

# SI Traceable Diffraction Measurements on the NIST Parallel Beam Diffractometer

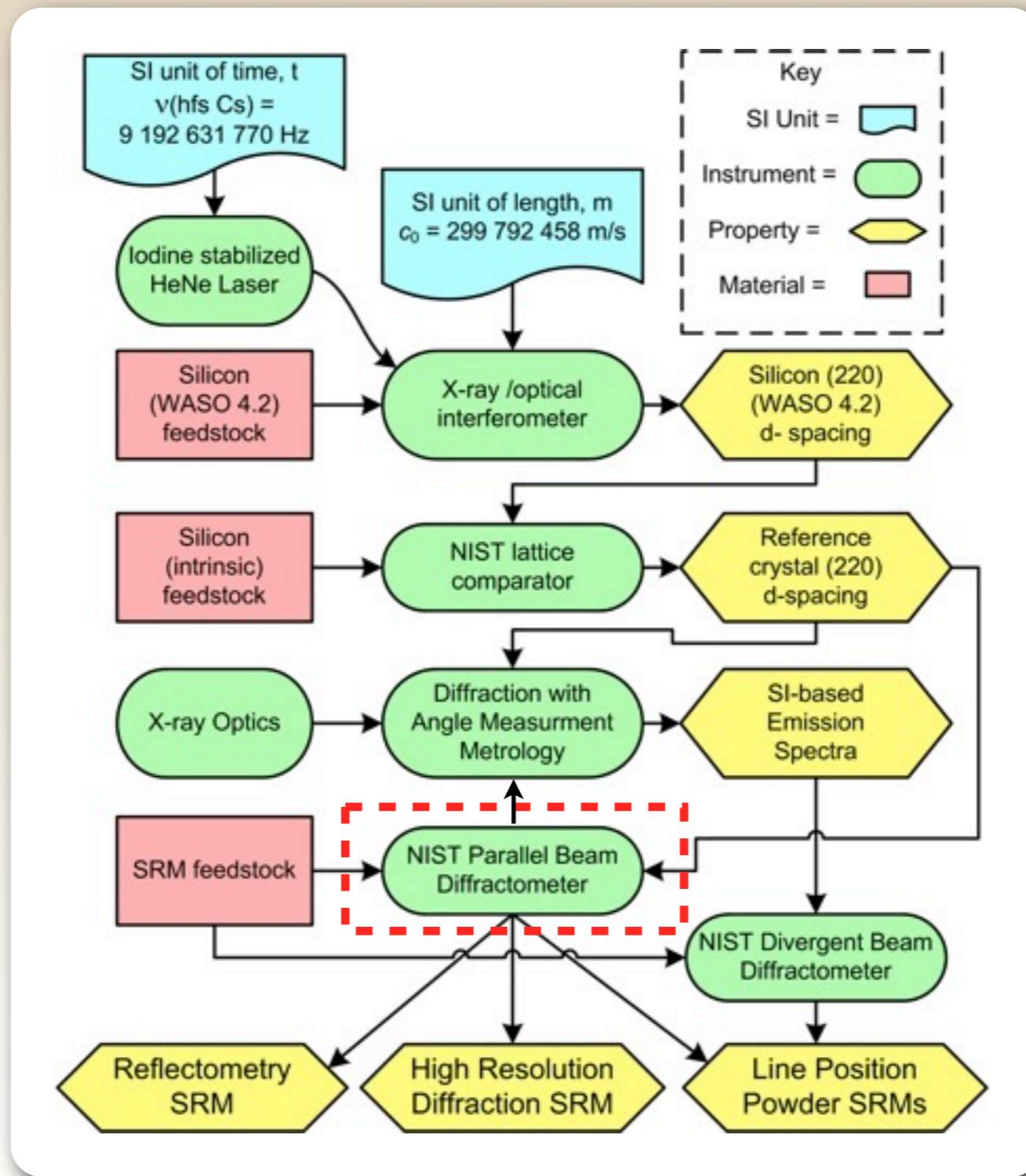
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# Making XRD Traceable

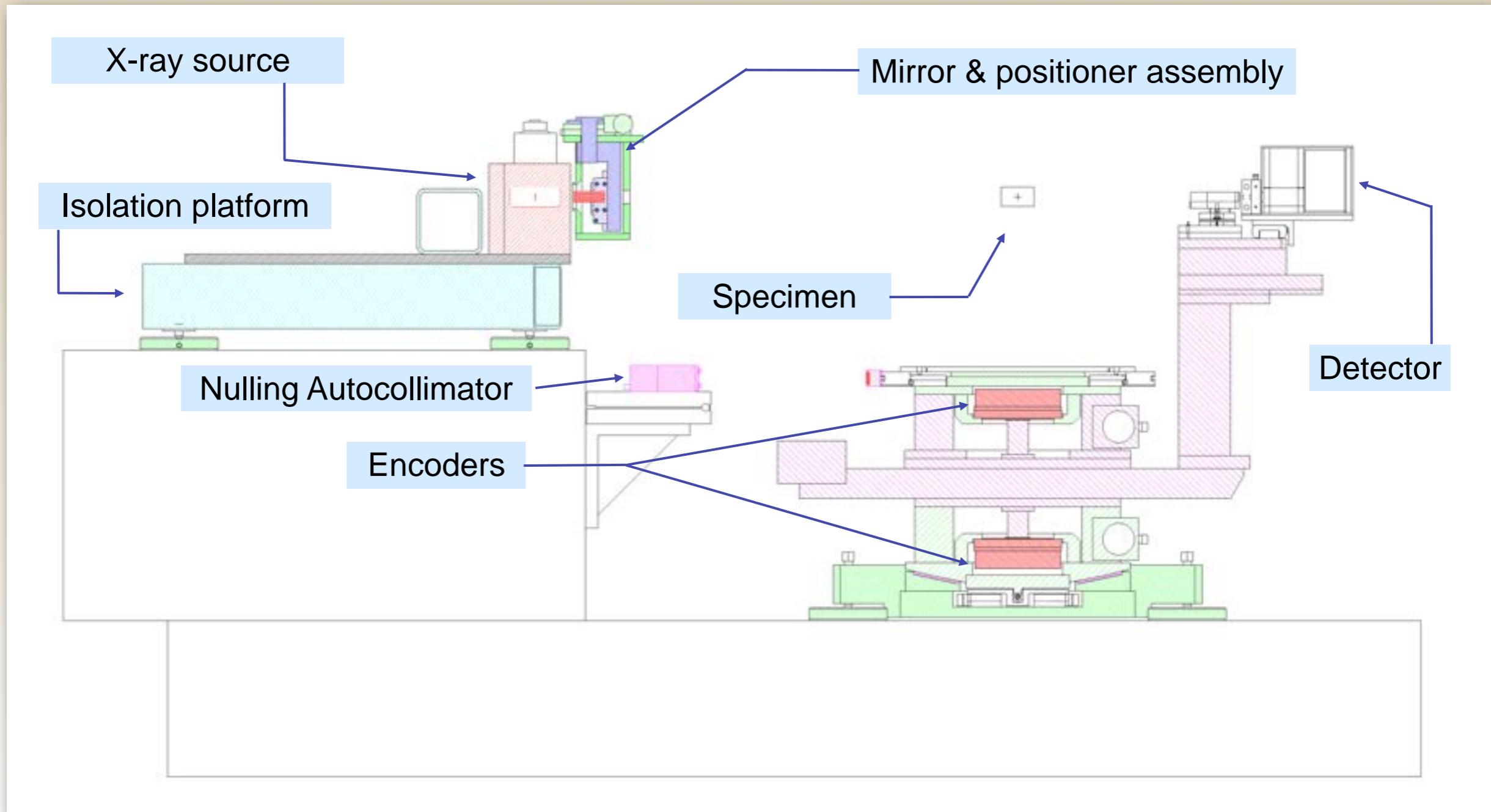


# Parallel Beam Diffractometer Overview

- Interchangeable optics and sample stages
- Vertical axes, concentrically mounted Huber 430 rotation stages
- Heidenhain RON 905 optical encoders on primary axes
- Short and long range encoder calibration
- SI-traceable reference crystals



# PBD Schematic

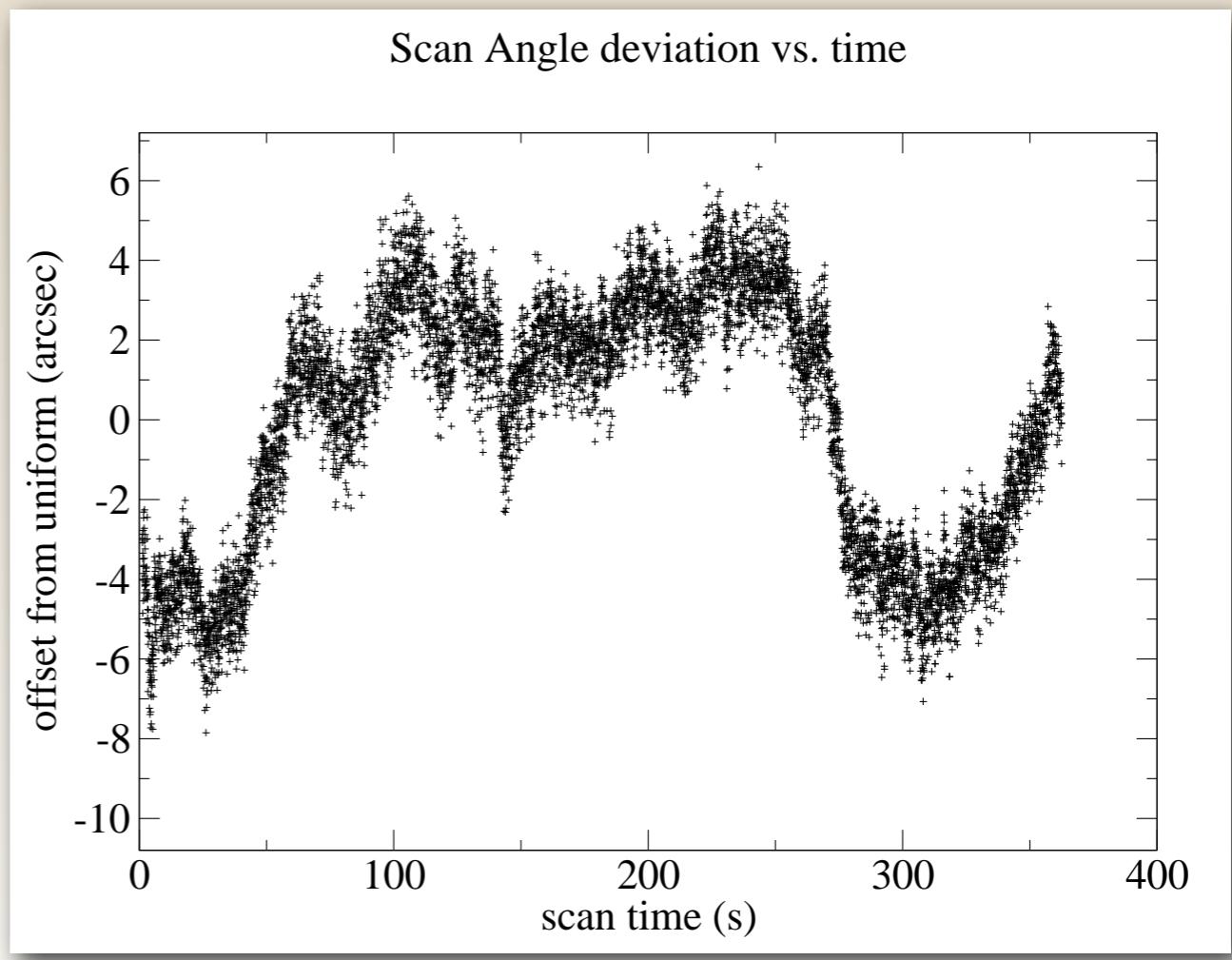


# Angular Measurements

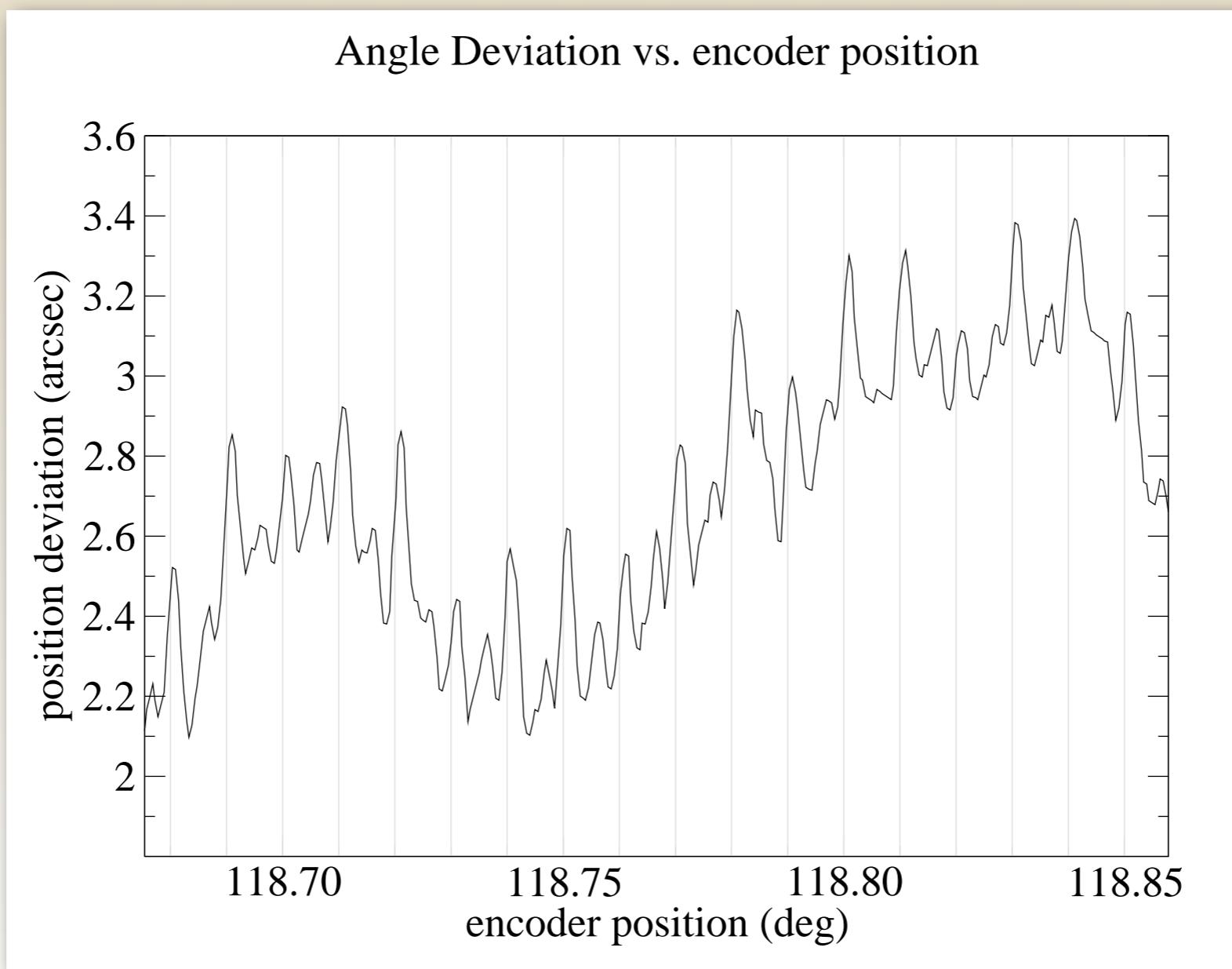
- Divide angular domain into two problems:
  - Short-range errors (coherent with encoder features at  $100 \text{ deg}^{-1}$ ) caused by nonlinearities in the digitizing electronics
  - Long-range errors caused by scale errors in the encoder wheel, eccentricity, etc.
- Avoid use of undocumented internal angular corrections from manufacturer

# Short-Period Compensation

- Scan a diffractometer axis at (roughly) uniform speed
- monitor encoder results as a function of time
- transform to deviations from linear as a function of angle
- these deviations include screw errors, motor speed variations, all kinds of noise

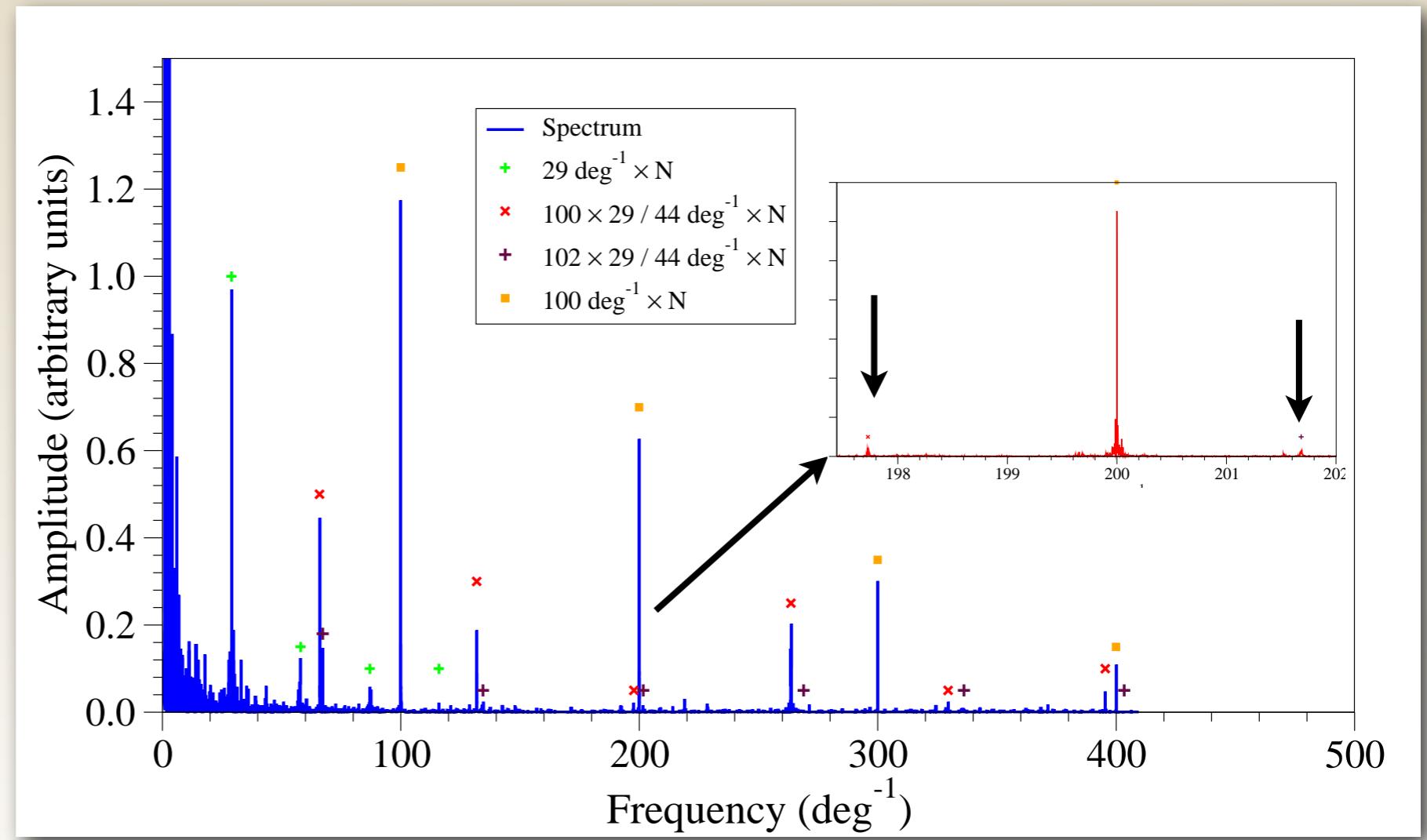


# Deviations have Periodic Structure



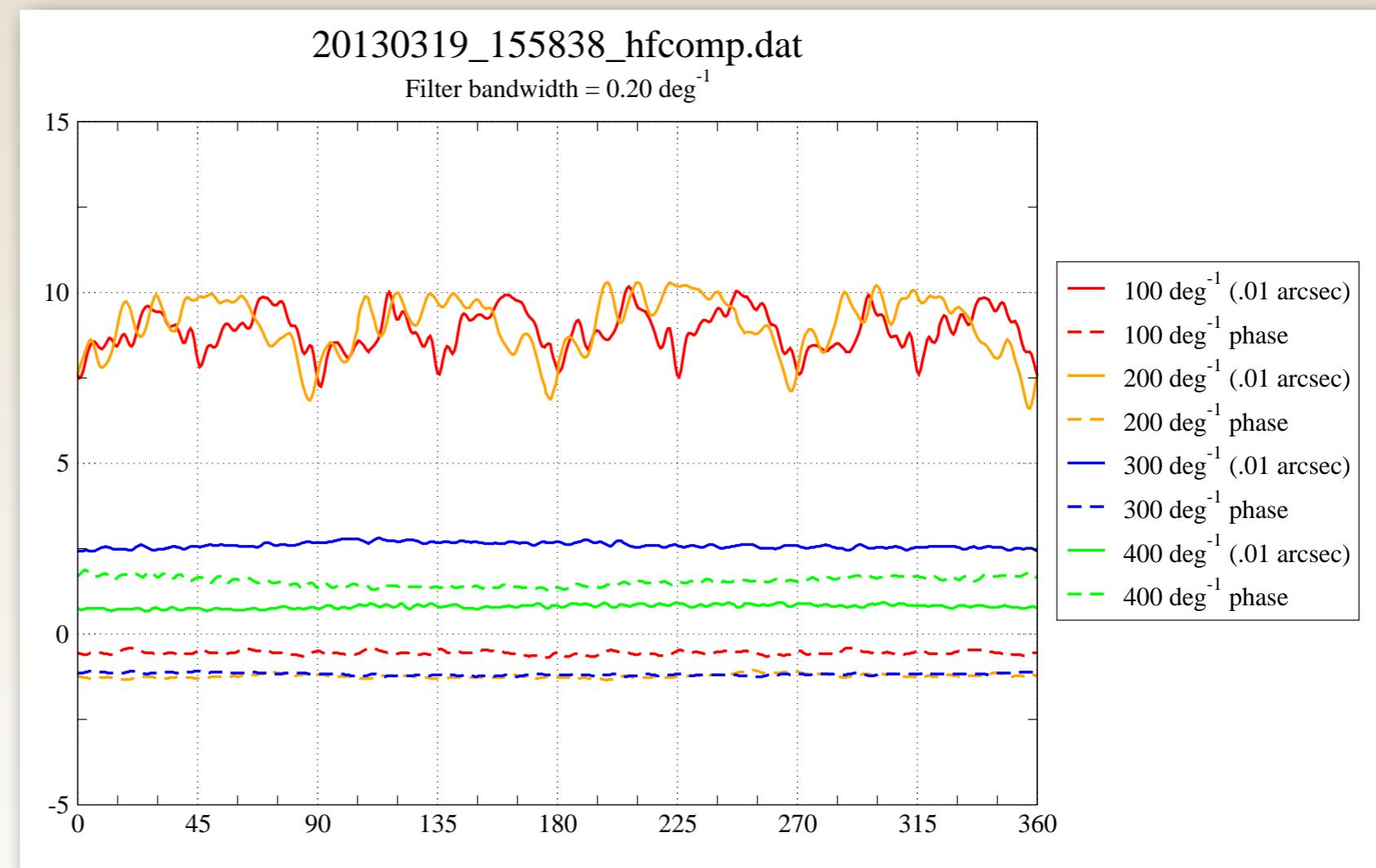
# Example Fourier Spectrum

- Strong peaks at multiples of 100/deg
- Also at motor and gearing frequencies!
- Inset shows how a near collision of gearing and real peak is very well resolved



# Extracted Short-period Correction

- Analyze as harmonic series of encoder feature period at 100 features/deg
- Demodulated from 100/deg signal to show coefficients as a function of angle, not correction as a function of angle



# Circle Closure Calibration

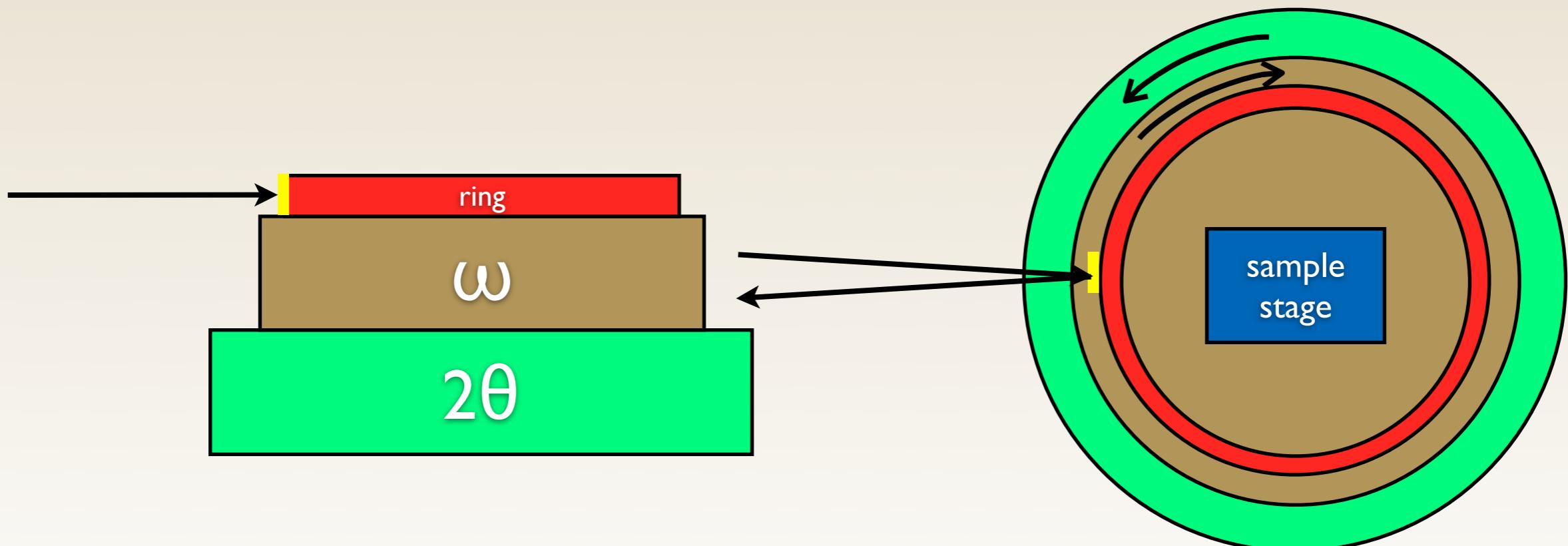
- Concept
  - compare sums of angles, subject to constraints that full circle is  $360^\circ$
- Two general methods
  - use polygonal mirror on single stage to provide set of very stable angle offsets
  - use ‘virtual polygon’ and stacked stages and solve for offsets

# The Virtual Polygon

$$\theta_{\text{mirror}} = 2\theta + \omega + \theta_{\text{ring}} = 0$$

$$2\theta_{\text{meas}} + \Delta 2\theta + \omega_{\text{meas}} + \Delta \omega + \theta_{\text{ring}} = 0$$

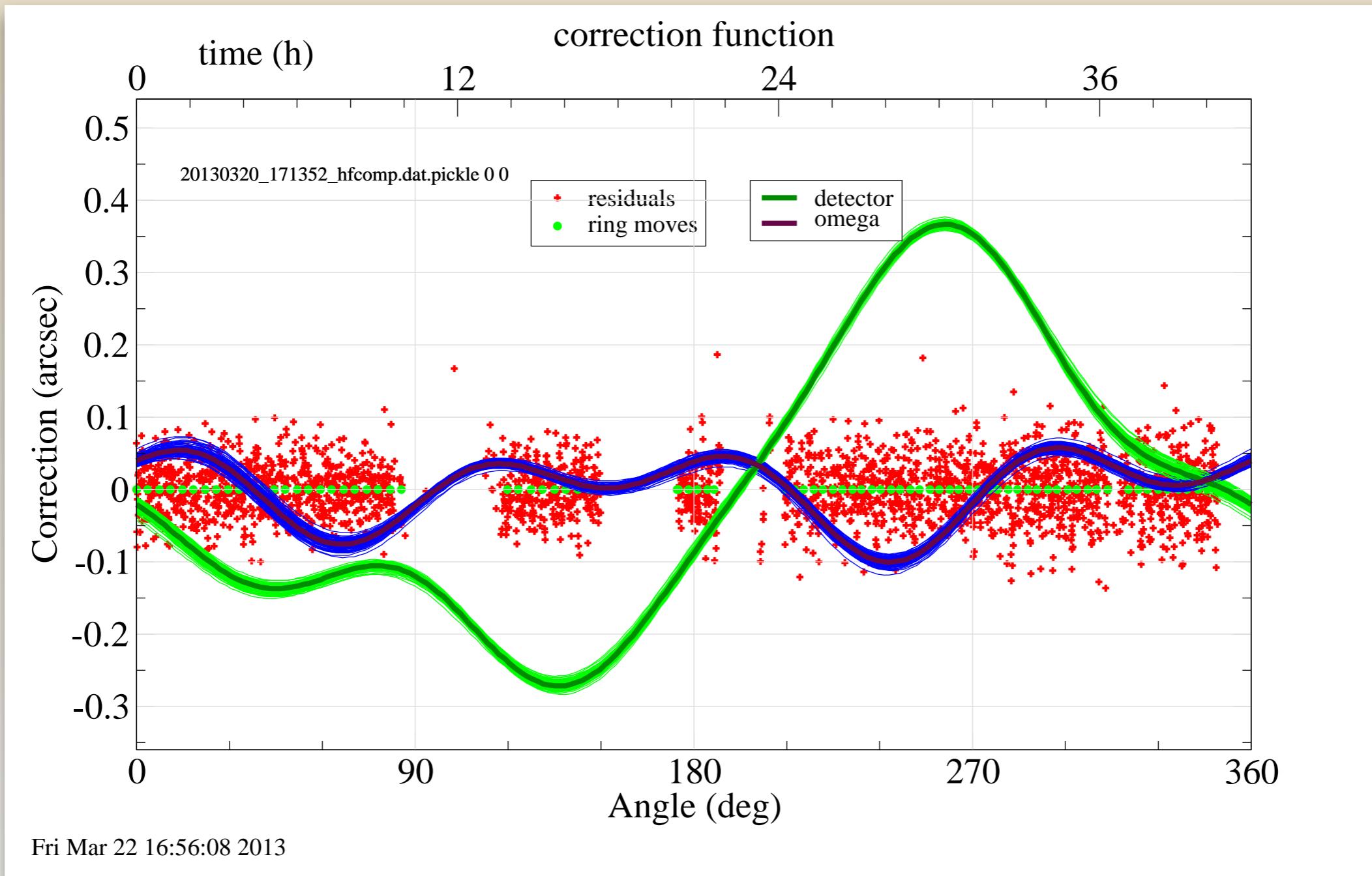
$$2\theta_{\text{meas}} + \omega_{\text{meas}} + \theta_{\text{ring}} = -\Delta 2\theta - \Delta \omega$$



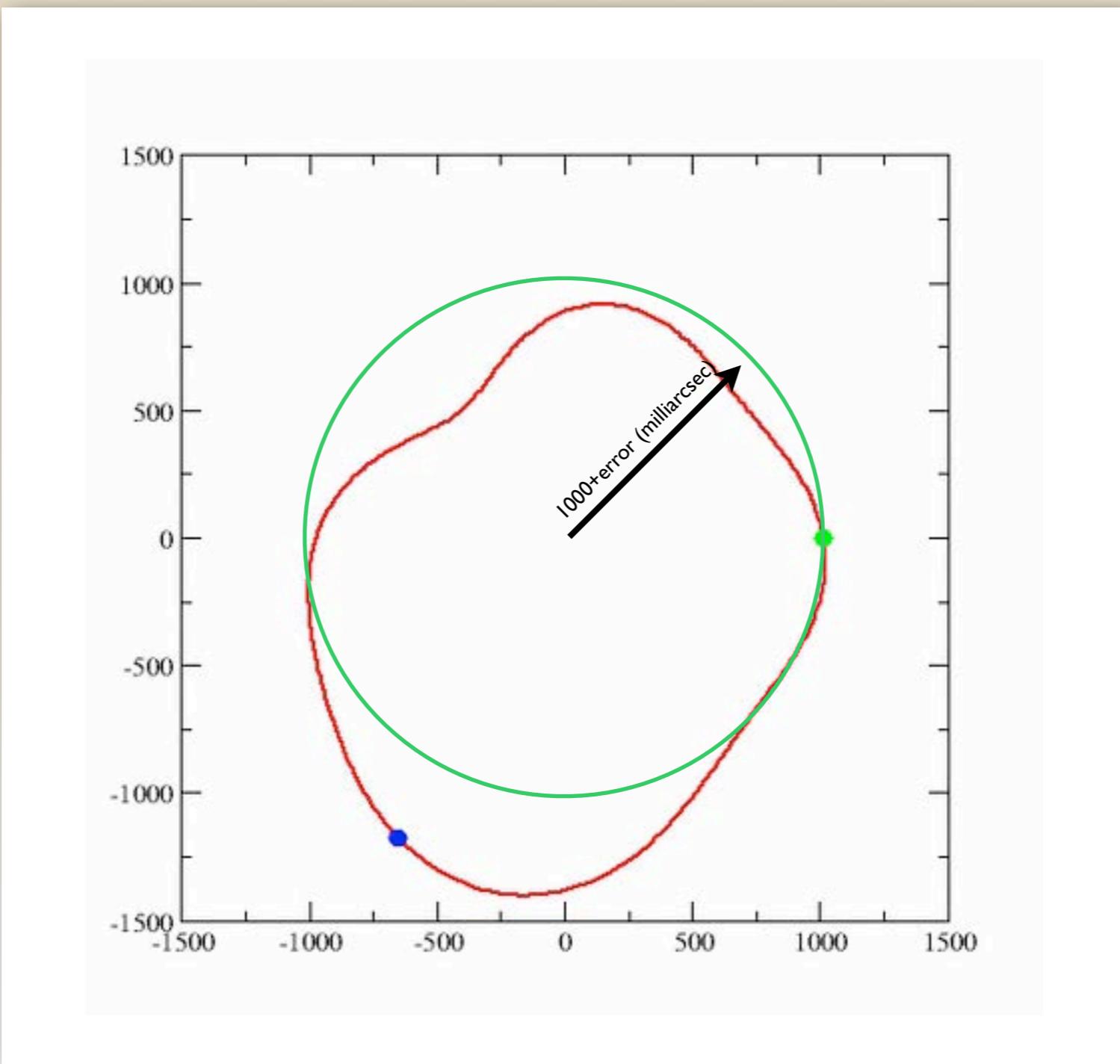
# Details of Virtual Polygon

- For a given ring setting  $\theta_{r,n}$  measure a set of angle errors  $\{\Delta 2\theta_{n,m} (2\theta_m) + \Delta \omega_{n,m} (-2\theta_m - \theta_{r,n})\}$  for (typically) 36 approximately equally spaced  $2\theta$  values and corresponding  $\omega$  values which null the autocollimator ( $n$  indexes ring,  $m$  indexes  $2\theta$ )
- repeat for at least 3 ring settings, to give enough degrees of freedom to solve for  $\Delta 2\theta$ ,  $\Delta \omega$ , and the  $\theta_r$  associated with each group.
- Do least squares fit for parameters

# Circle Closure Results



# Visualization of Error Sum



- $\omega=0$
- $2\theta=0$

# Spectrum Measurement (the *future...*)

- Next Step: measure spectrum through our optics, with fully traceable steps
- use ‘beam walking’ technique in combination with Dectris detector array to map out properties
- requires traceable lattice constants on diffractive optics. These optics are already fabricated.

# Beam Walking Experiment

- Measure angular geometry of beam in non-dispersive configuration (top)
- Measure spectrum of beam in dispersive configuration (bottom)
- Depends on fully qualified angle metrology from compensation and circle closure
- Fast, using Dectris Pilatus 2-D detector array

