

# Sample Development for Small Angle Scattering and Neutron Interferometry

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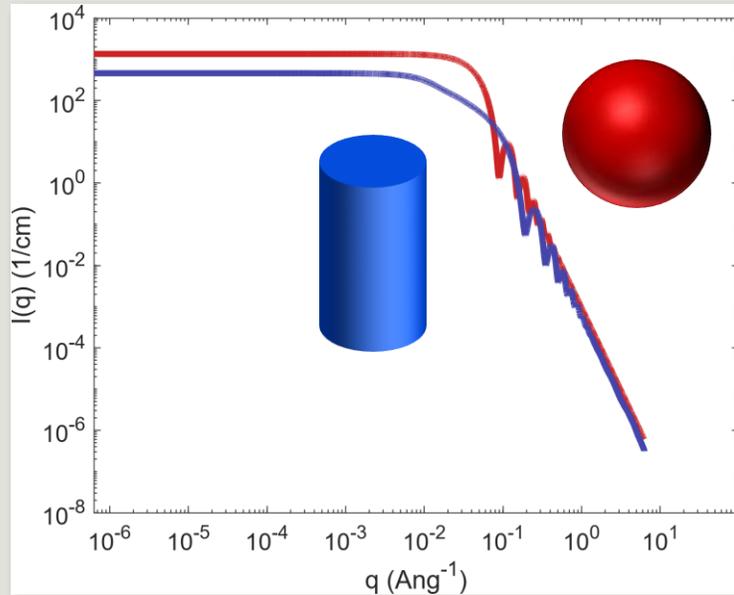
NIST SURF PROGRAM 2023



RICE UNIVERSITY

# Small Angle Scattering (SAS)

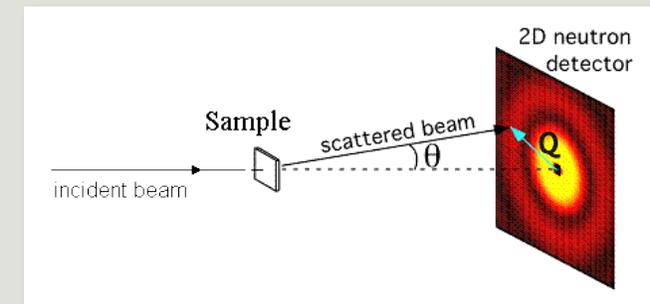
- Statistical **characterization** of materials
  - Reveals interatomic detail smaller than wavelength of visible light
  - Works at length scales of **1nm – 10μm**



$$I(Q) = \phi \Delta\rho^2 P(Q) S(Q)$$

- Small Angle X-Ray Scattering (SAXS)
  - Scattered by **electrons** in material
  - Good for heavy elements with many electrons
- Small Angle Neutron Scattering (SANS)
  - Scattered by **nuclei** in material
  - Much better penetration, but weaker scattering effect

$$Q = \frac{4\pi}{\lambda} \sin\left(\frac{\theta}{2}\right)$$

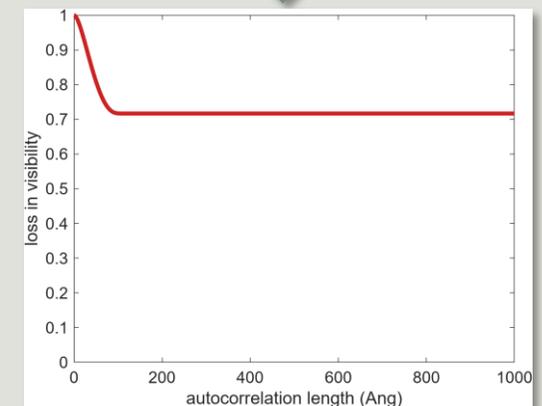
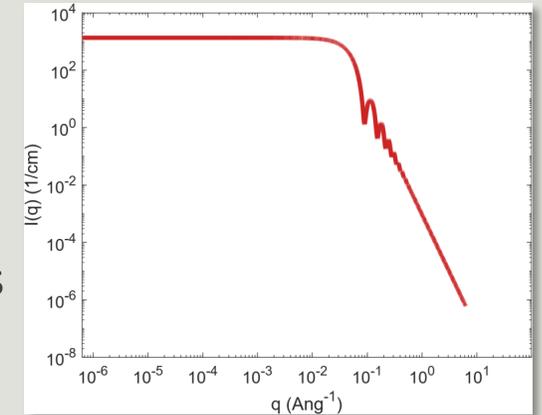
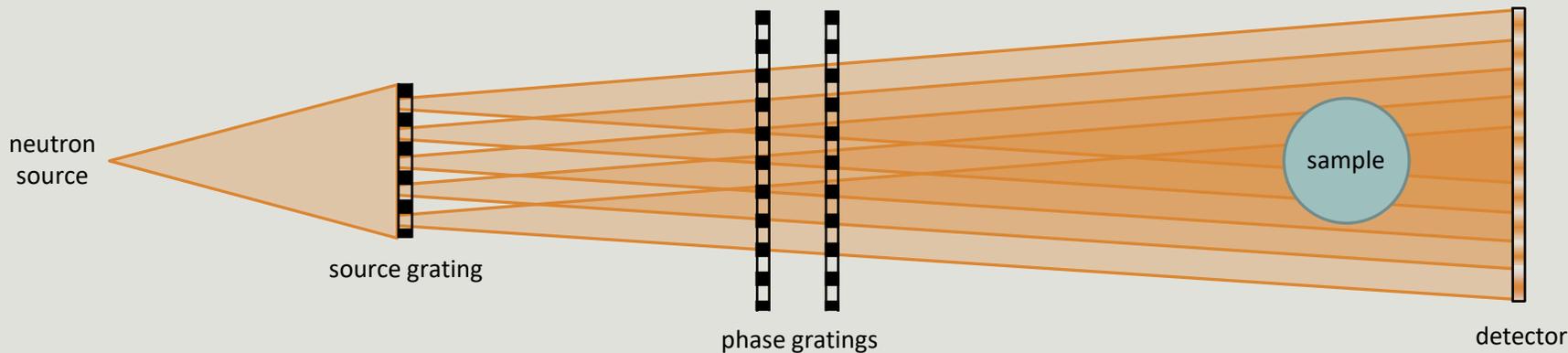


<https://www.nist.gov/image/scatteringgif-0>

- **Difficult to use for heterogenous samples**

# Neutron Interferometry & INFER

- Characterize materials at **multiple length scales** simultaneously
  - Dark field interferometry: 1nm-10 $\mu$ m (same as SAS)
  - Direct imaging: 50 $\mu$ m-100 $\mu$ m
- SAS information for more complex (**heterogenous** or **hierarchical**) materials
- Data is **related to SAS data** by a Hankel transform



# Sample System

- Self-assembling Sodium Dodecyl Sulfate /  $\beta$ -Cyclodextrin complex (SDS@2 $\beta$ -CD)
- Concentration-dependent phase behavior

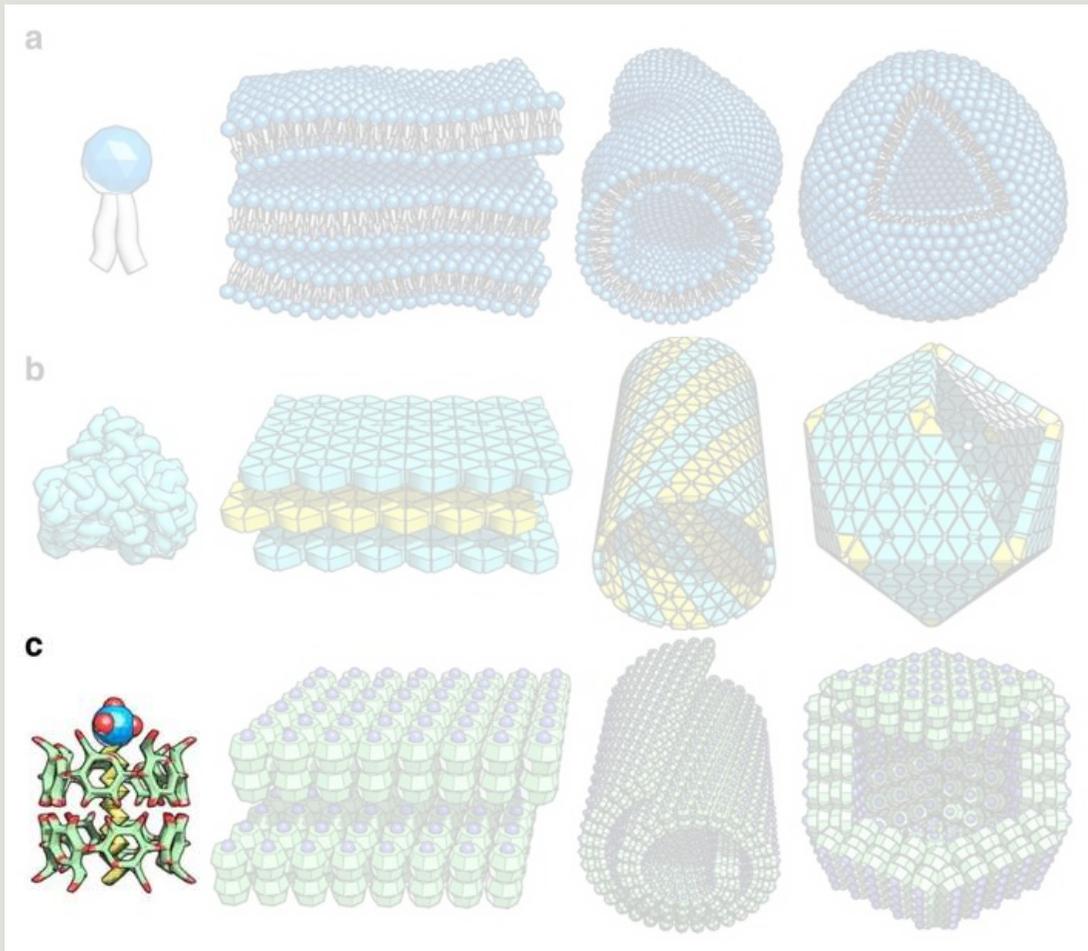
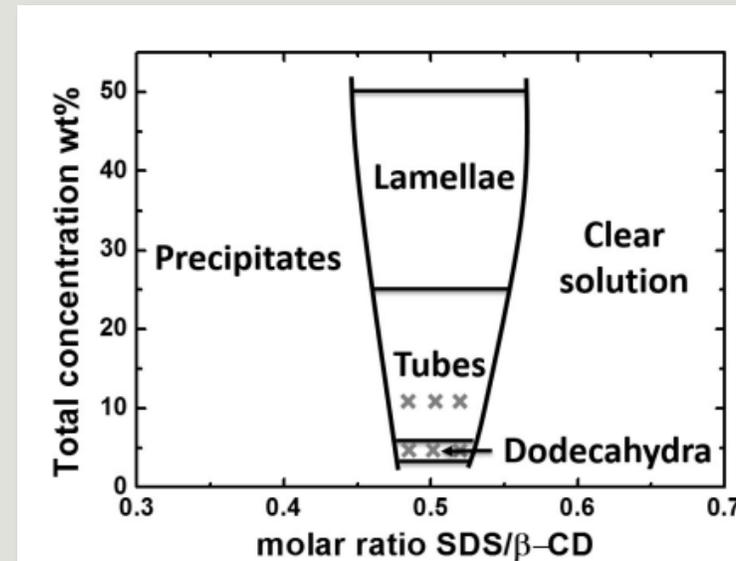


Figure 1. Stylized view of the lipid-like and protein-like self-assembly. Yang, S., Yan, Y., Huang, J. *et al.* Giant capsids from lattice self-assembly of cyclodextrin complexes. *Nat Commun* **8**, 15856 (2017). <https://doi.org/10.1038/ncomms15856>



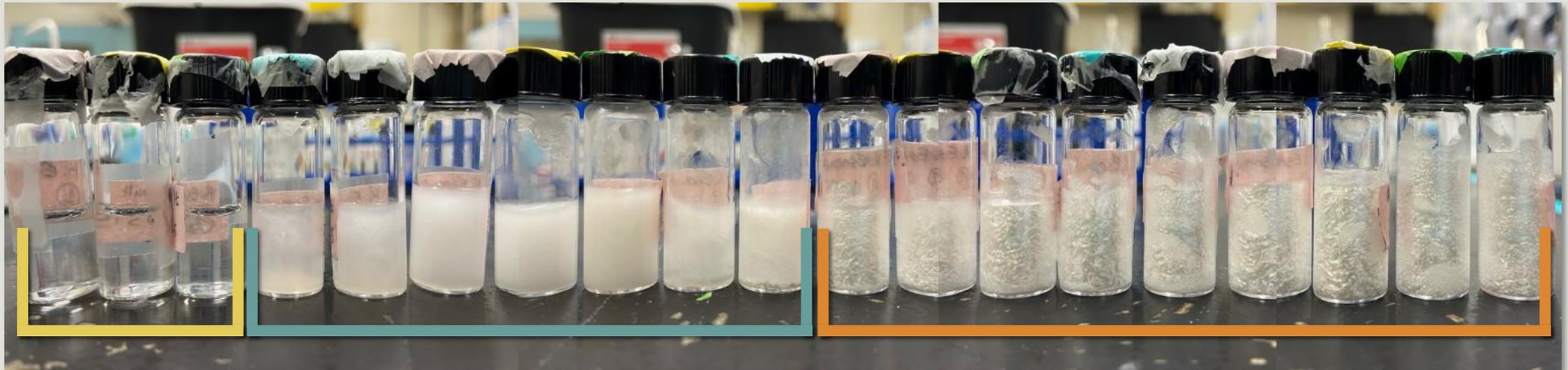
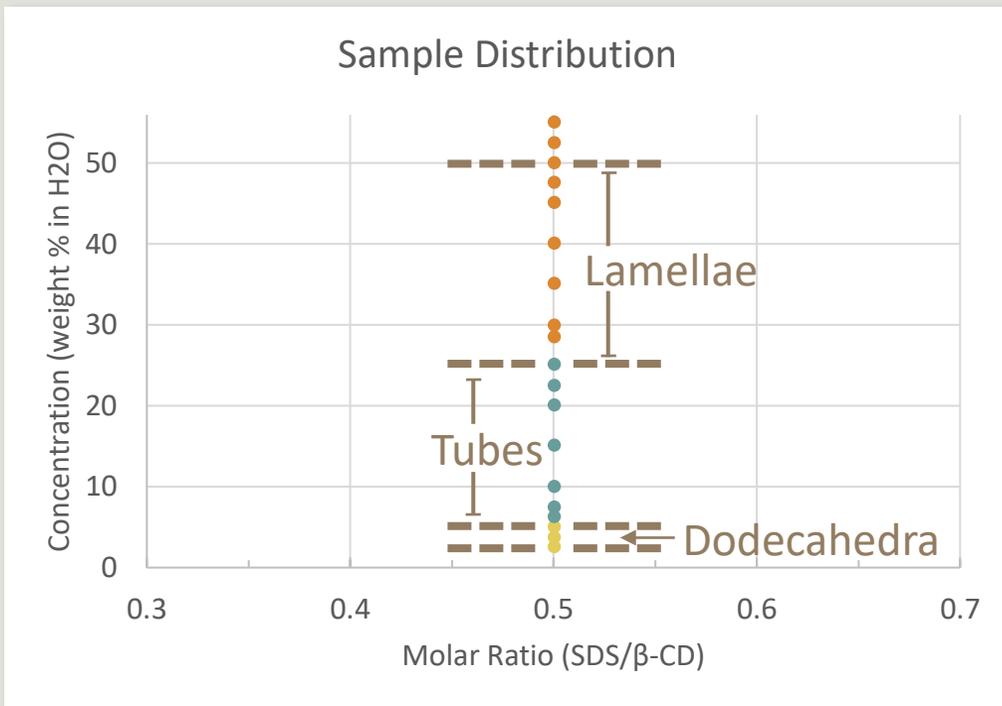
Supplementary Figure 1. The general phase diagram of the SDS/ $\beta$ -CD aqueous solution at room temperature. Yang, S., Yan, Y., Huang, J. *et al.* Giant capsids from lattice self-assembly of cyclodextrin complexes. *Nat Commun* **8**, 15856 (2017). <https://doi.org/10.1038/ncomms15856>

# My Objectives

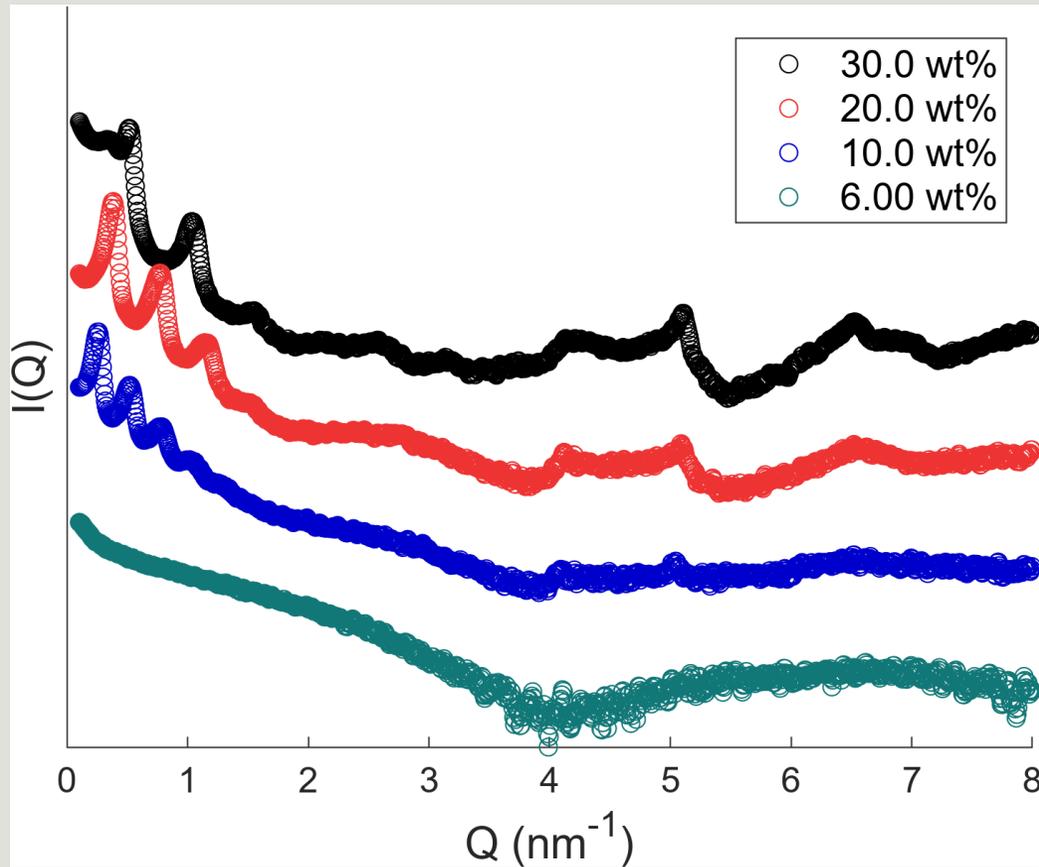
1. Develop a more comprehensive **phase space** for the SDS@2 $\beta$ -CD system using SAS characterization techniques
2. Facilitate the system's use in **testing the accuracy** of a novel far field interferometer

# Preliminary Samples

- **Recreate** literature findings
- Dynamic Light Scattering (DLS)
  - Look for trends in particle radii
- Small Angle X-Ray Scattering (SAXS)
  - Get structural information from data fitting



# SAXS results



\*\*\*Graphs are artificially spaced out along y-axis for clarity\*\*\*

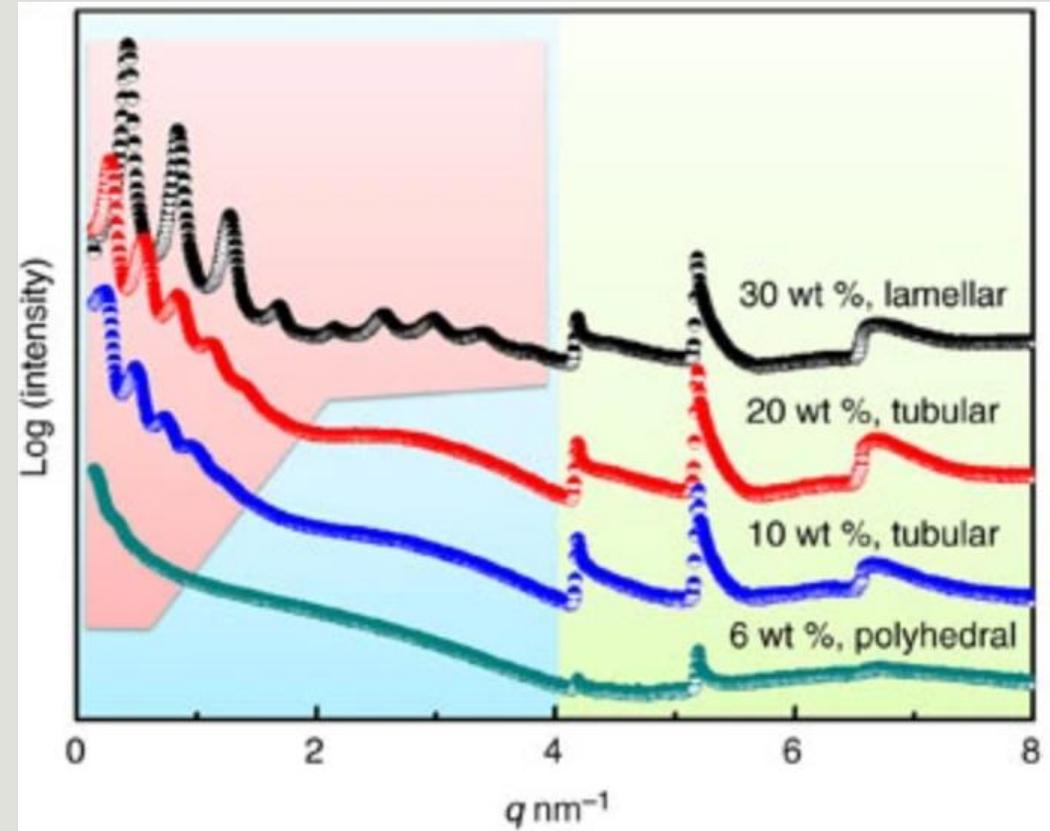
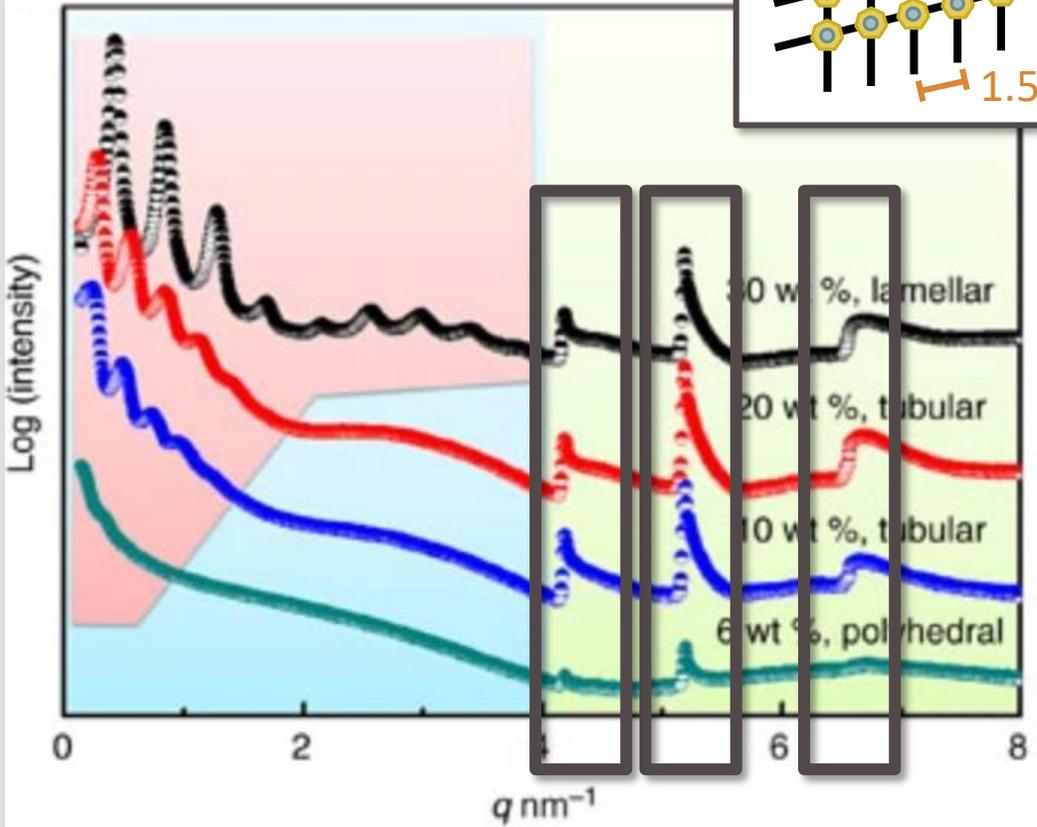
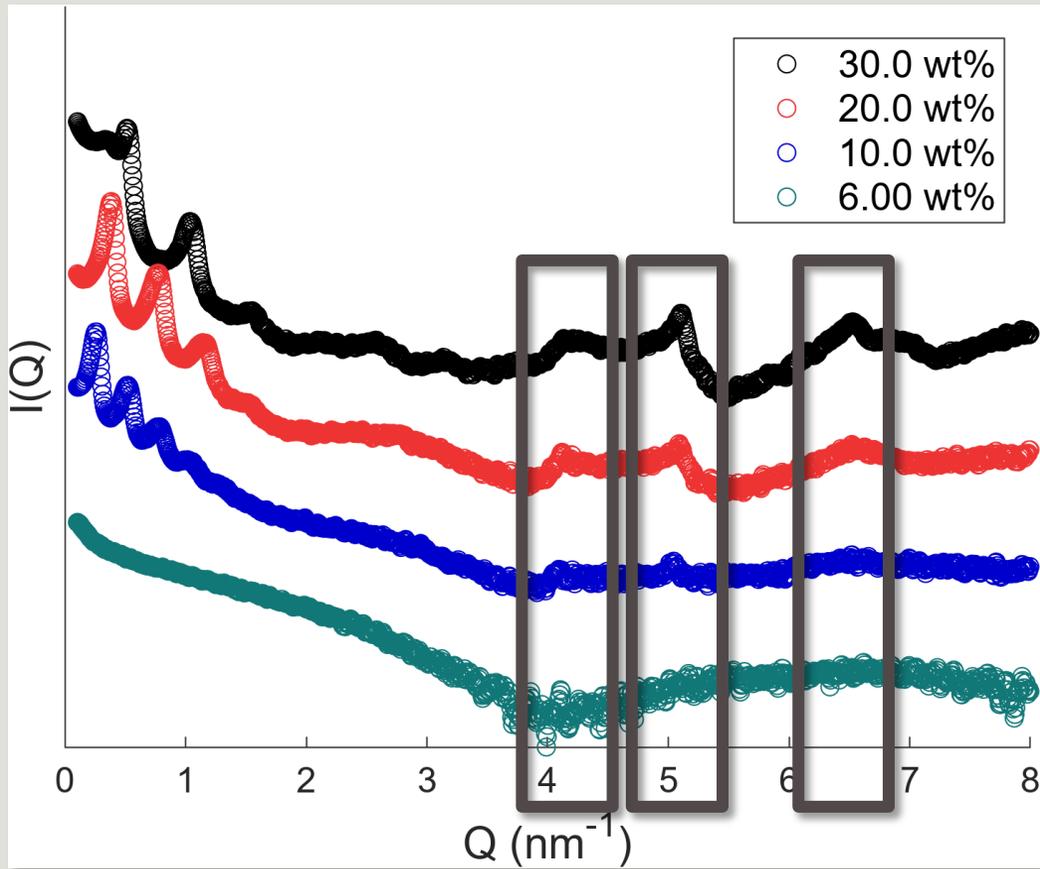
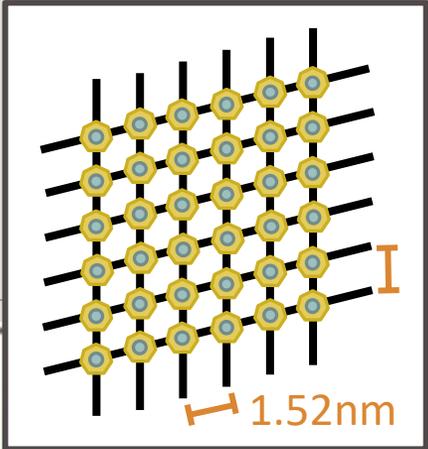


Figure 4a. X-ray scattering of the SDS@2 $\beta$ -CD structures. Yang, S., Yan, Y., Huang, J. *et al.* Giant capsids from lattice self-assembly of cyclodextrin complexes. *Nat Commun* 8, 15856 (2017). <https://doi.org/10.1038/ncomms15856>

# SAXS results

$$\frac{2\pi}{4.1} \approx 1.52$$

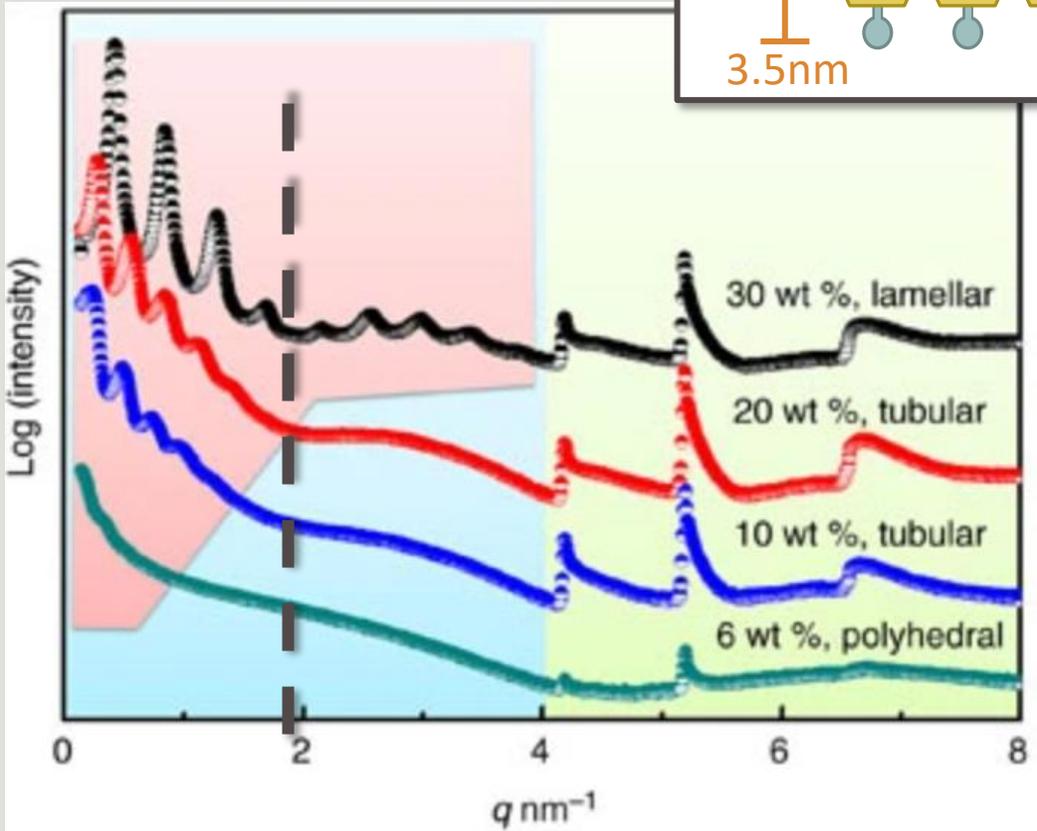
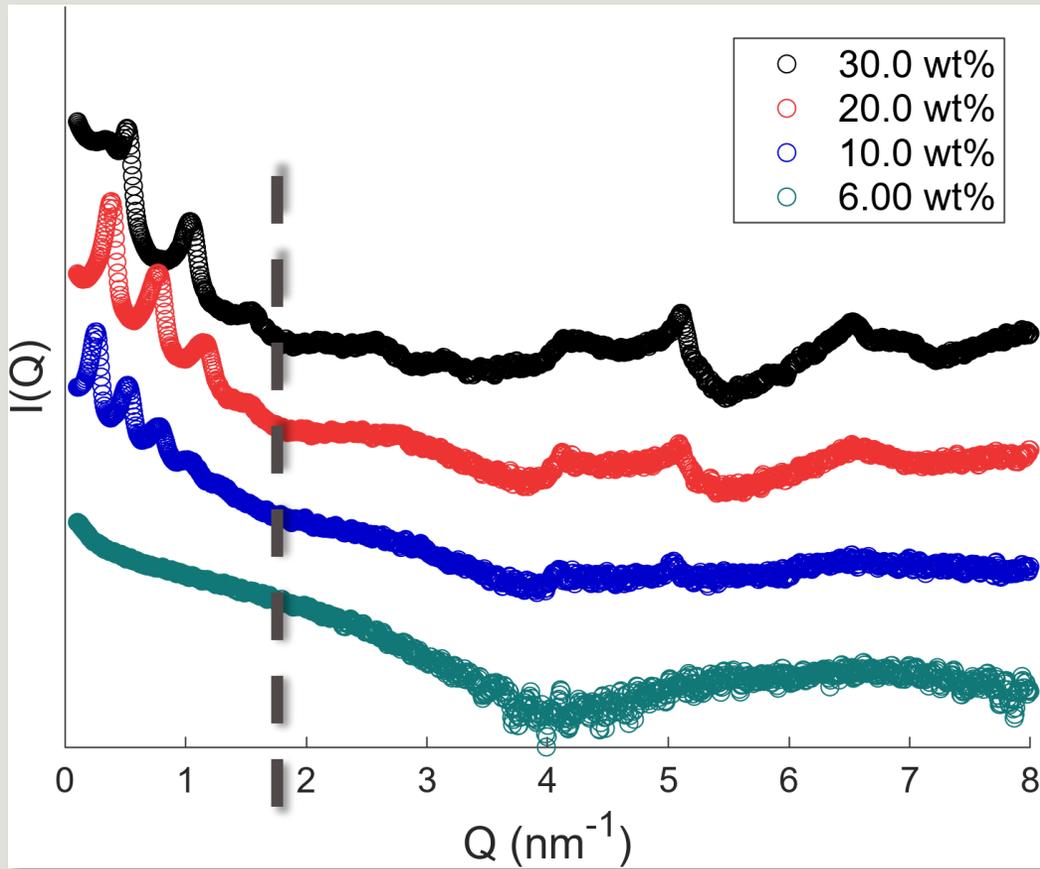
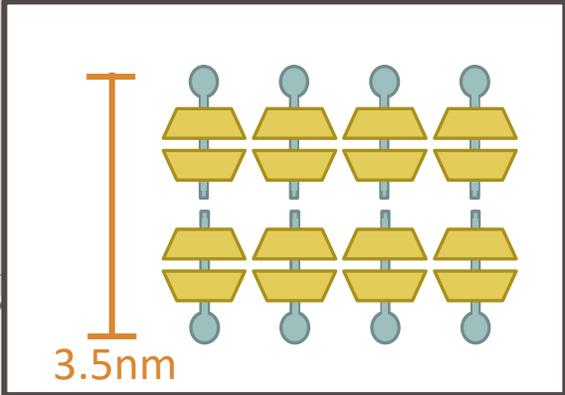


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Figure 4a. X-ray scattering of the SDS@2 $\beta$ -CD structures. Yang, S., Yan, Y., Huang, J. *et al.* Giant capsids from lattice self-assembly of cyclodextrin complexes. *Nat Commun* 8, 15856 (2017). <https://doi.org/10.1038/ncomms15856>

# SAXS results

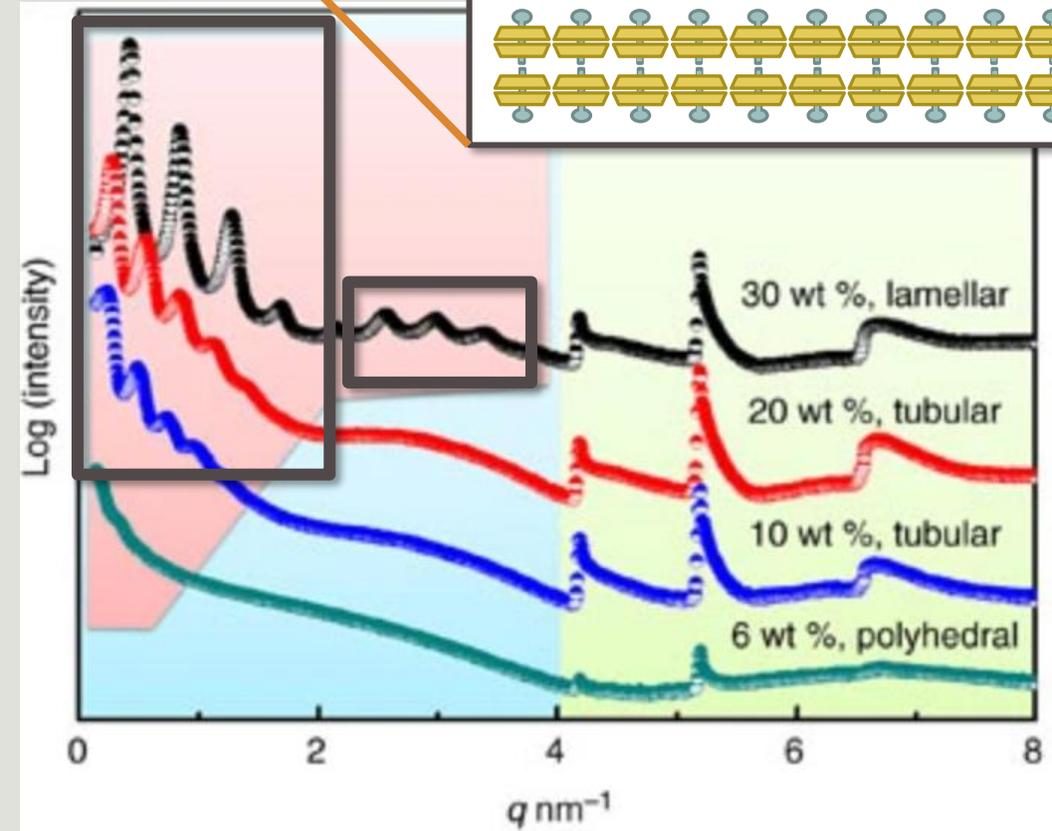
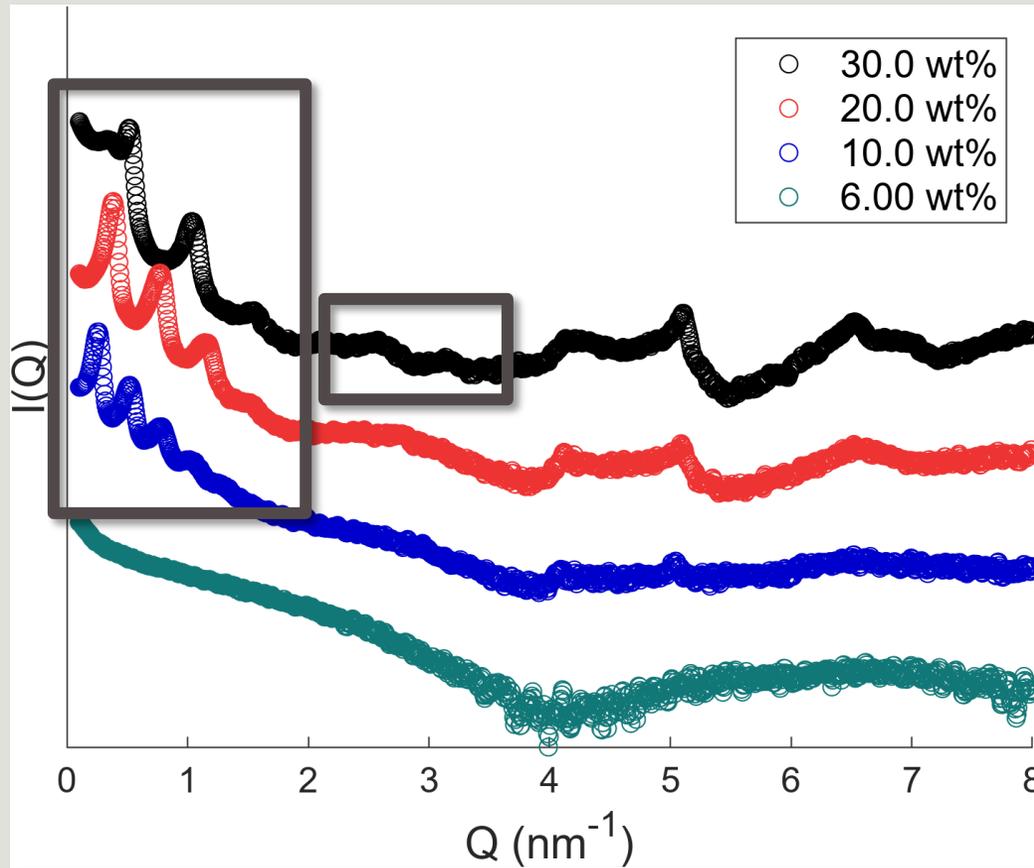
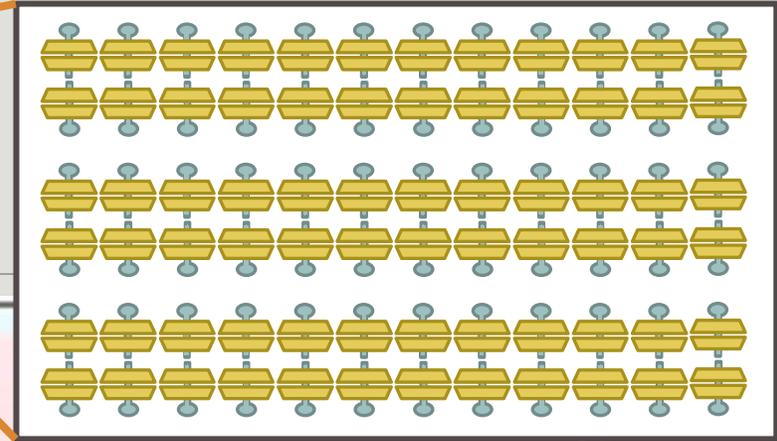
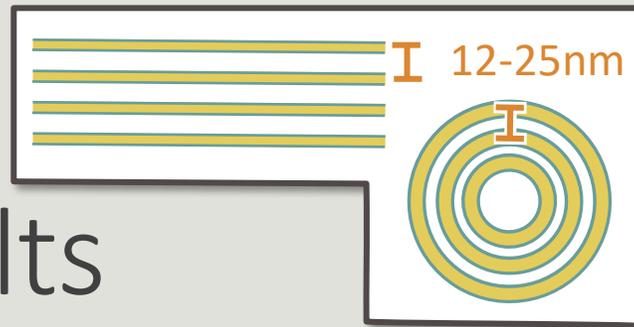
$$\frac{2\pi}{1.8} \approx 3.5$$



\*\*\*Graphs are artificially spaced out along y-axis for clarity\*\*\*

Figure 4a. X-ray scattering of the SDS@2β-CD structures. Yang, S., Yan, Y., Huang, J. *et al.* Giant capsids from lattice self-assembly of cyclodextrin complexes. *Nat Commun* 8, 15856 (2017). <https://doi.org/10.1038/ncomms15856>

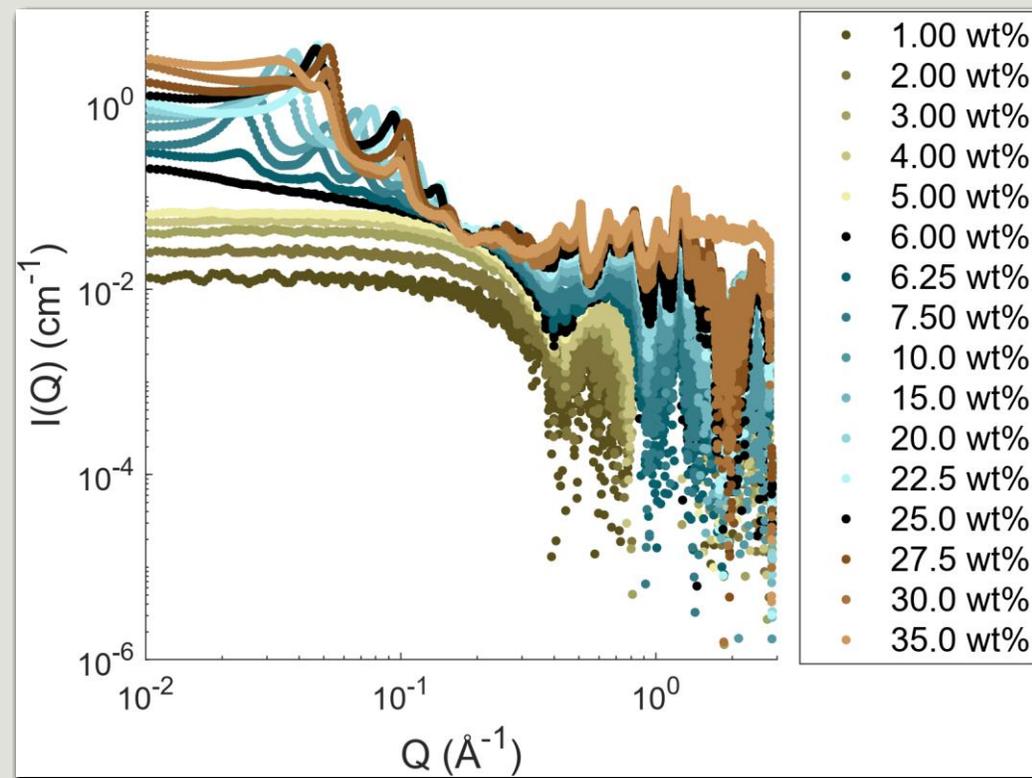
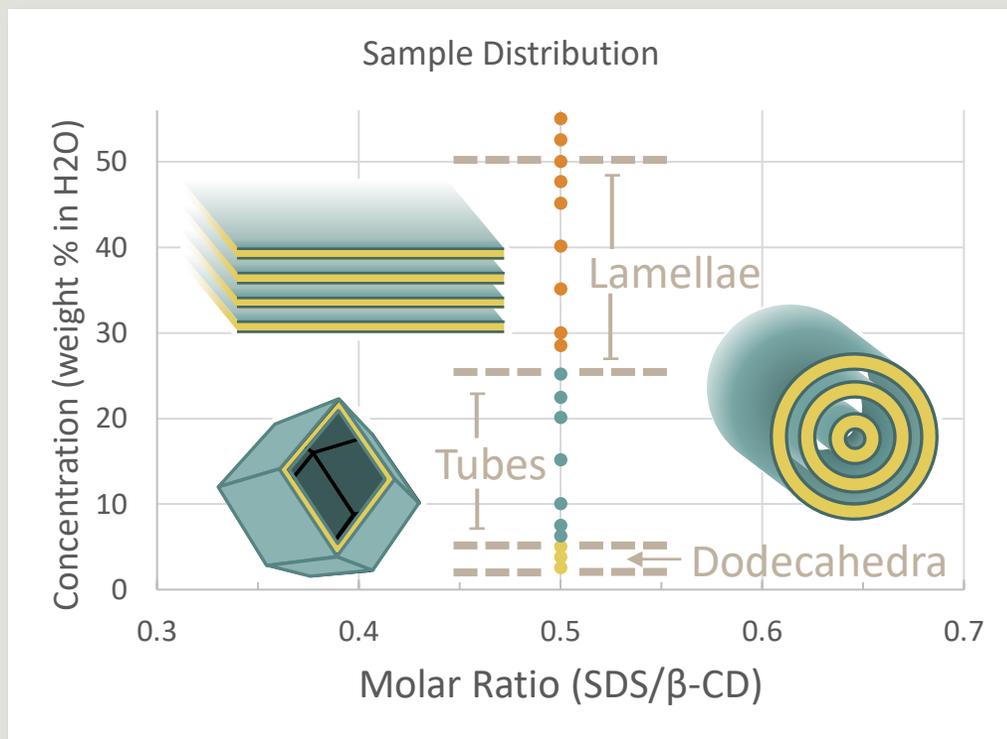
# SAXS results



\*\*\*Graphs are artificially spaced out along y-axis for clarity\*\*\*

Figure 4a. X-ray scattering of the SDS@2̢-CD structures. Yang, S., Yan, Y., Huang, J. *et al.* Giant capsids from lattice self-assembly of cyclodextrin complexes. *Nat Commun* 8, 15856 (2017). <https://doi.org/10.1038/ncomms15856>

# SAXS results

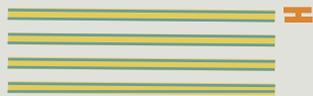


# Data Fitting

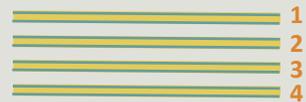
- SASView ([www.sasview.org](http://www.sasview.org))
  - *lamellar\_stack\_paracrystal* form factor
    - Incorporates **bilayer form factor** and a term to account for interference caused by having **lamellar stacks of bilayers**

- Key parameters:

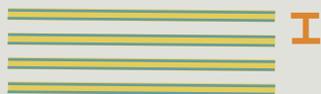
- **thickness** – thickness of layers



- **Nlayers** – number of layers

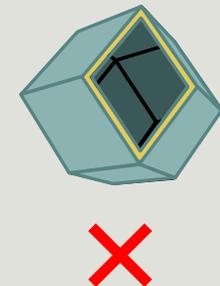
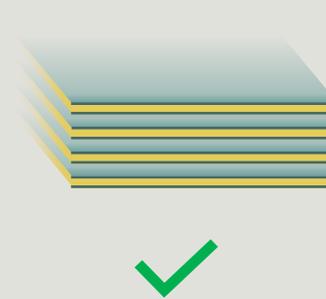


- **d\_spacing** – spacing between layers

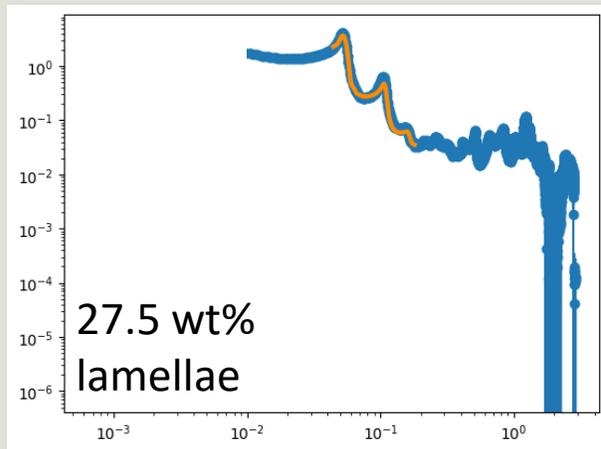
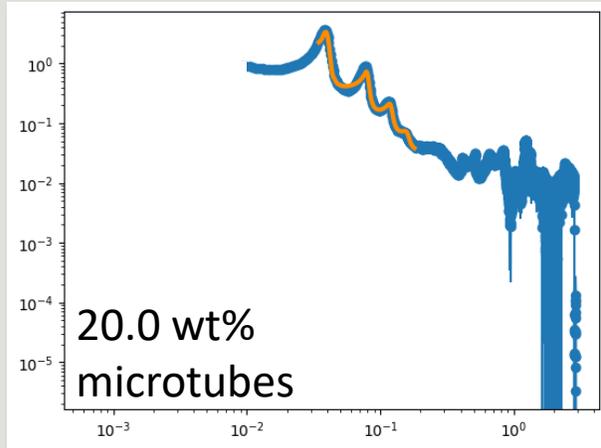


$$I(Q) = \phi \Delta \rho^2 \mathbf{P}(Q) S(Q)$$

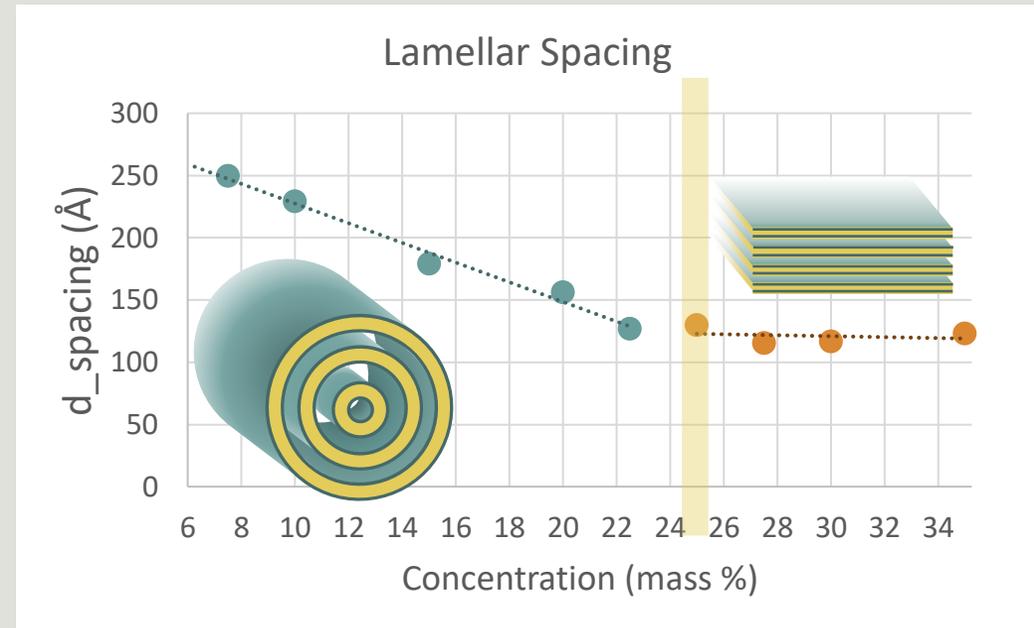
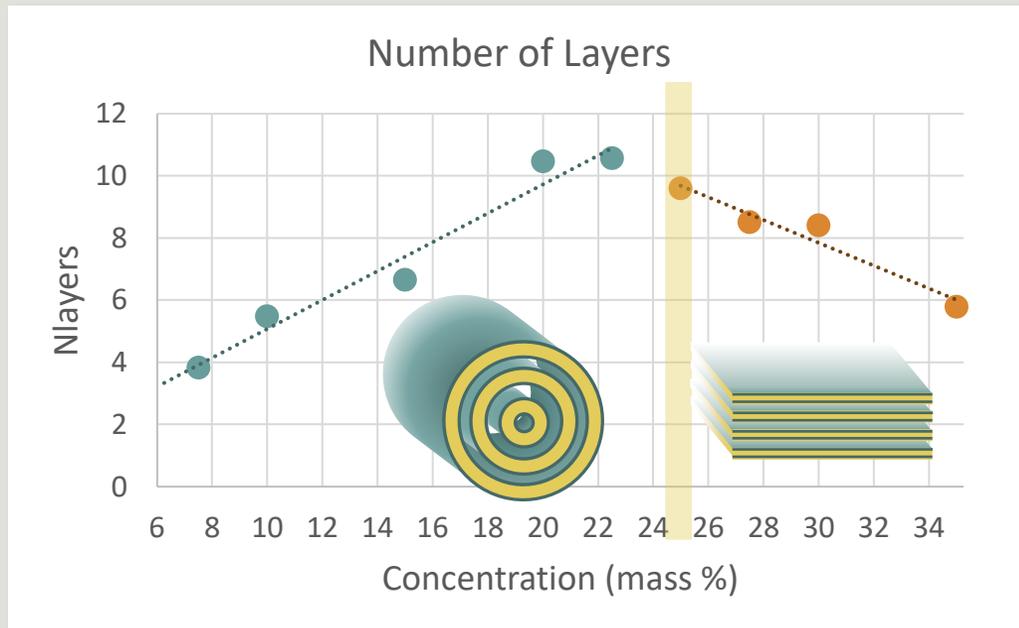
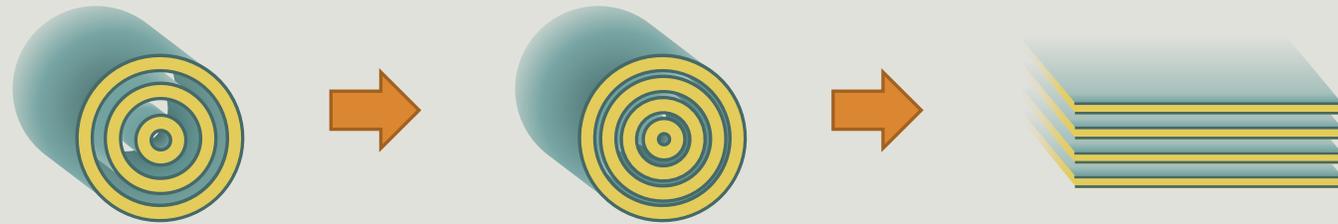
- Used for **lamellar** phase and **microtube** phase



# Data Fitting

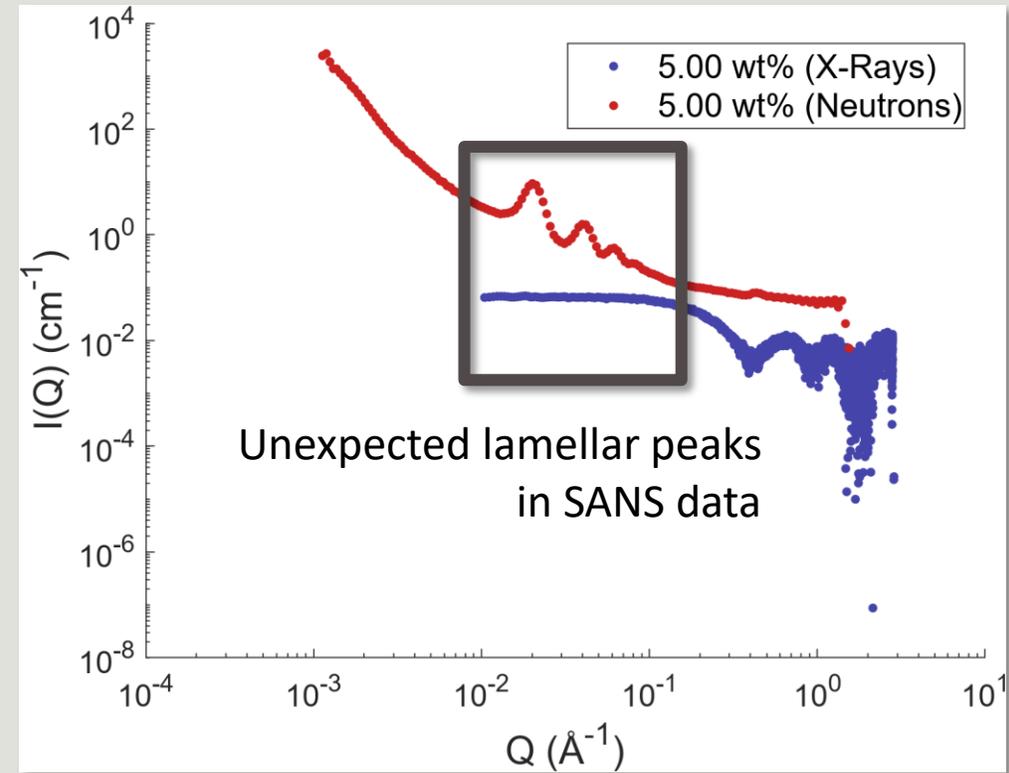
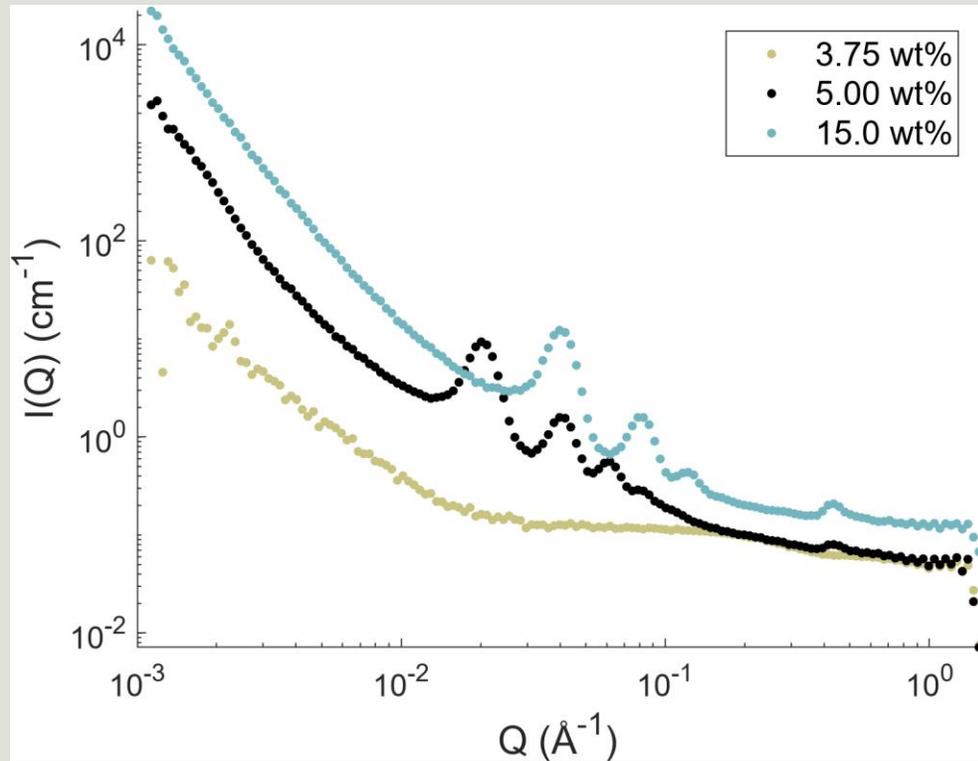


# Data Fitting



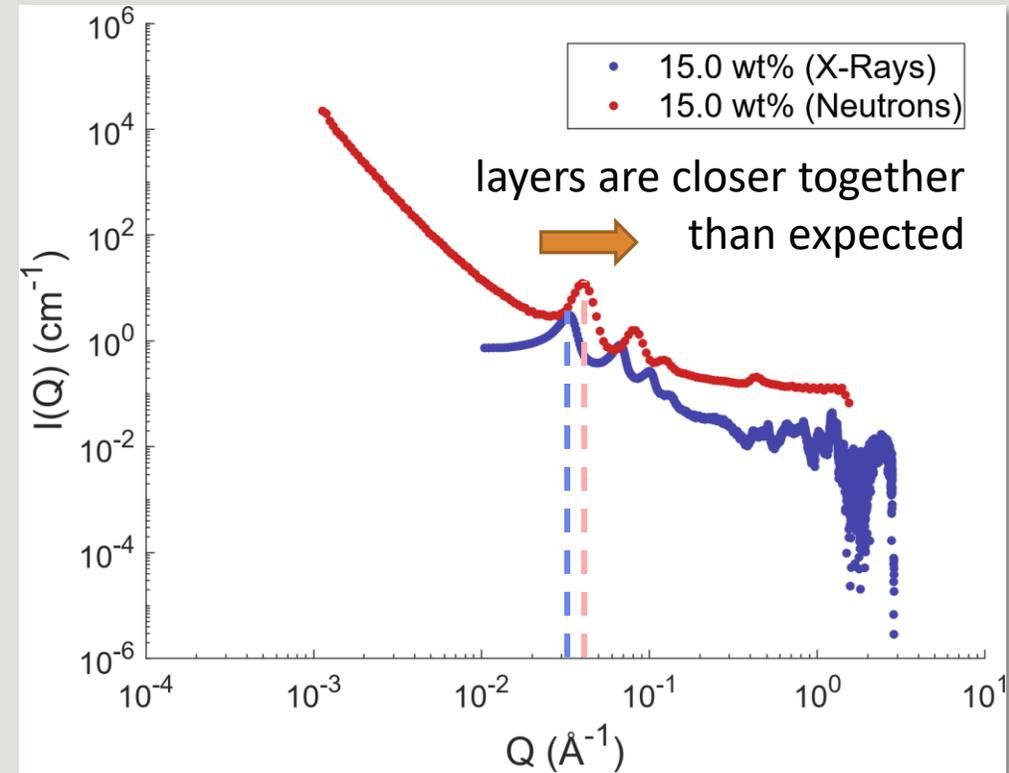
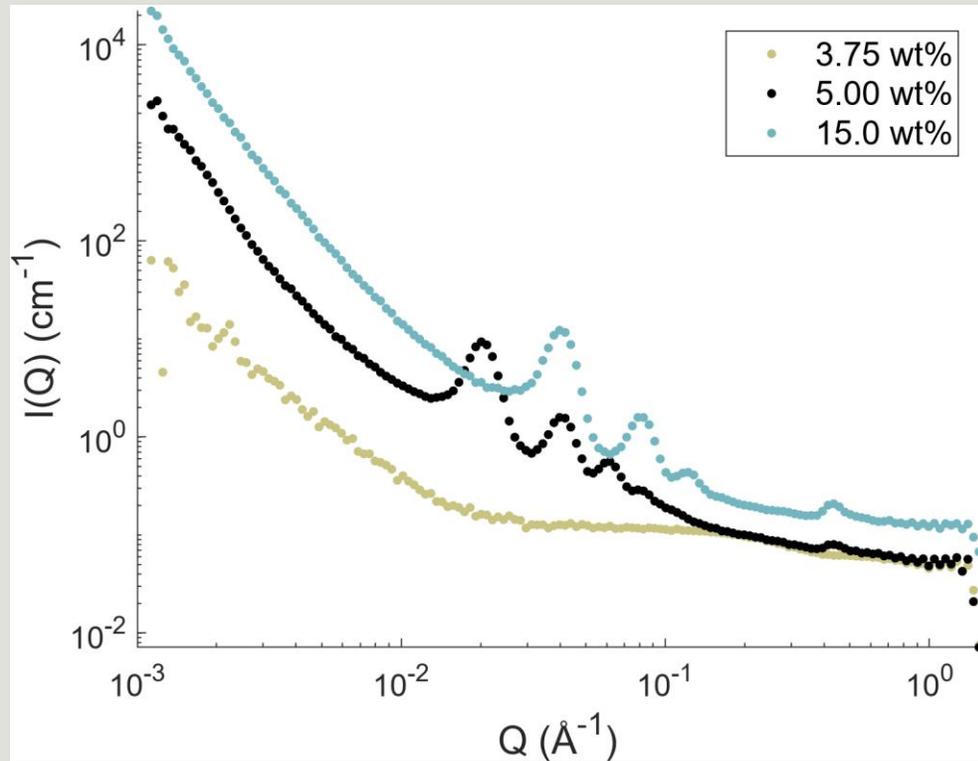
\*\*\* Error bars are too small to be visible on these graphs \*\*\*

# SANS Data



\*\*\*SANS data was collected by Katie Weigandt and Kelsi Rehmann at the Australian Nuclear Science and Technology Organisation (ANSTO) on the Bilby beamline\*\*\*

# SANS Data



- Samples prepared in **D2O** rather than H2O

\*\*\*SANS data was collected by Katie Weigandt and Kelsi Rehmann at the Australian Nuclear Science and Technology Organisation (ANSTO) on the Bilby beamline\*\*\*

# Transformation to Dark Field Intensity

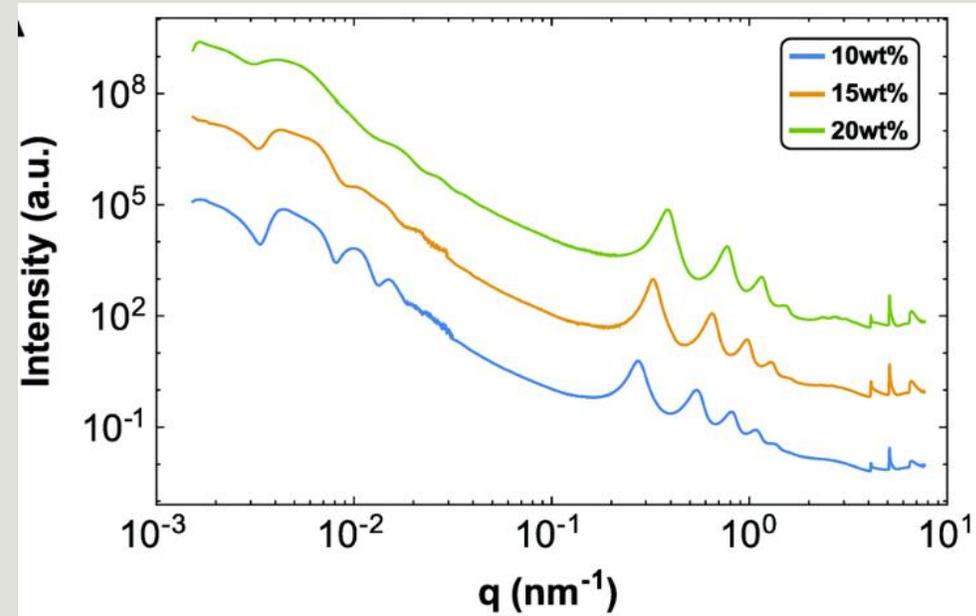
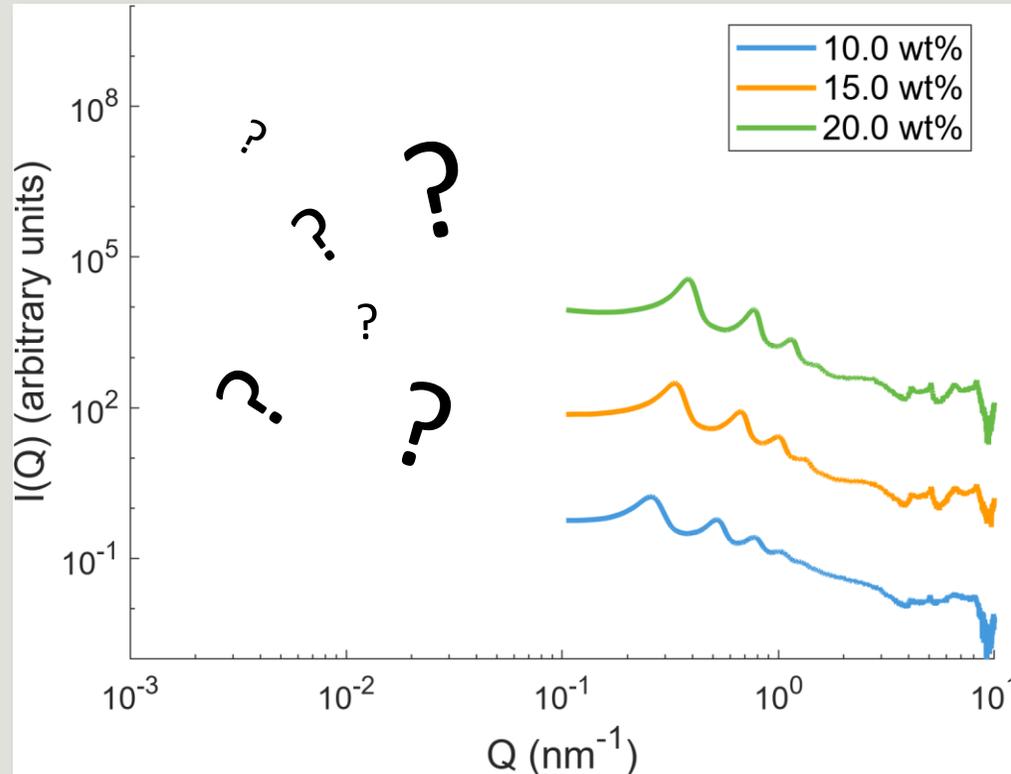
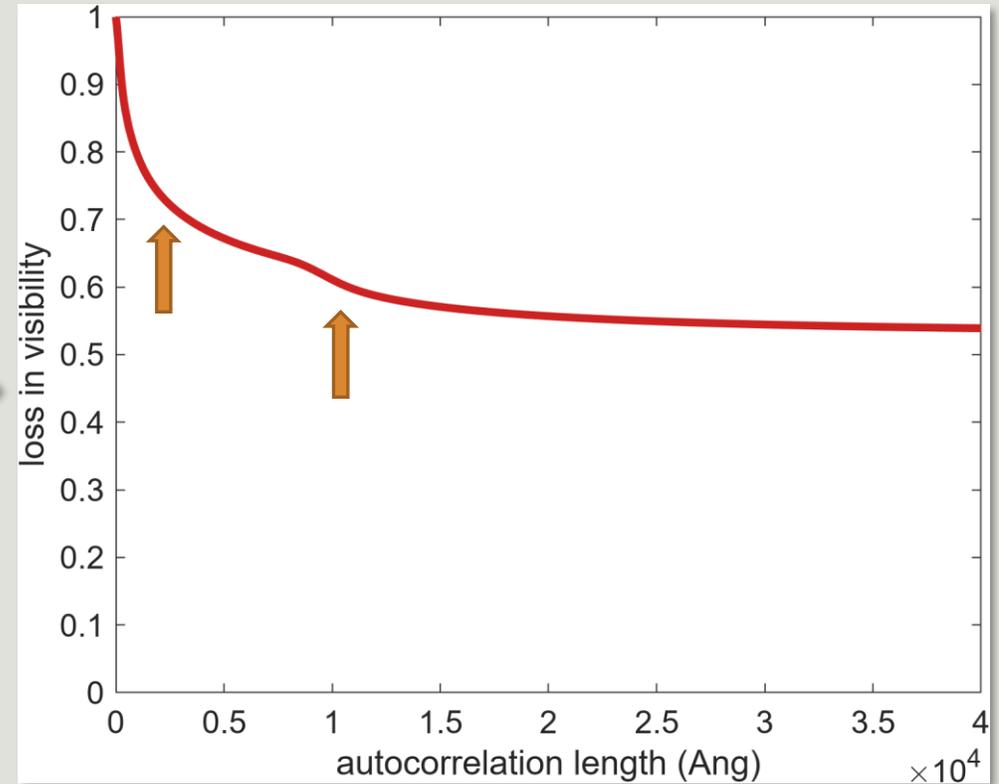
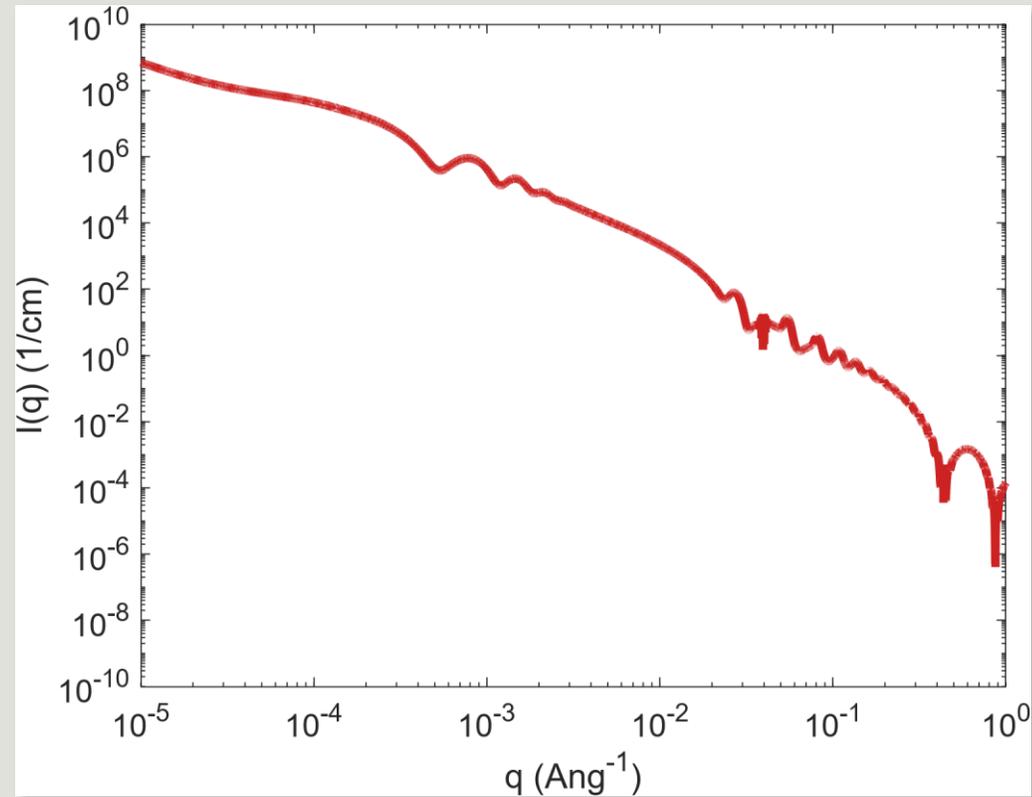


Figure 4a. The response of the thermo-reversible microtubes to variations in concentration. Ouhajji, Samia, *et al.* In Situ Observation of Self-Assembly of Sugars and Surfactants from Nanometres to Microns. *Soft Matter*, vol. 13, no. 13, Mar. 2017, pp. 2421–25. [pubs.rsc.org](https://pubs.rsc.org), <https://doi.org/10.1039/C7SM00109F>.

# Transformation to Dark Field Intensity

- Add *hollow\_cylinder* form factor to **approximate low-Q data** from literature values



# Conclusions & Future Research

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- This system is a **good candidate** for validating data from the new interferometer
- Areas for further study:
  - Other **cyclodextrins**
  - Effect of **D2O**
  - More powerful **SAS** instrument for lower Q study
  - Better **models** for dodecahedral and microtube phases

# References

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1. Landman, J. *et al.* Inward growth by nucleation: Multiscale self-assembly of ordered membranes. *Sci. Adv.* **4**, eaat1817 (2018). <https://doi.org/10.1126/sciadv.aat1817>
2. Strobl, M. General solution for quantitative dark-field contrast imaging with grating interferometers. *Sci Rep* **4**, 7243 (2014). <https://doi.org/10.1038/srep07243>
3. Wolf, C. M. *et al.* Blend Morphology in Polythiophene–Polystyrene Composites from Neutron and X-ray Scattering. *Macromolecules* **54** (6), 2960 (2021). <https://doi.org/10.1021/acs.macromol.0c02512>
4. Yang, S., Yan, Y., Huang, J. *et al.* Giant capsids from lattice self-assembly of cyclodextrin complexes. *Nat Commun* **8**, 15856 (2017). <https://doi.org/10.1038/ncomms1585>

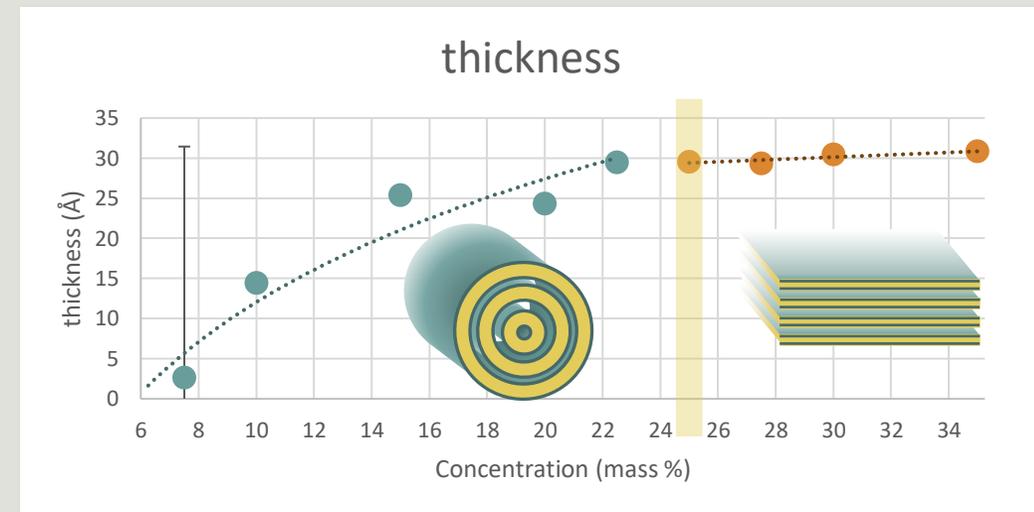
*This work benefited from the use of the SasView application, originally developed under NSF award DMR-0520547. SasView also contains code developed with funding from the European Union's Horizon 2020 research and innovation programme under the SINE2020 project, grant agreement No 654000.*

# Supplemental Slides

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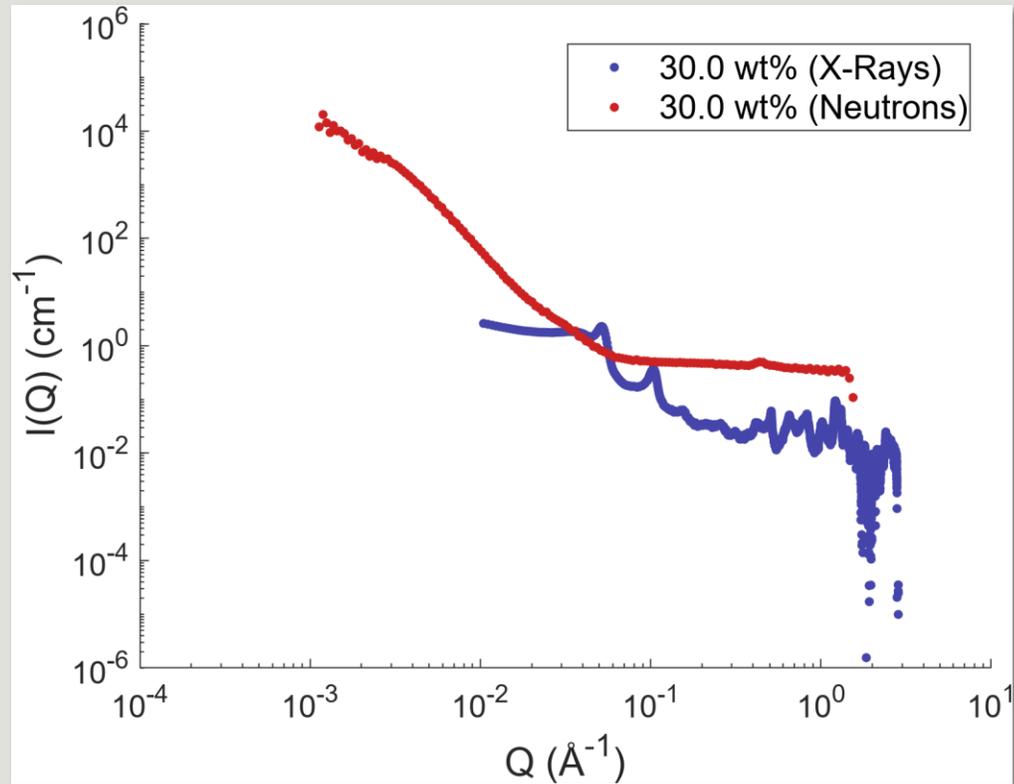
# *lamellar\_stack\_paracrystal* thickness parameter

- Bilayer thickness should be constant
- Further evidence this model may not be the best fit for the microtube phase
- Perhaps an artifact from the curvature of the tubes
- Note the error bar on the 7.5 wt% sample



# 30 wt% Sample SANS Data

- Suspected issues loading sample – lamellar peaks absent



# *lamellar\_stack\_paracrystal* Model Fitting – Raw Data

sample	concentration	background	error	scale	error	Nlayers	error	d_spacing	error	sigma_d	error	thickness	error	$\chi^2$
5A	7.5	3.6318E-06	2.8093E-02	3.9084E-01	1.1141E-03	3.8269E+00	4.4691E-02	2.4934E+02	1.4759E-01	6.2764E-02	3.2191E-03	2.6302E+00	2.8842E+01	8.9507
6A	10	1.7741E-07	3.0989E-03	7.6143E-01	2.4814E-03	5.4764E+00	5.9880E-02	2.2914E+02	8.2188E-02	6.3246E-02	5.1847E-04	1.4399E+01	5.4875E-01	18.652
7A	15	2.8180E-02	2.7798E-04	1.7703E+00	4.5201E-03	6.6491E+00	5.8205E-02	1.7909E+02	4.3471E-02	5.7677E-02	3.5589E-04	2.5379E+01	6.5646E-02	22.91
8A	20	2.5091E-02	3.7408E-04	2.0632E+00	5.6064E-03	1.0457E+01	1.5140E-01	1.5586E+02	3.6304E-02	6.2845E-02	3.5145E-04	2.4295E+01	7.0081E-02	42.746
9A	22.5	4.5582E-02	7.9176E-04	3.2838E+00	1.8328E-02	1.0569E+01	1.2259E-01	1.2689E+02	2.7204E-02	5.1189E-02	4.7271E-04	2.9457E+01	1.2023E-01	56.273
10A	25	3.0886E-02	7.6085E-04	3.8791E+00	1.7334E-02	9.5918E+00	1.5194E-01	1.2982E+02	3.5502E-02	1.7334E-02	4.4086E-04	2.9528E+01	1.0042E-01	25.784
11A	27.5	2.8919E-02	7.1873E-04	3.9127E+00	1.7799E-02	8.5022E+00	8.0421E-02	1.1546E+02	2.4681E-02	5.7803E-02	4.2741E-04	2.9367E+01	1.0050E-01	28.406
12B	30	3.9406E-02	3.9193E-04	2.2963E+00	1.0334E-02	8.4077E+00	8.8577E-02	1.1657E+02	2.8128E-02	5.9877E-02	5.2205E-04	3.0463E+01	9.7483E-02	18.874
13B	35	3.9630E-02	3.2523E-04	1.8982E+00	8.9735E-03	5.7868E+00	7.7784E-02	1.2298E+02	5.2324E-02	9.3762E-02	6.7624E-04	3.0820E+01	1.0243E-01	9.2532