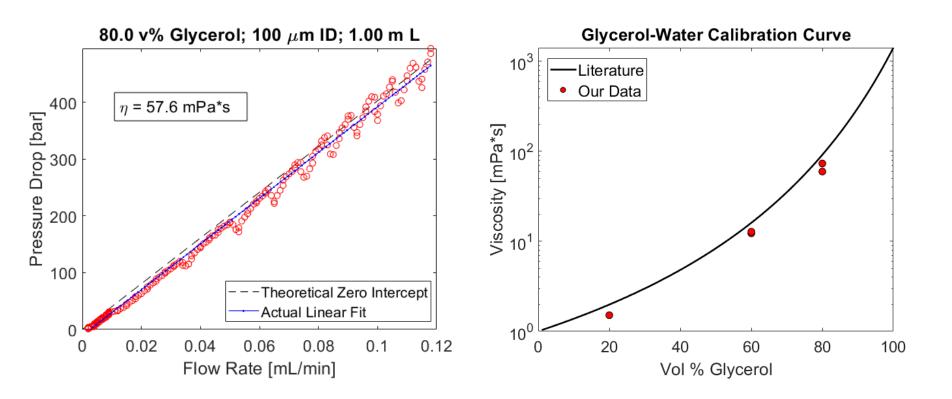
Shear Stress

Comparison to Slit µRheoSANS



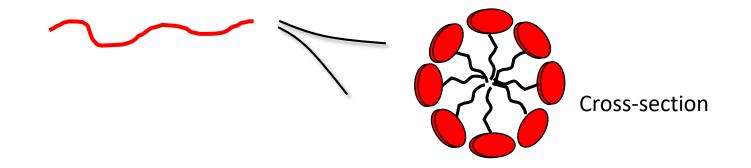
Approximate Scattering Volume [μL]	
SANS	100
Slit Cell	10
Capillary	1

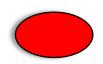
Determining physical limits





Wormlike micelles

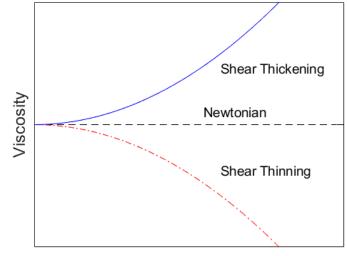




Hydrophilic head

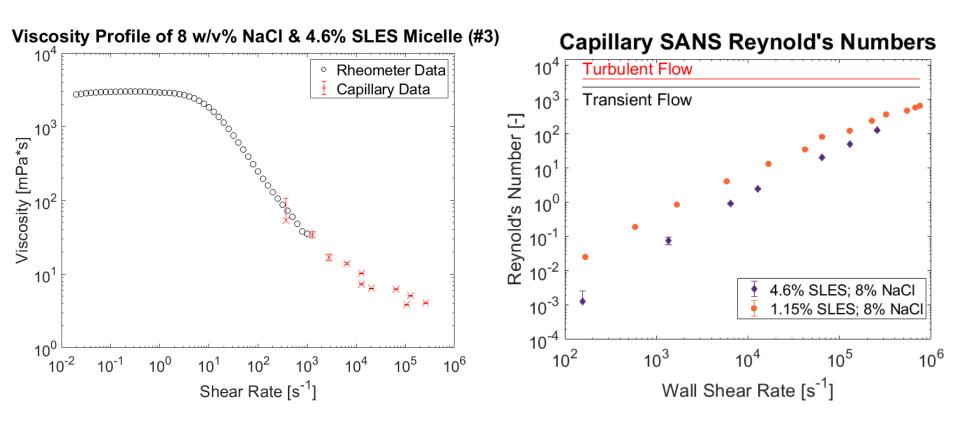


Hydrophobic tail



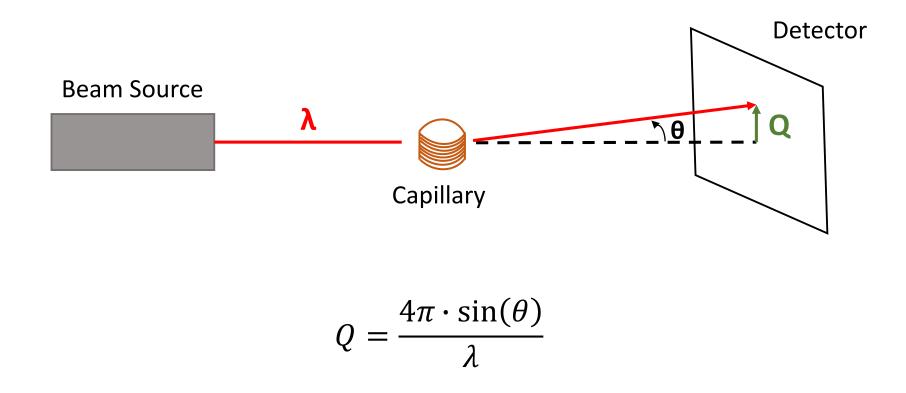
Shear Rate

Micelles under high shear

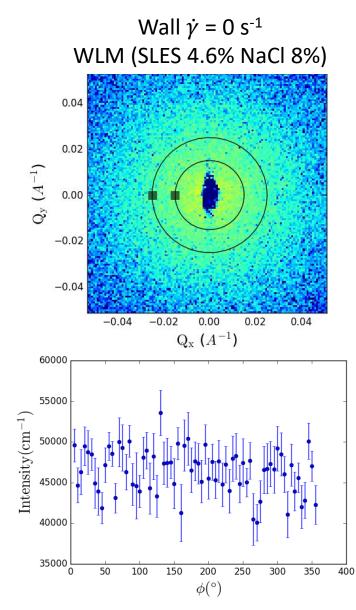




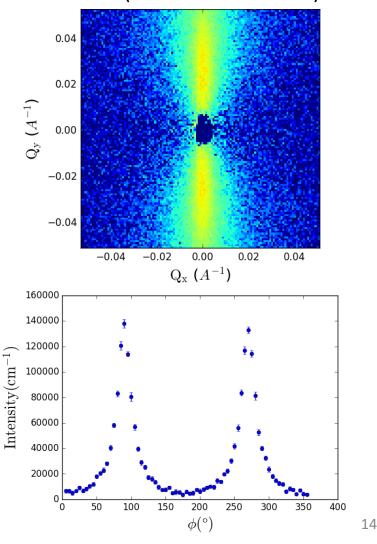
Small Angle Neutron Scattering (SANS)



2D SANS profiles



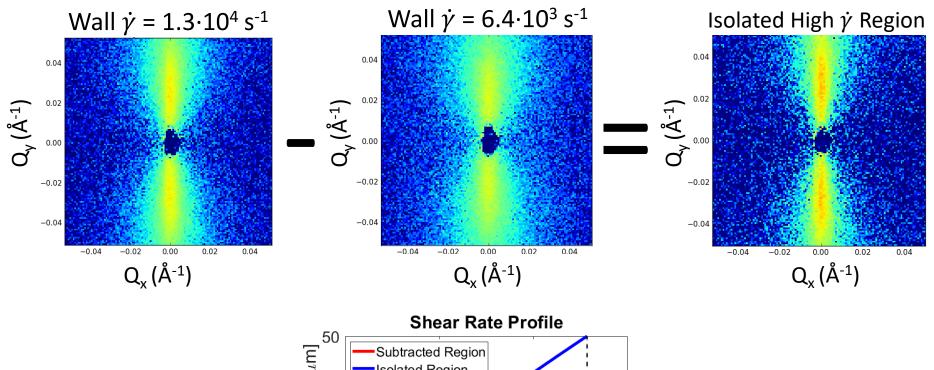
Wall $\dot{\gamma} = 1.3 \cdot 10^4 \, \text{s}^{-1}$ WLM (SLES 4.6% NaCl 8%)

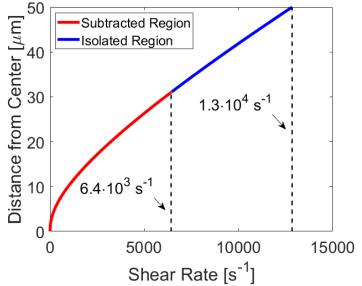


Micelle alignment factors

Capillary SANS Alignment 0.8 0.7 Alignment Factor [-] 9.0 0.2 4.6% SLES; 8% NaCl 0.1 1.15% SLES; 8% NaCl 0 10² 10³ 10⁴ 10⁵ 10⁶ 10¹ Wall Shear Rate [s⁻¹]

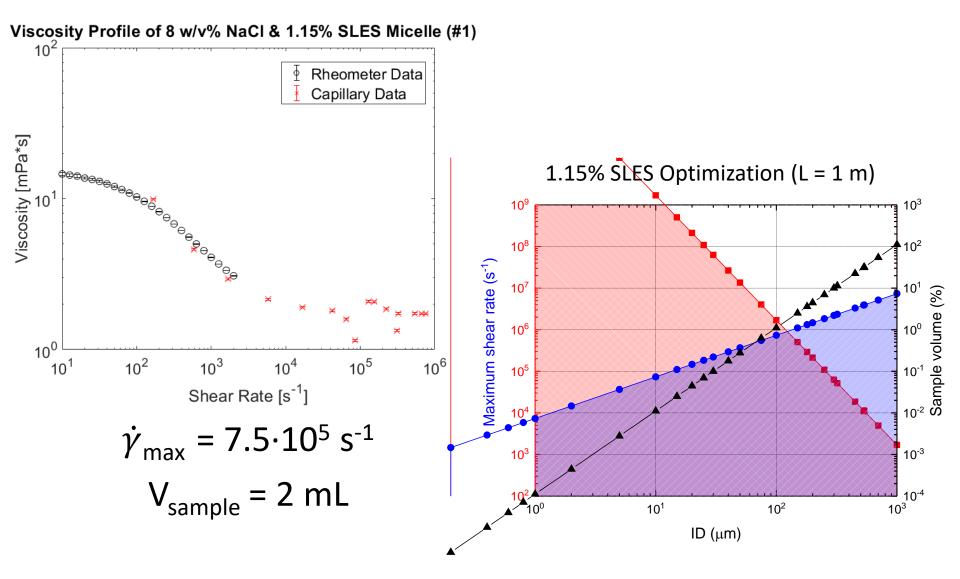
Wall shear rate scattering isolation







Validating results



Acknowledgements

- Katie Weigandt
- Ryan Murphy
- Javen Weston



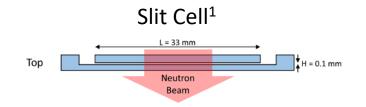


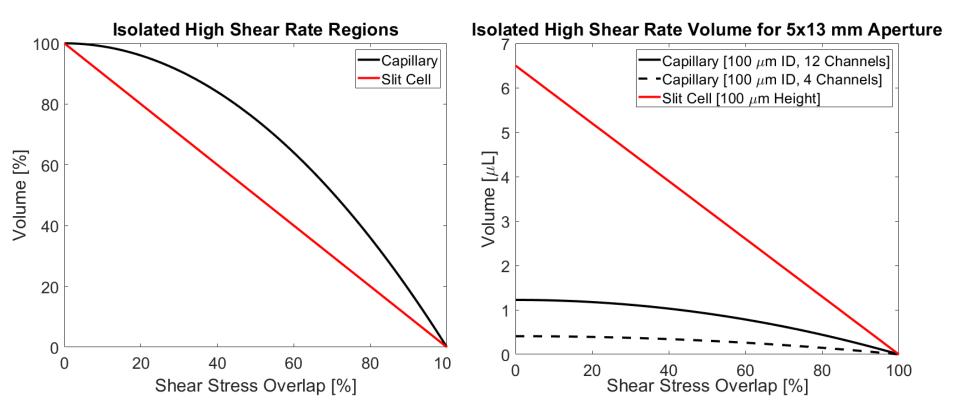
SURF Award Number: 70NANB18H141

Questions

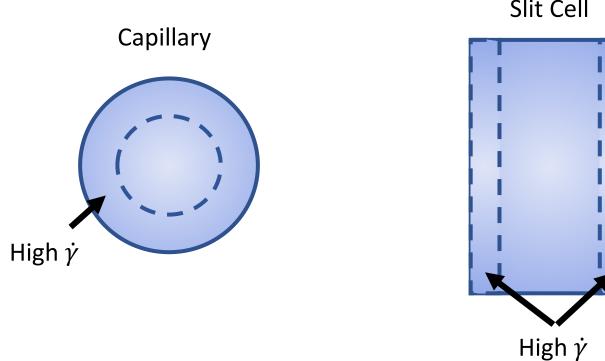
Extra Slides

Comparison to Slit µRheoSANS





Comparison to Slit µRheoSANS



Slit Cell

Important equations

 $au = \mu \dot{\gamma}$

$$\tau = \frac{\Delta PR}{2L}$$

$$v = \frac{\Delta P R^2}{4\mu L} \left[1 - (r/R)^2\right]$$

Shear Stress

Capillary Shear Stress

$$\mu = \frac{\Delta P \pi R^4}{8LQ}$$

Capillary Viscosity (Hagen-Poiseuille)

$$\dot{\gamma} = \frac{4Q}{\pi R^3}$$

Apparent Wall Shear Rate

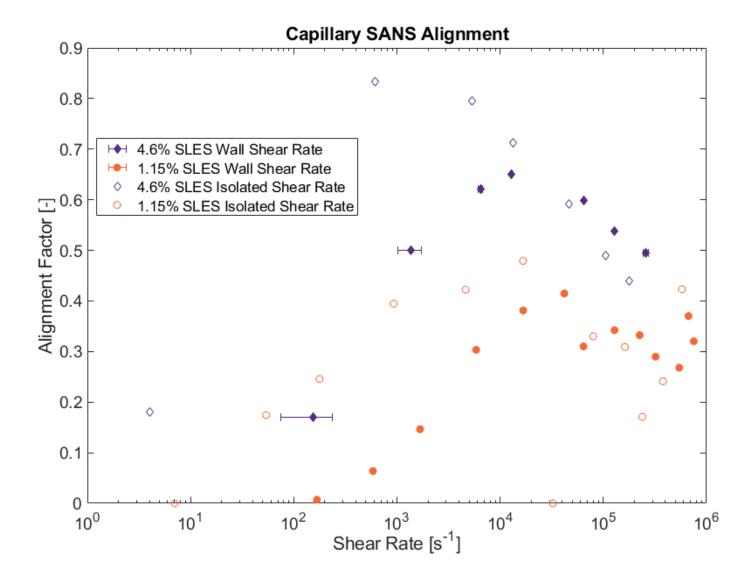
$$\dot{\gamma}_{WR} = \dot{\gamma}_a \left[\frac{1}{4} \left(3 + \frac{d \ln \dot{\gamma}_a}{d \ln \tau} \right) \right]$$

Corrected Wall Shear Rate (Weissenberg-Rabinowitsch)

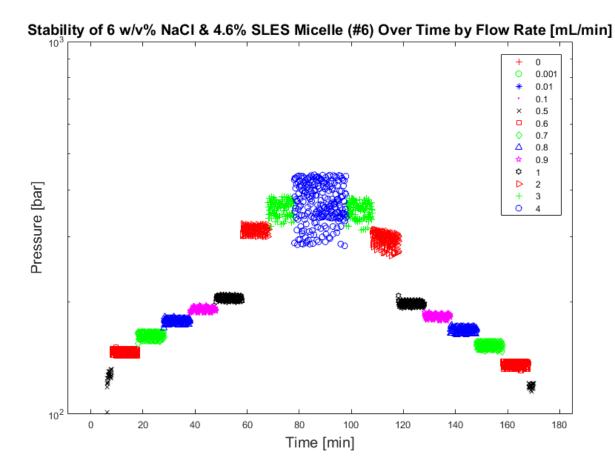
$$Re = \frac{\rho DQ}{A\mu}$$

Reynold's Number

Micelle alignment factors



Stability of micelle pressure drops



Other capillary jet video

