



Boeing Research & Technology

Absolute Accuracy & Robot Calibration

Phil Freeman

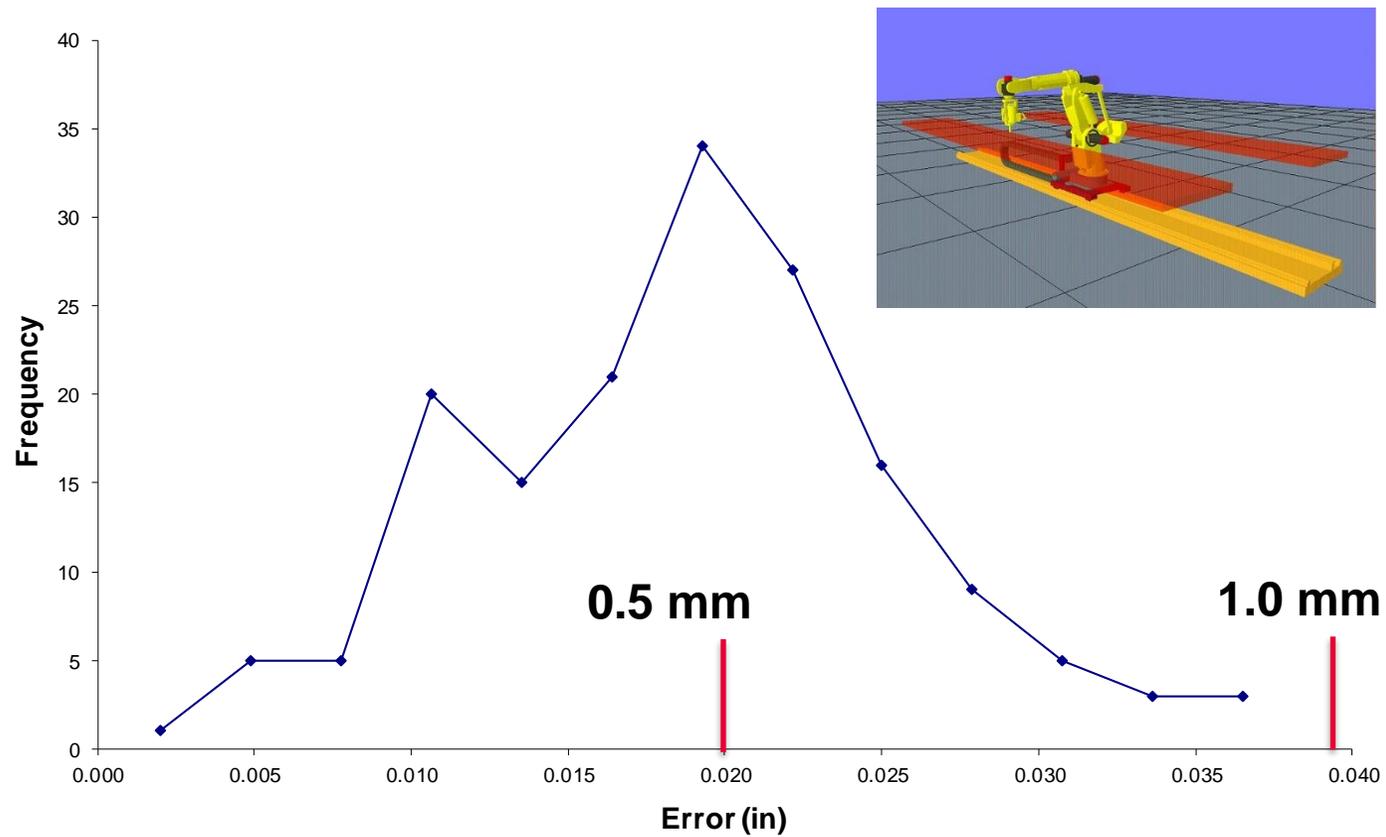
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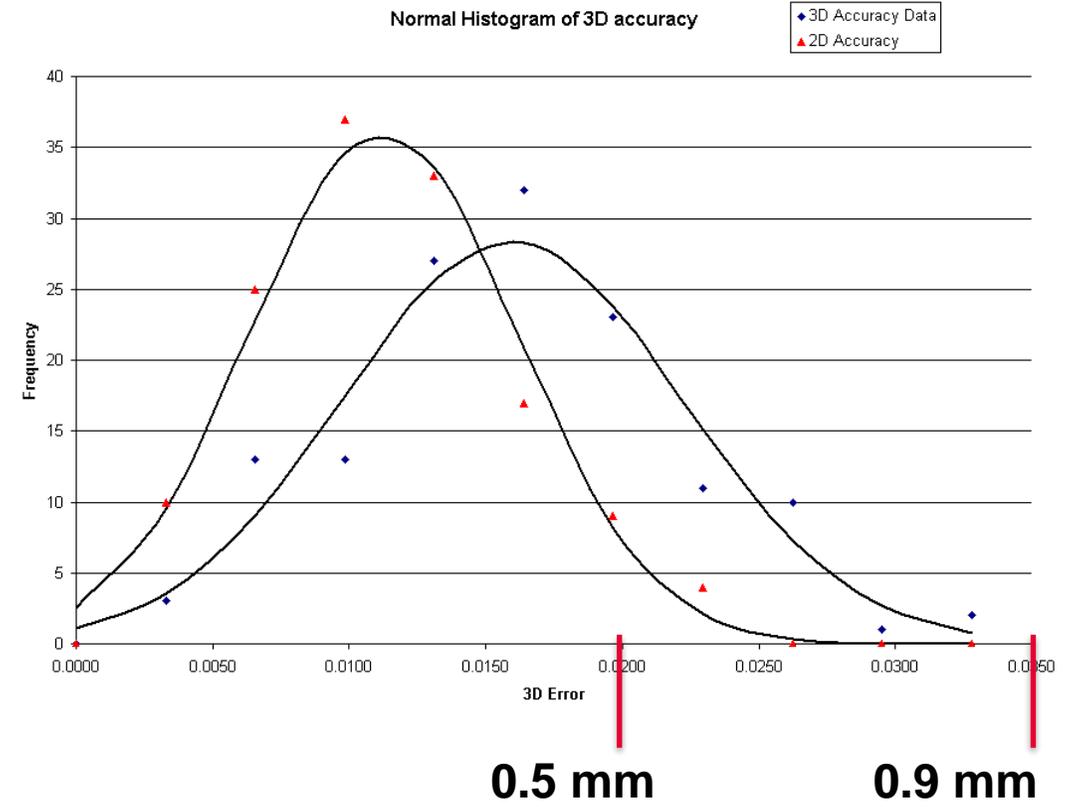


c. 1999

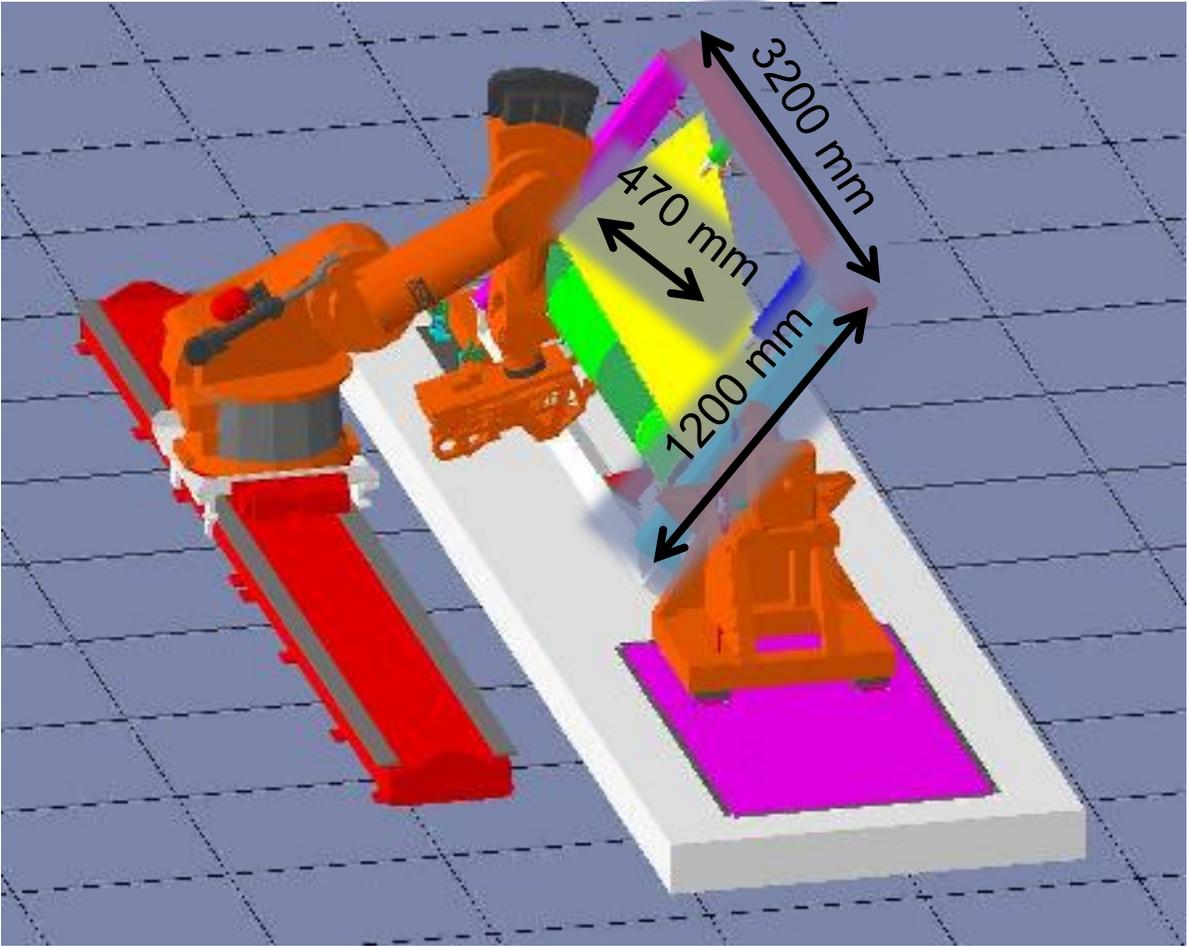
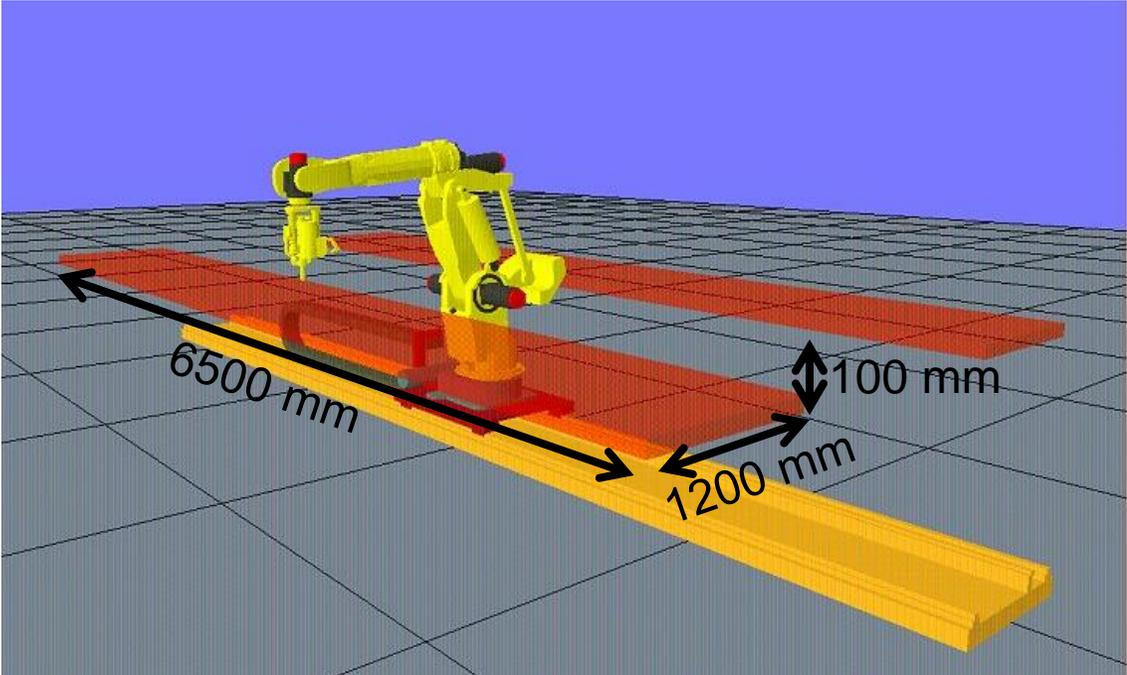
3-D Error Histogram



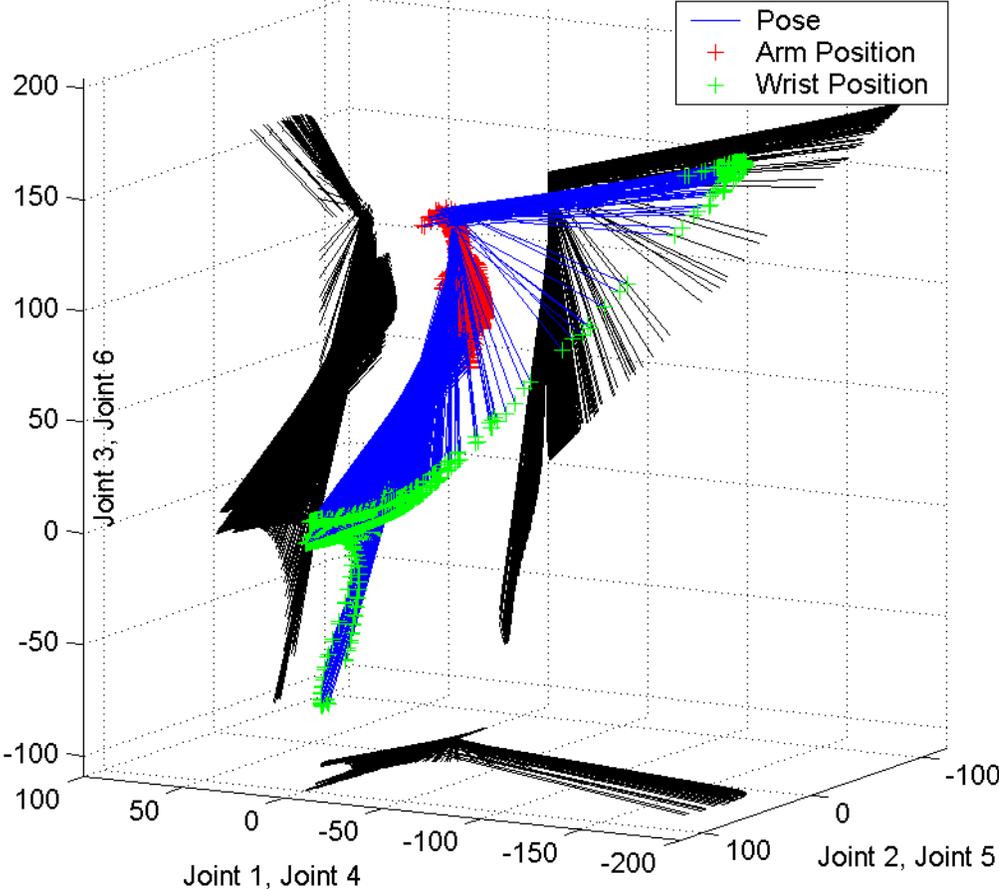
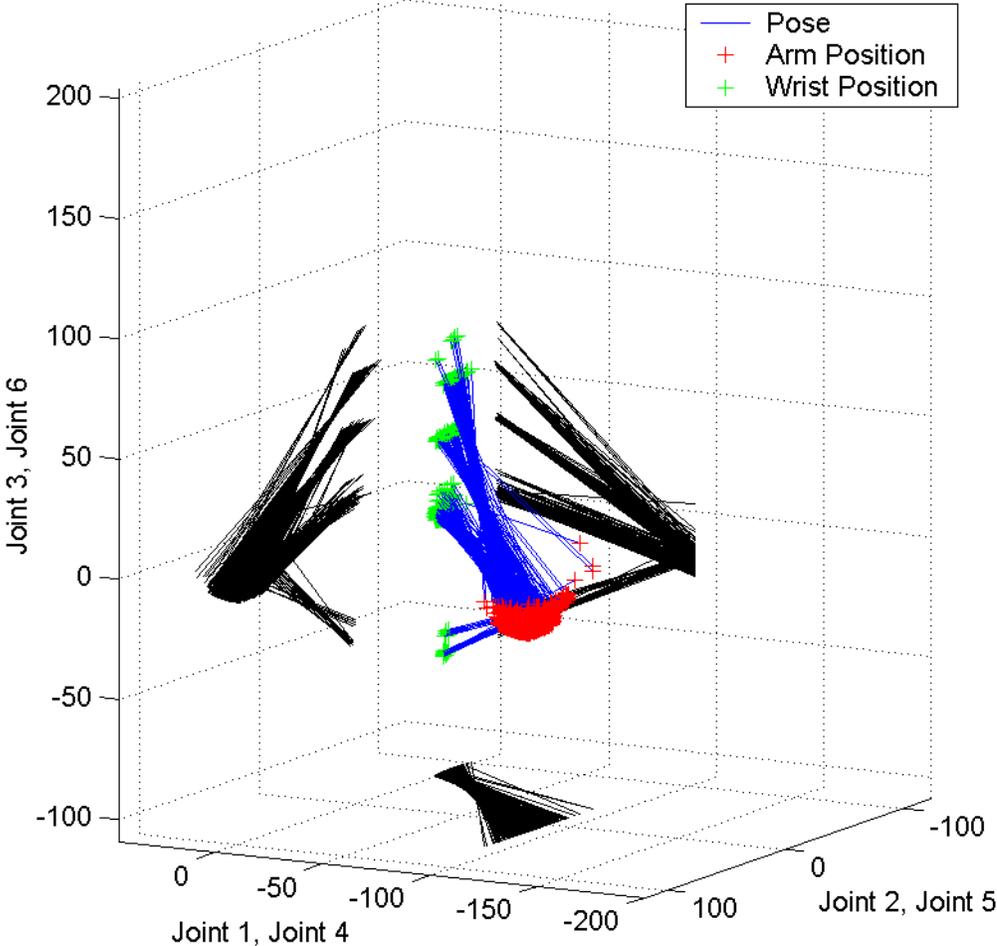
c. 2002



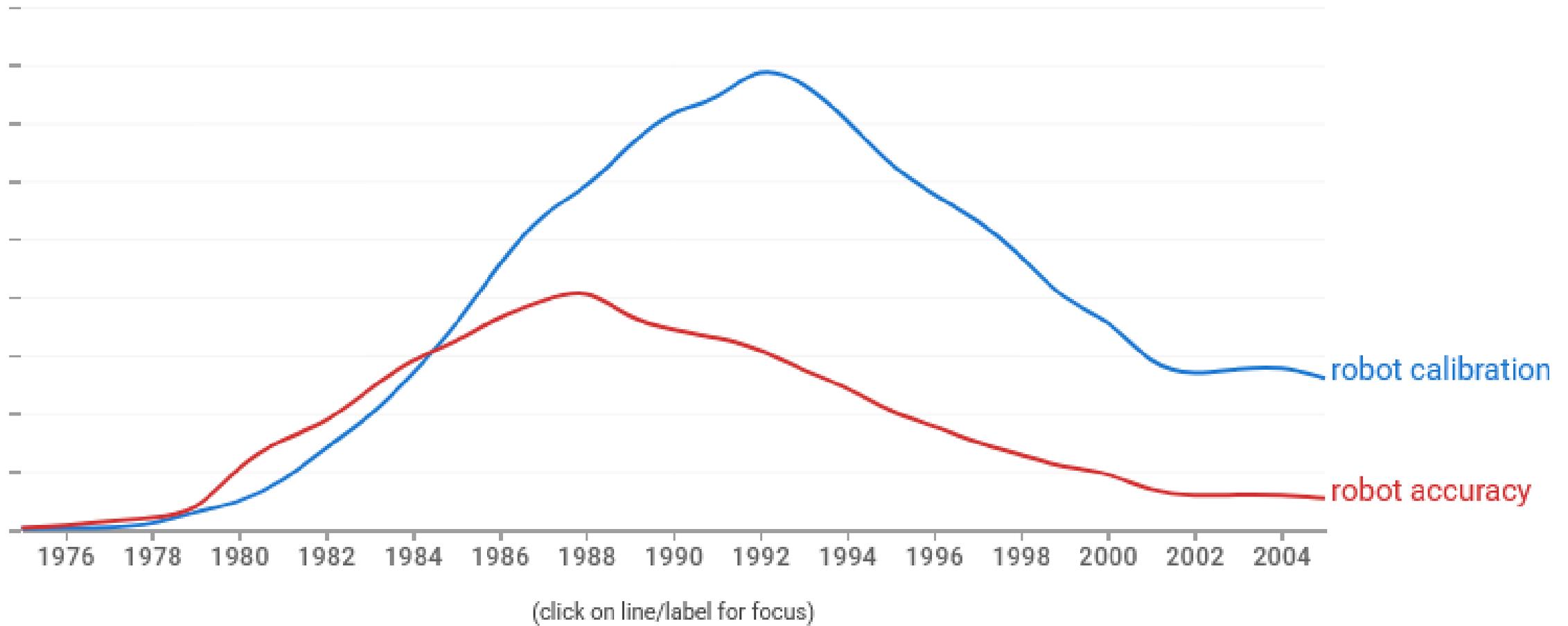
Comparable – But not really



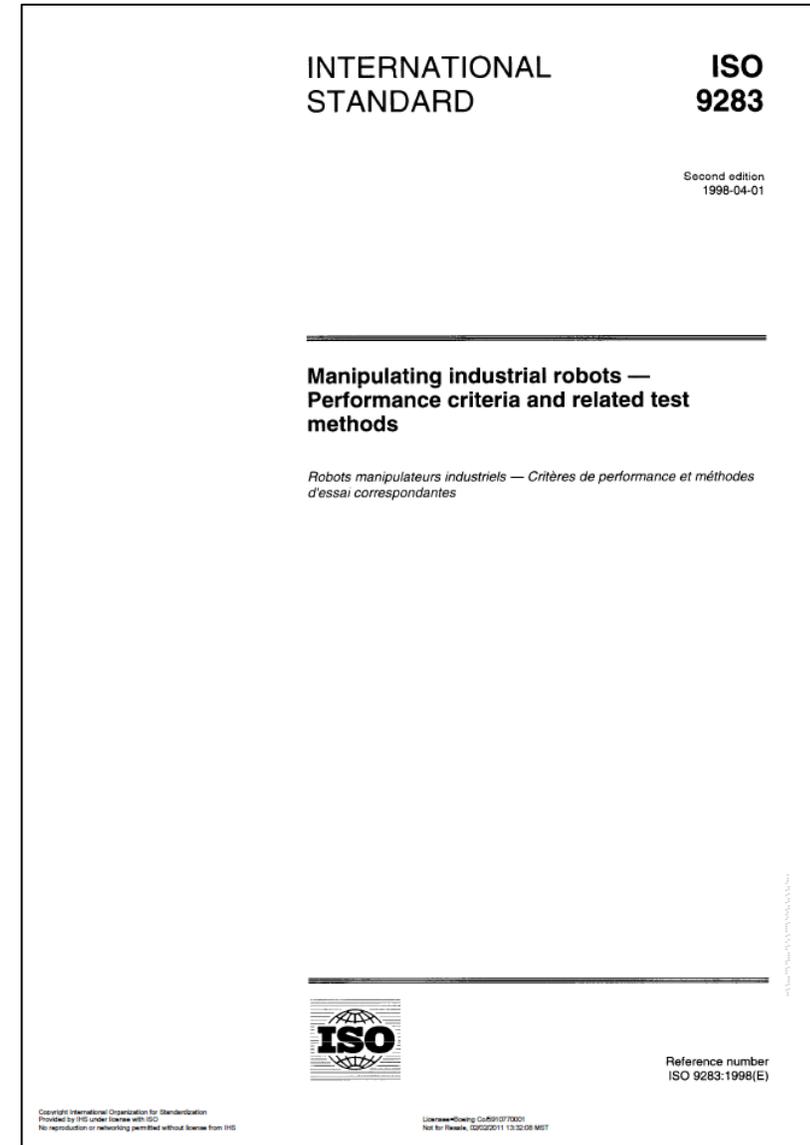
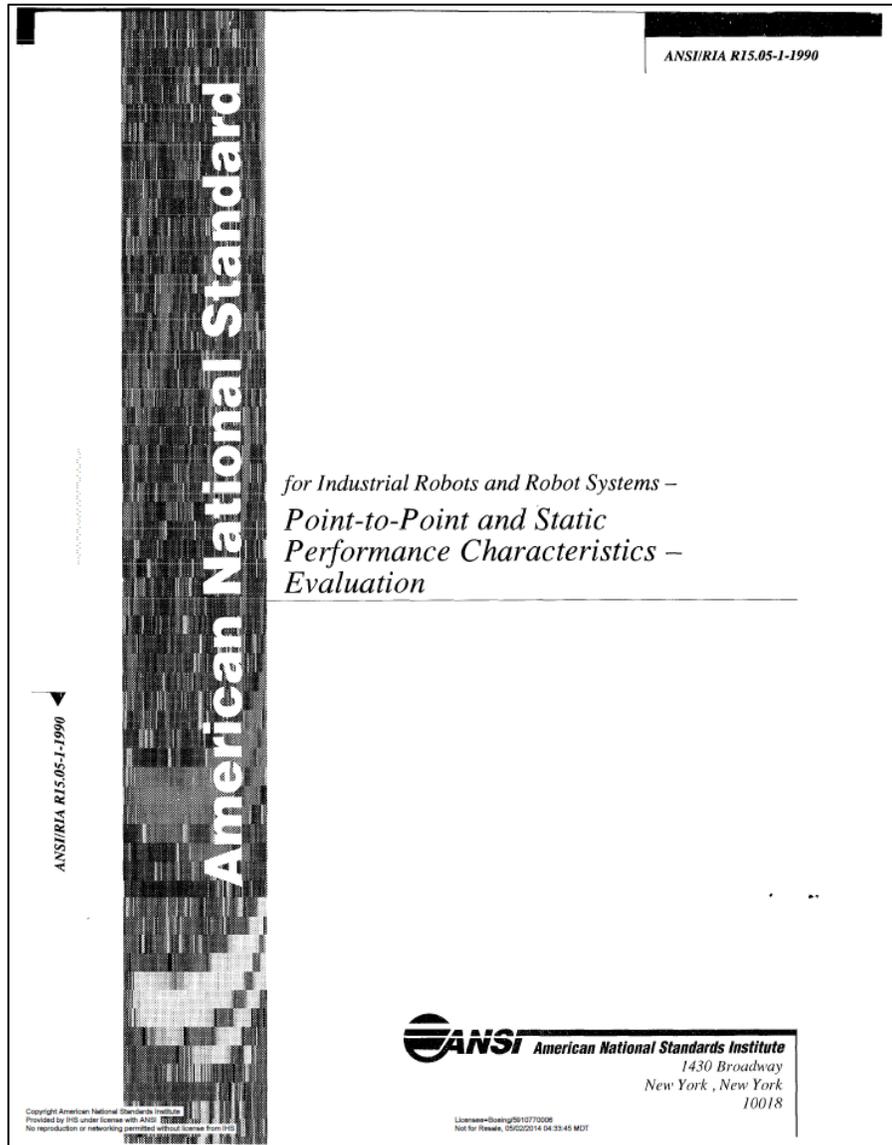
Comparable – But not really



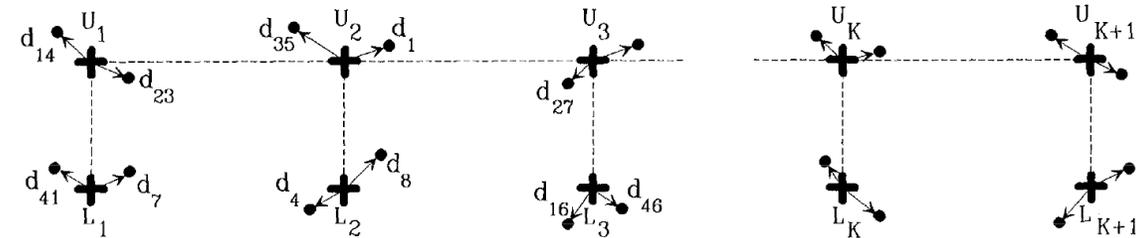
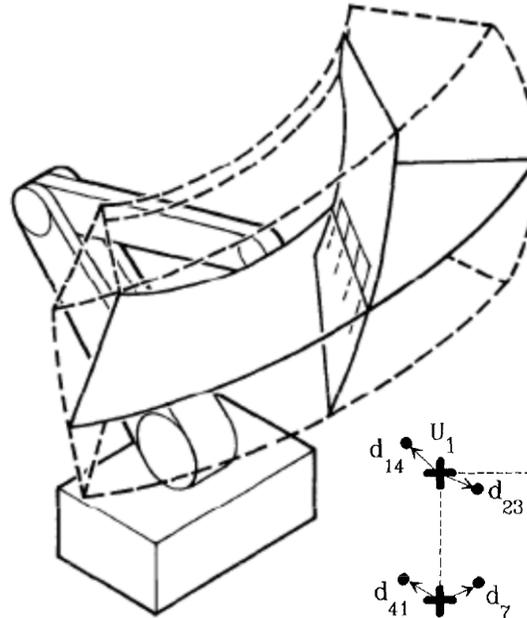
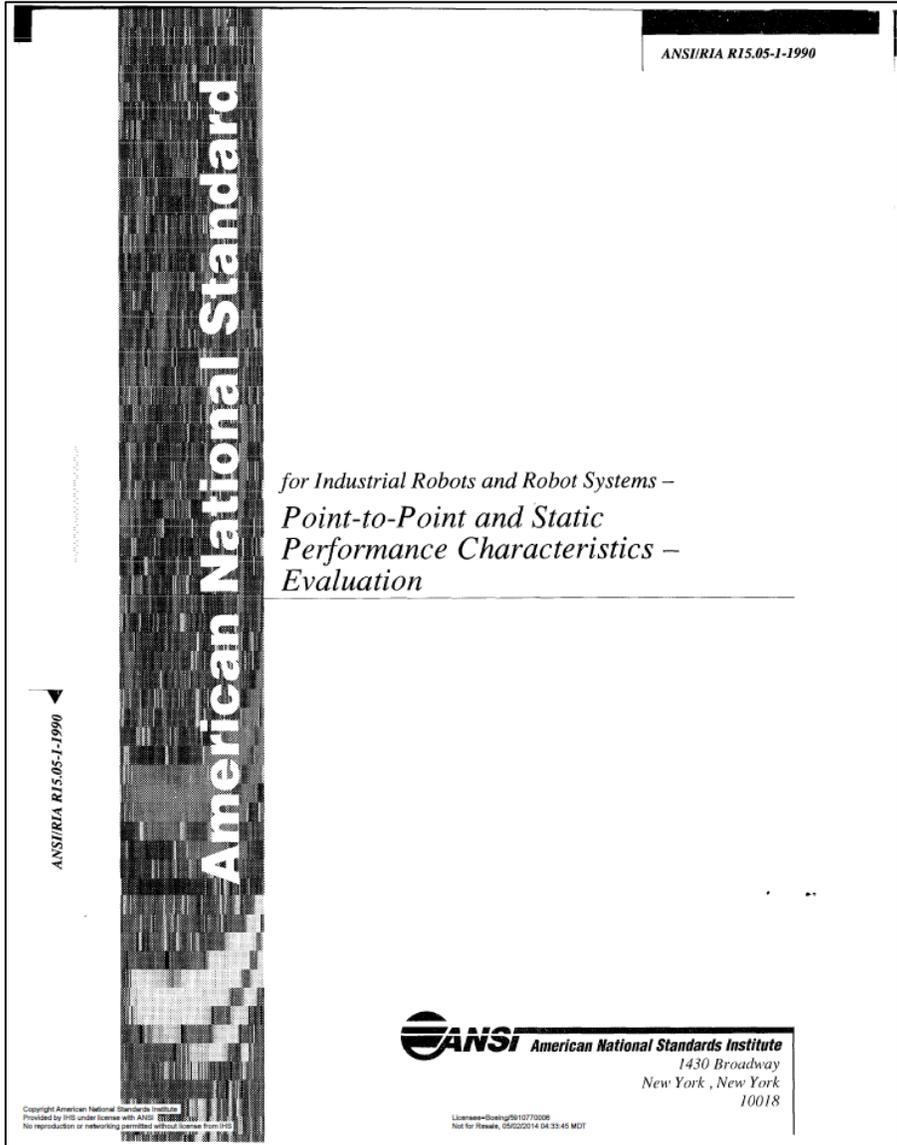
The golden age of robot accuracy?



A tale of two standards



ANSI/RIA R15.05-1-1990 (R1999)



- +** VERTICES ALONG STANDARD PATH $(U_1, L_1, U_2, L_2, \dots, U_{K+1}, L_{K+1})$
- ACHIEVED POSITION (X_{ai}, Y_{ai}, Z_{ai})
- d_i DEVIATION ERROR VECTOR AT THE i^{th} MEASUREMENT

“Static position accuracy is a statistical measure of the spatial deviation between commanded and achieved robot positions. ... Two statistics on positional accuracy are reported: mean and standard deviation.” (Sec. 8.2.1.1)

ISO 9283:1998

INTERNATIONAL
STANDARD

ISO
9283

Second edition
1998-04-01

Manipulating industrial robots — Performance criteria and related test methods

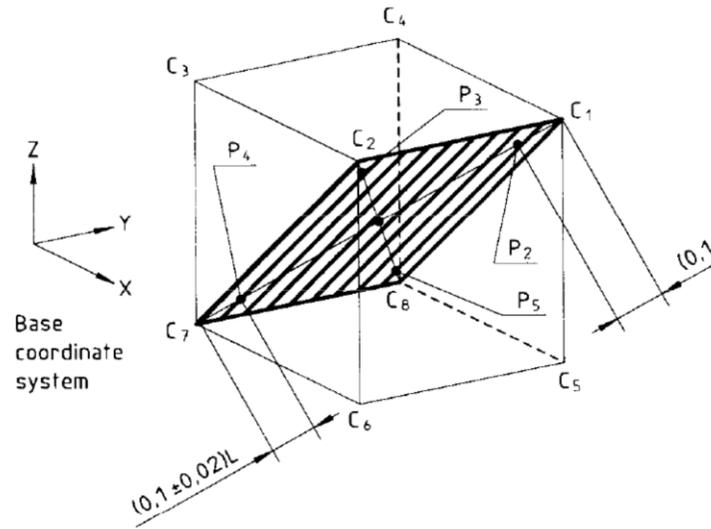
Robots manipulateurs industriels — Critères de performance et méthodes
d'essai correspondantes



Reference number
ISO 9283:1998(E)

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L = Length of diagonal
Example showing plane a) $C_1 - C_2 - C_7 - C_8$ with
poses $P_1 - P_2 - P_3 - P_4 - P_5$

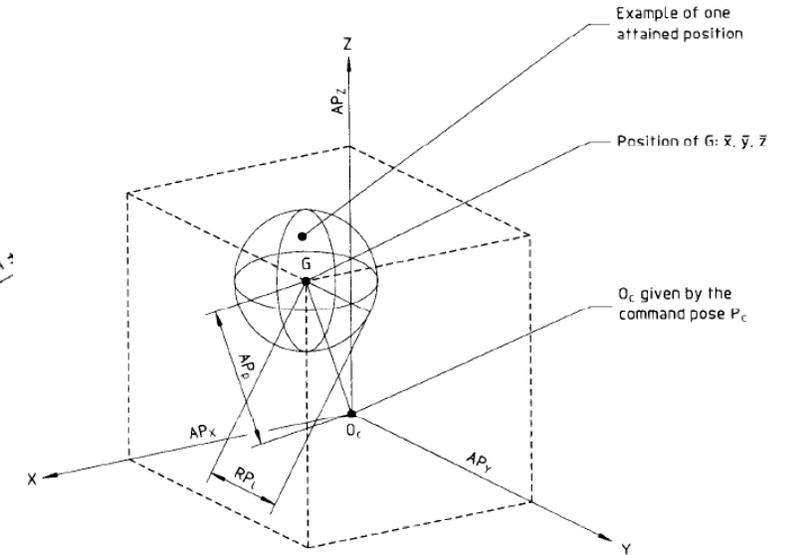
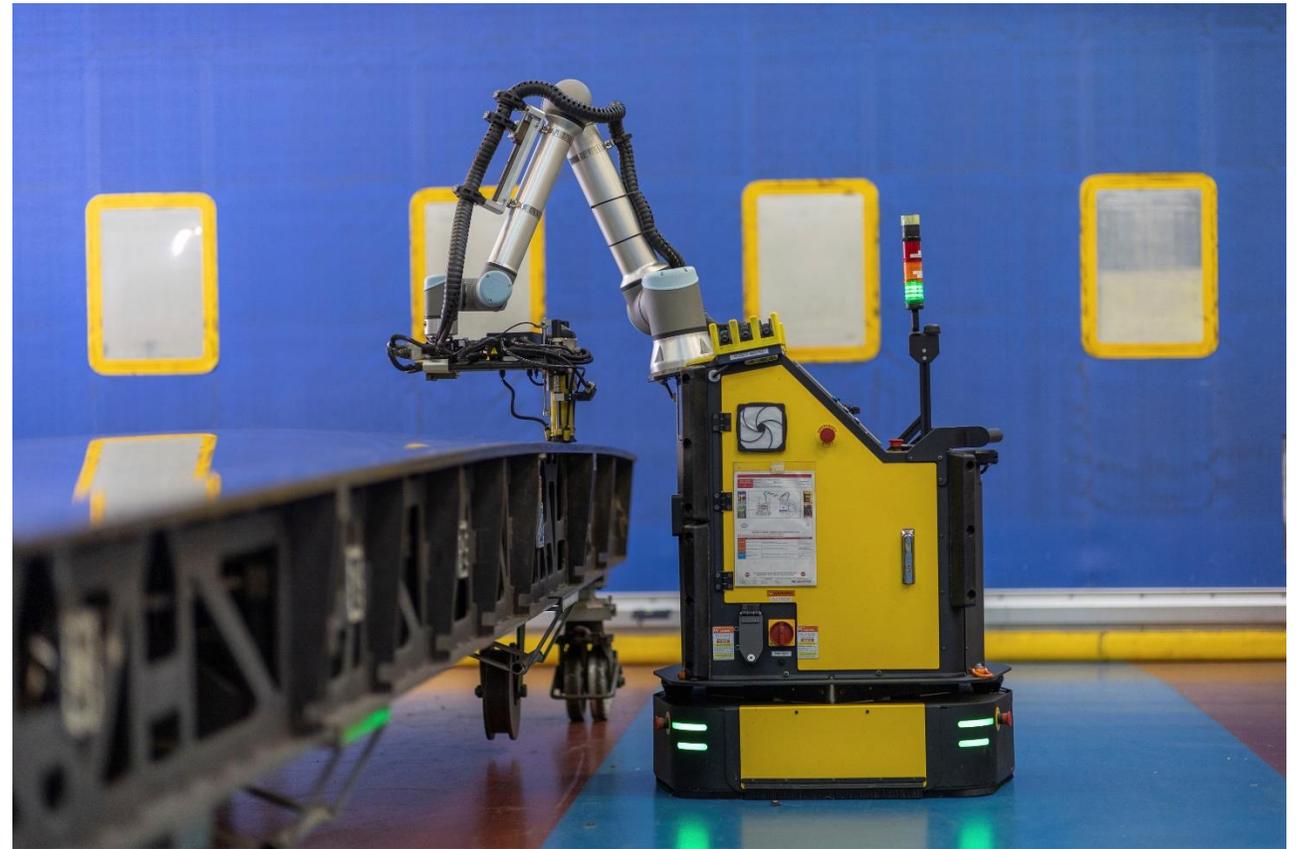


Figure 8 - Positioning accuracy and repeatability

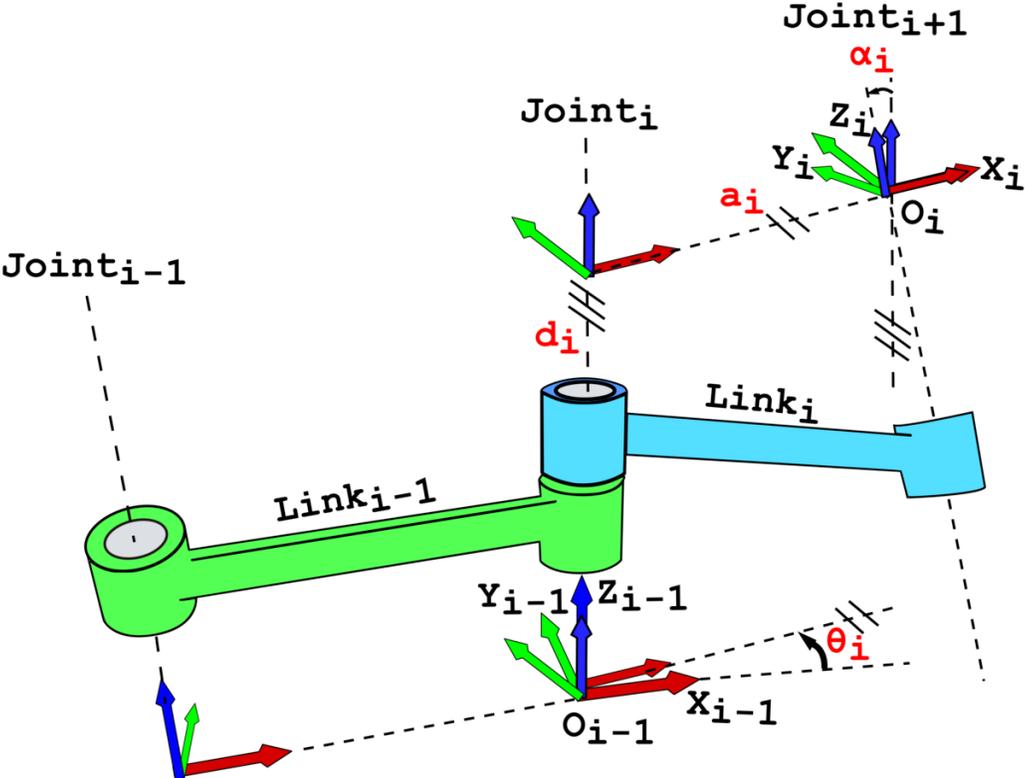
“*positioning accuracy*: the difference between the position of a **command pose** and the **barycentre** of the attained positions.” (Sec 7.2.1 – bolded emphasis mine)

“The **commanded poses** for teach programmed robots are to be defined as the measurement point on the robot. ... The coordinates **registered on the measuring system** are then used as “command pose” when calculating accuracy based on the consecutive attained poses.” (Sec 7.1 – bolded emphasis mine)

Then vs. Now



Parametric Calibration



+

Stiffness

High accuracy robots



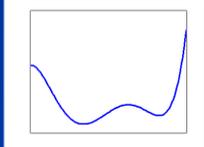
Complete Parametric Models

Axis Error Motion

$$K_{forward} = E_0 A_1 E_1 A_2 E_2 \cdots A_N E_N$$

Nominal Axis Motion

$$\begin{bmatrix} 1 & -\varepsilon_z(q) & \varepsilon_y(q) & \delta_x(q) \\ \varepsilon_z(q) & 1 & -\varepsilon_x(q) & \delta_y(q) \\ -\varepsilon_y(q) & \varepsilon_x(q) & 1 & \delta_z(q) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Gantry (XYZCA)

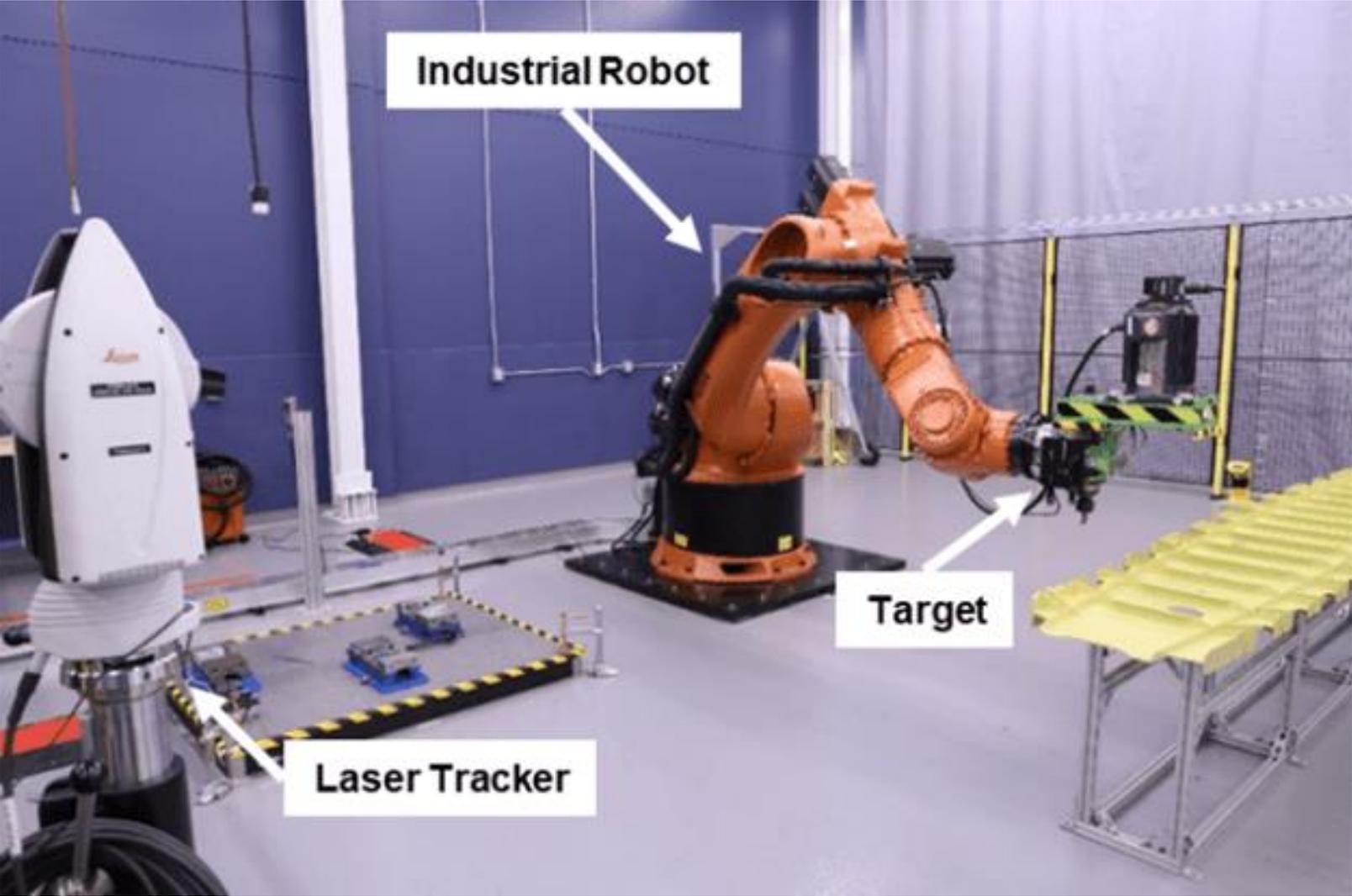


	Accuracy (in)	
	Median	Max
Before	0.015	0.029
After	0.003	0.005

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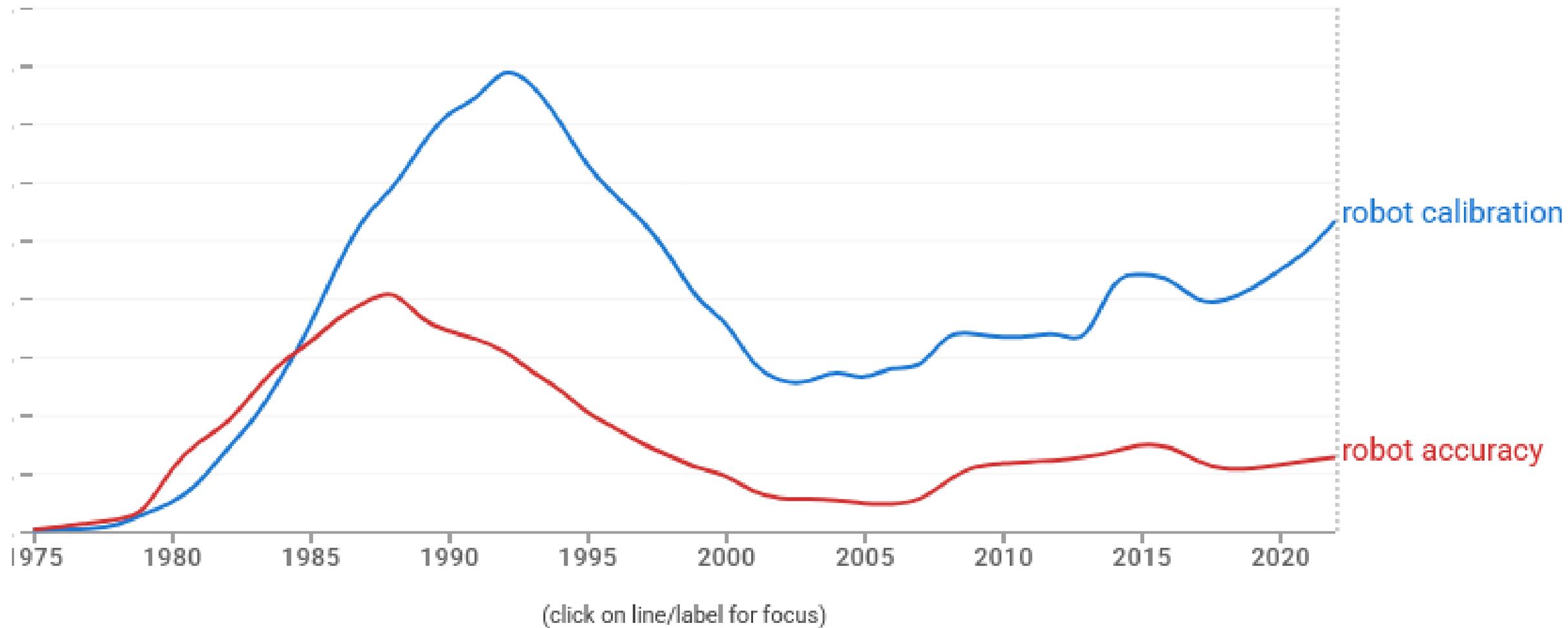
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Dynamic control



Where should we go?

- A better definition of accuracy
- A better way to report accuracy
 - Accuracy compared to omni-directional repeatability
 - Accuracy compared to “distance”
- Non-parametric calibration
 - Error similarity measures
 - ML approaches
 - Something new?
- Accuracy for sensor driven robots
- Accuracy for program-free robots
- Registration/Alignment/Mapping



(click on line/label for focus)

Parting thoughts

- Stop reporting “percent improvement”.
- Why do we seem to be stuck at 1 mm for COTS robots?
- Focus on the configuration space, not the task space.



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