



# Discrete Tomography in Materials Science

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(presenting joint work with Sara Bals)

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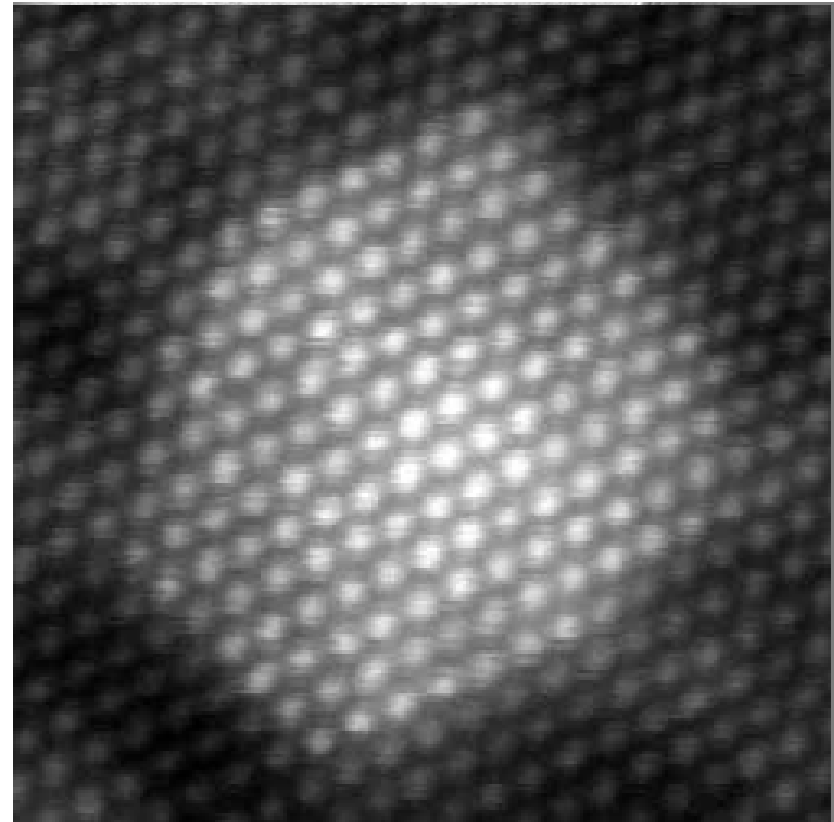


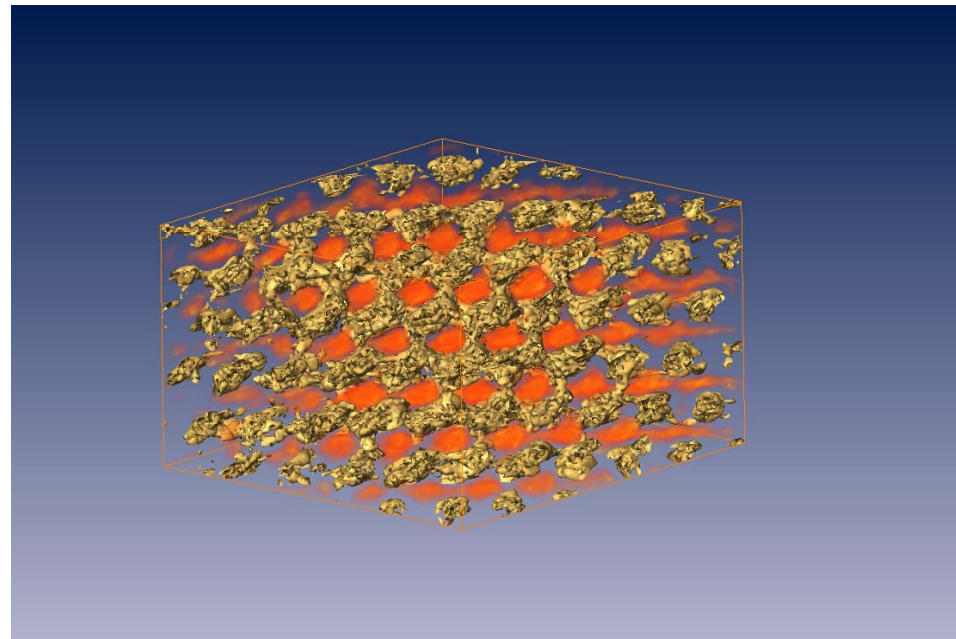
# Overview

- **Introduction to tomography**
- **Electron tomography**
- **Discrete electron tomography**
- **Outlook**

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# Electron microscopy

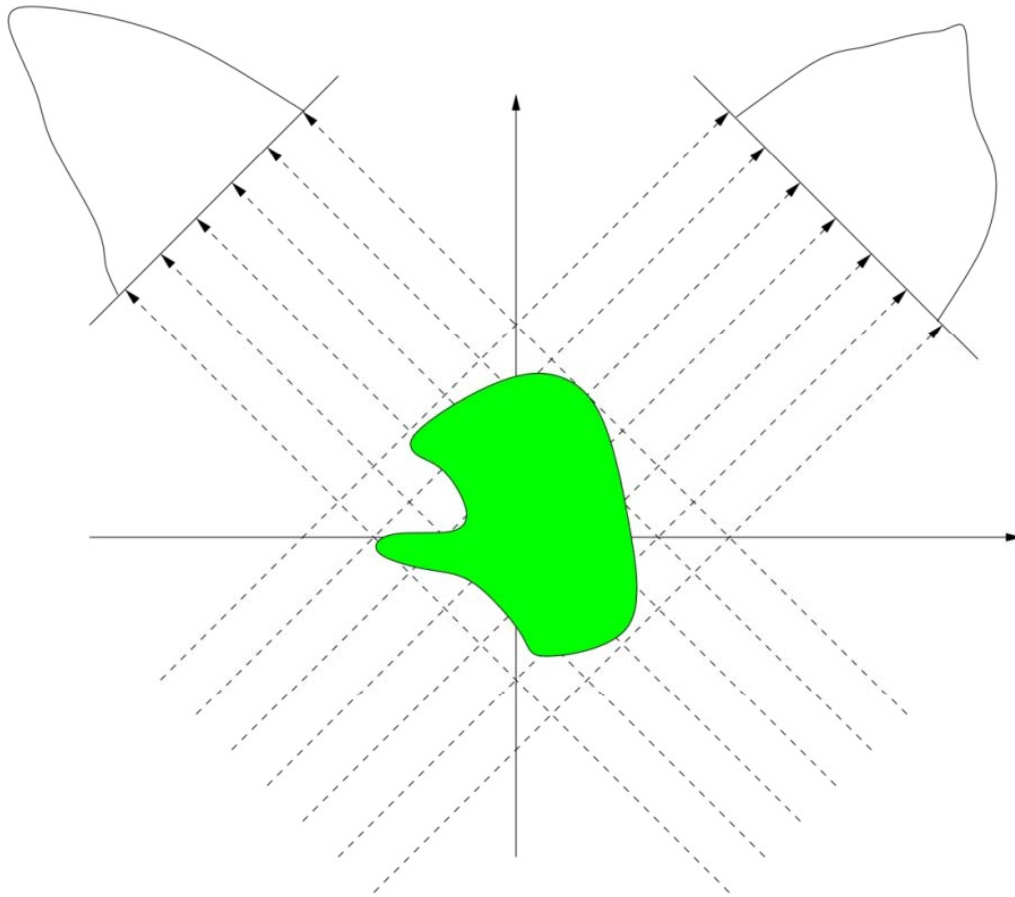




Sara Bals, K. Joost Batenburg, Duoduo Liang, Oleg Lebedev, Gustaaf Van Tendeloo, Alexander Aerts, Johan A. Martens, and Christine E. A. Kirschhock, *J. Am. Chem. Soc.*, 131(13), 4769, 2009

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# Tomography: principle



$$N_d = N_{in} e^{-\int_{\text{ray}} f(x,y) ds}$$

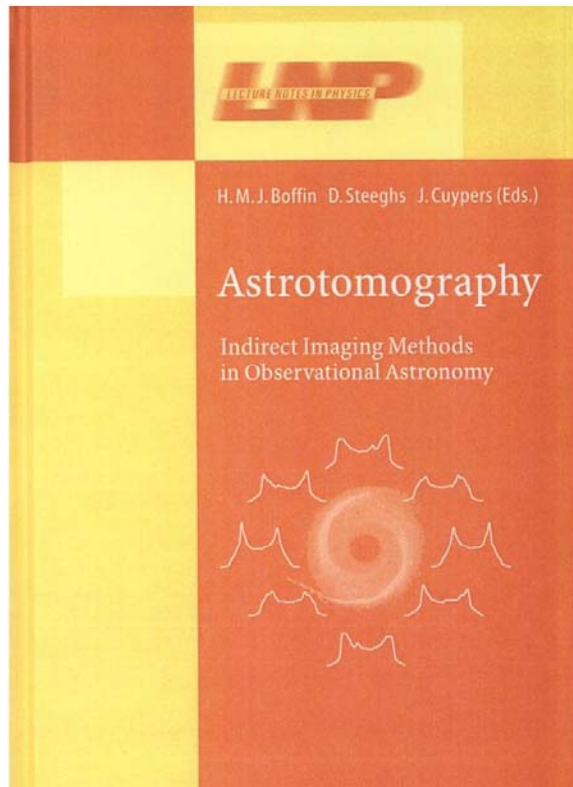
$$\int_{\text{ray}} f(x,y) ds = \log \frac{N_{in}}{N_d}$$

# Tomography at all scales

- Medical tomography (CT) is by far the most common subfield of tomography research
- Tomography is also being used outside of CT, at all imaginable scales, from light years down to sub-nm
- Electron tomography covers the smallest of these scales

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# Tomography at all scales: astrotomography

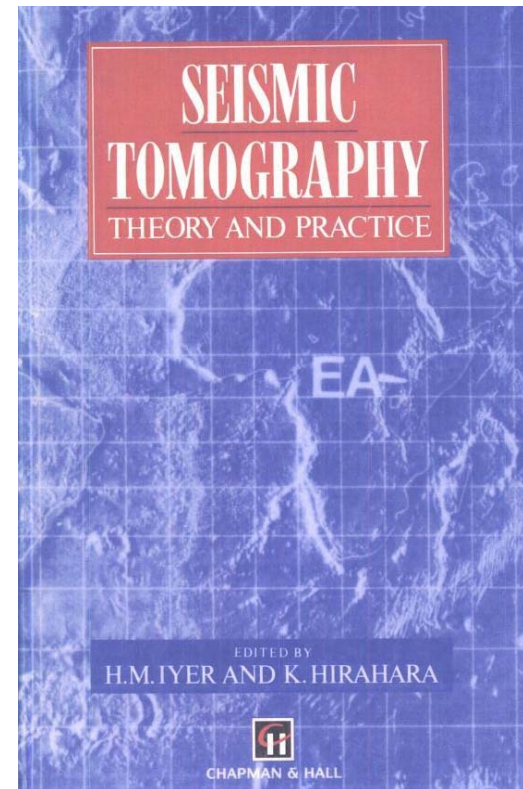
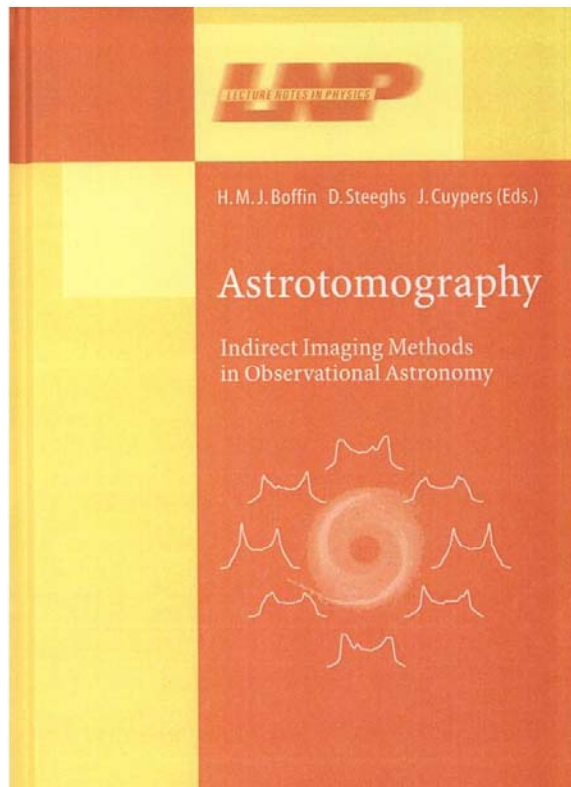


Light year



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# Tomography at all scales: seismic tomography



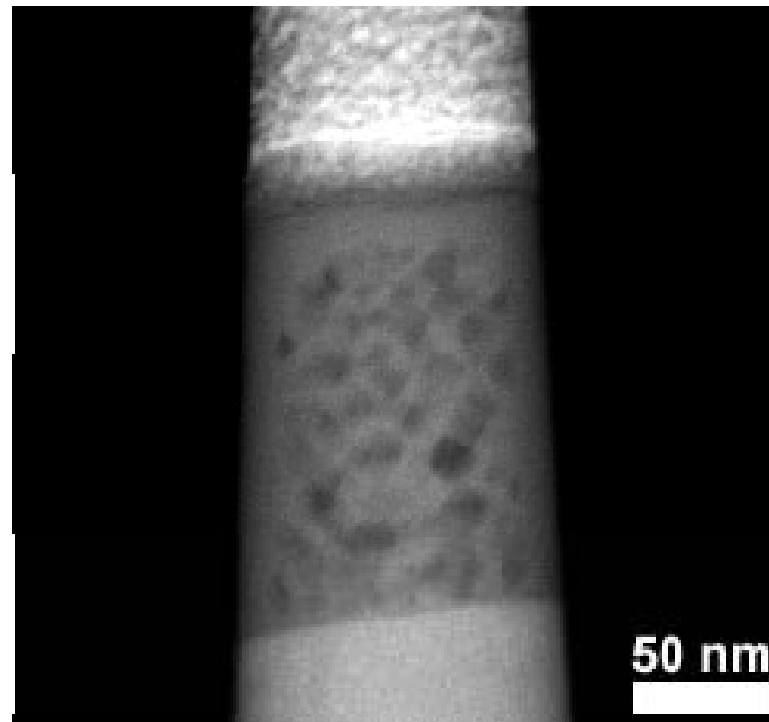
Light year



km



# Tomography at all scales: Electron tomography



STEM image of LZO, Ellen Biermans

Light year



km



mm



$\mu\text{m}$



nm



# Electron tomography: Key limitations

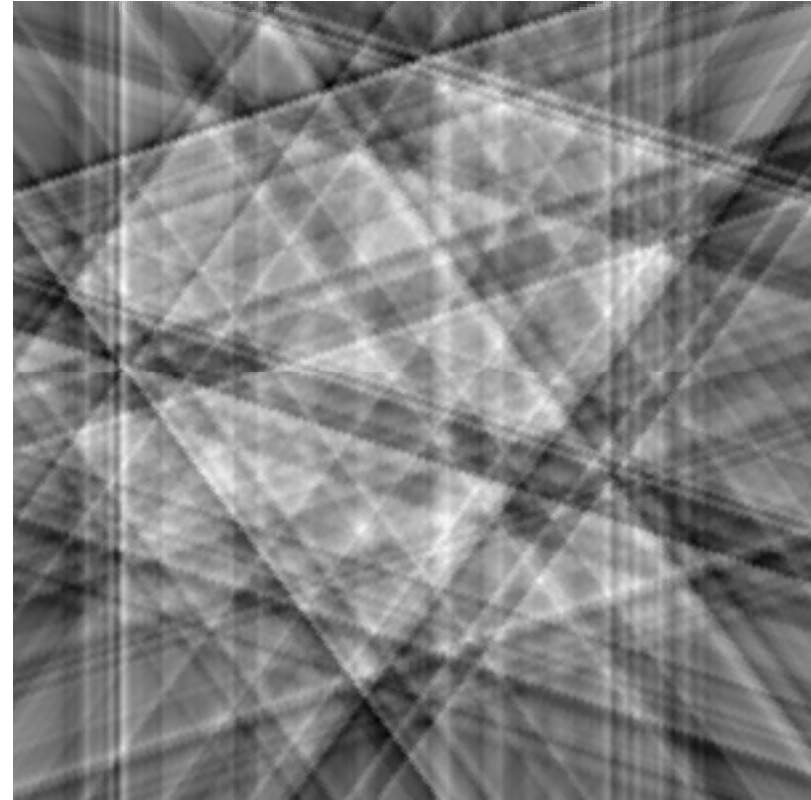
- Tomography requires a large number of projection angles
  - Beam damage
  - Time consuming
- ... sampled at regular intervals
  - Full angular range is needed

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# Few projections



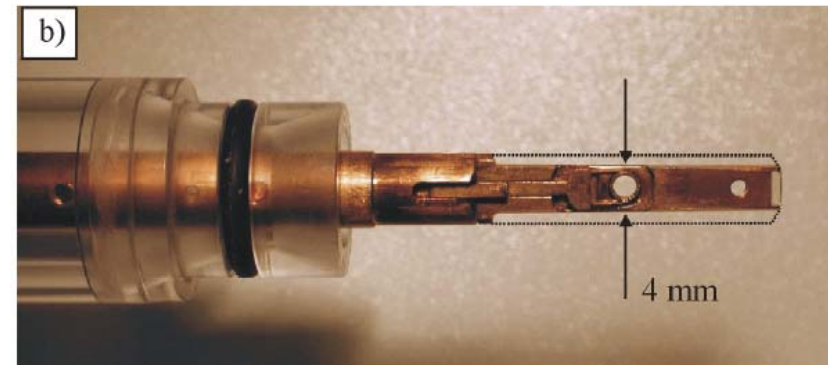
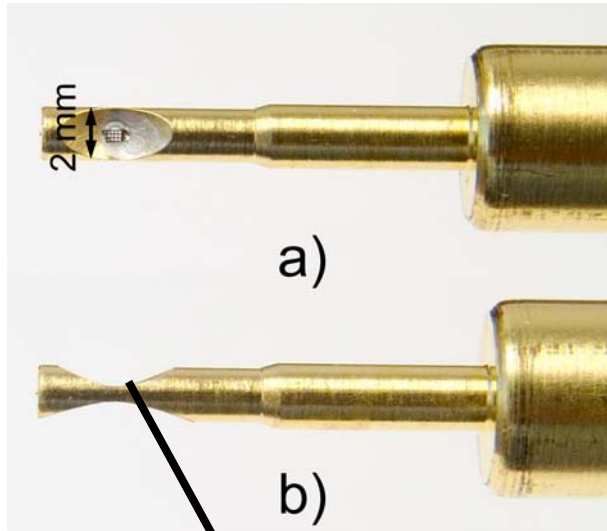
Original image



Filtered backprojection, 5 projections

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# Electron tomography: Tomography holder

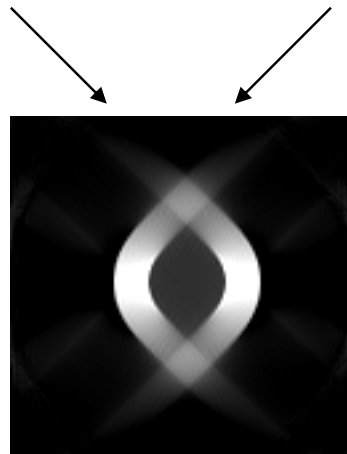
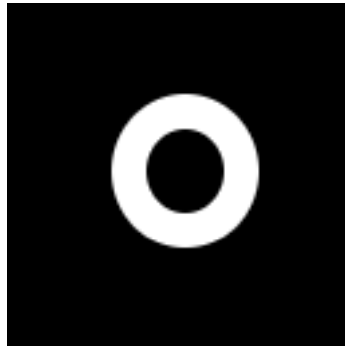


Fischione

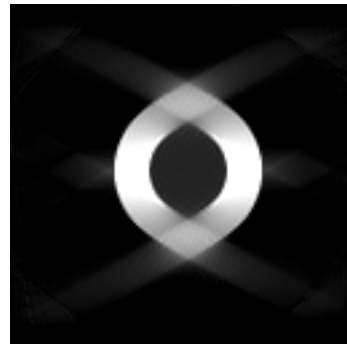
??

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Missing wedge



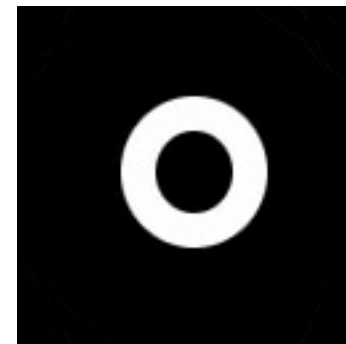
$-45^\circ$  -  $+45^\circ$



$-60^\circ$  -  $+60^\circ$



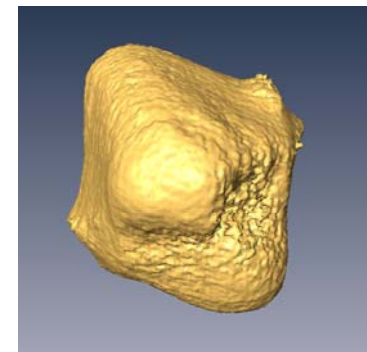
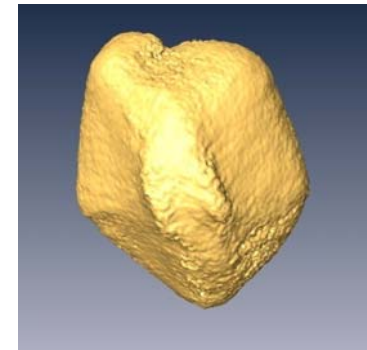
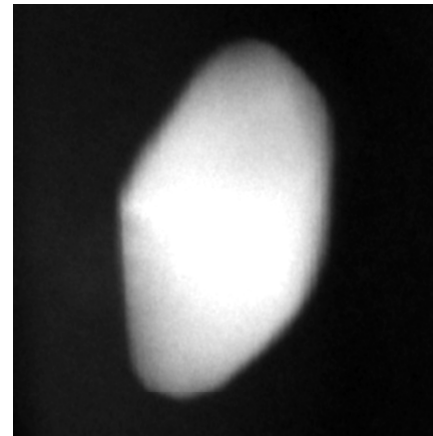
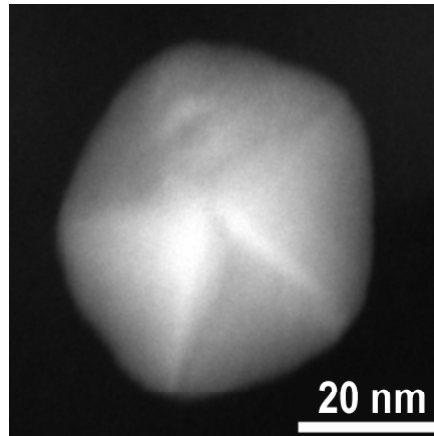
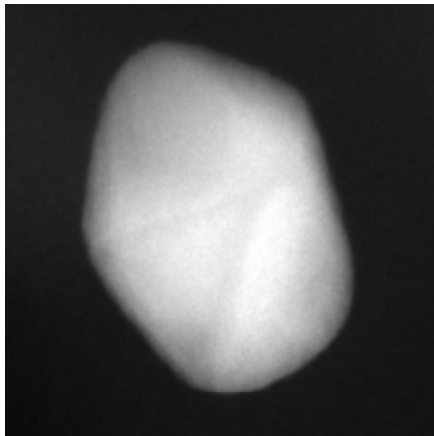
$-75^\circ$  -  $+75^\circ$



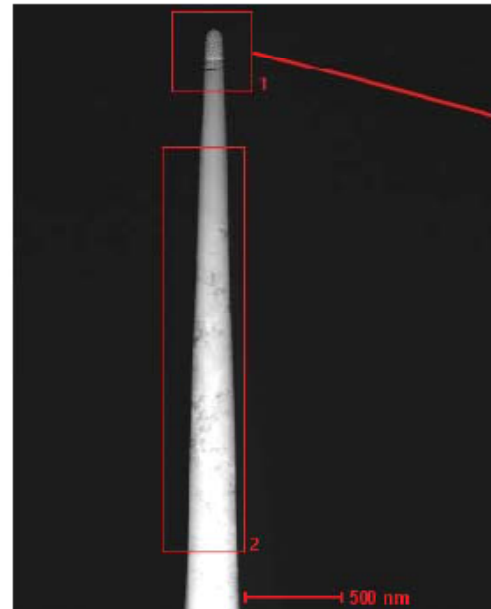
$-90^\circ$  -  $+90^\circ$

# Missing wedge artefacts

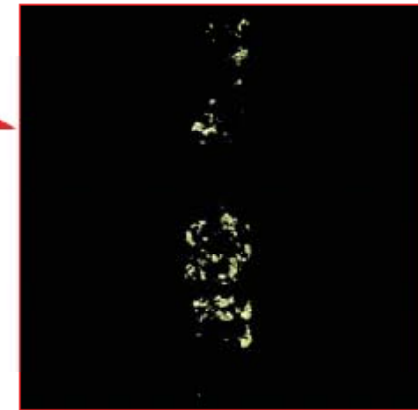
- Insufficient number of projections
- Limited angular range



# Electron Tomography: Tomography holder



HAADF STEM image of a Ni specimen containing alumina particles. The needle-shape was created using an FEI DB 235 DualBeam Instrument equipped with an Omniprobe nanomanipulator for specimen lift-out.



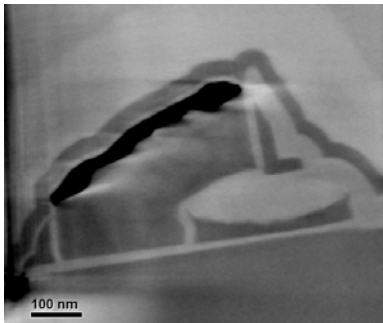
## Reconstruction of alumina particles.

An FEI Tecnai F30 TEM was used to collect 19 x-ray spectral images, 500 x 100 pixels by 1024 channels at a rate of 50msec/pixel. The specimen was rotated on-axis in 10° increments from -90° to +90°. Total data acquisition was approximately one million x-ray spectra taken in the course of 4 days. Analysis was conducted simultaneously with the Sandia multivariate statistical analysis software. In the image, Ni is shown as red and the alumina component is shown after image alignment in green.

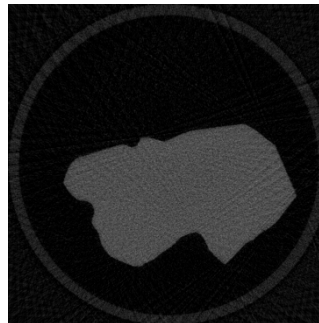


# Discrete tomography

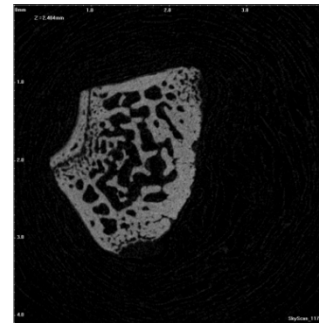
- Fixed set of possible intensities (grey values)
- Materials should be known in advance
- Use prior knowledge about the materials in the reconstruction



*C. Kübel, FEI*



*DiamCAD NV*



*Skyscan NV*

- **DART: Discrete Algebraic Reconstruction Technique**
  - Iterative method
  - Input: projection images + set of intensities
  - Output: segmented image

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DART



Simulation image

13 projections  
-60/+60 degrees



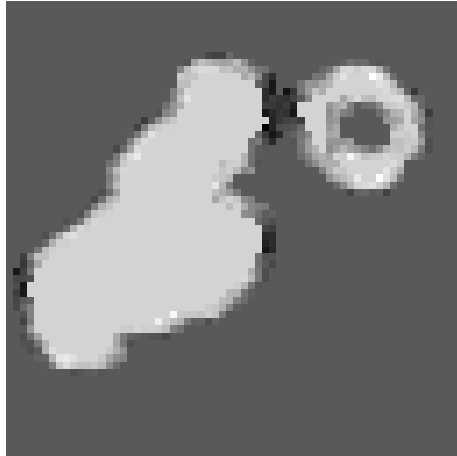
SIRT reconstruction



SIRT reconstruction,  
thresholded

K.J. Batenburg, S. Bals et al.,  
*Ultramicroscopy*, 109(6), 730-740, 2009

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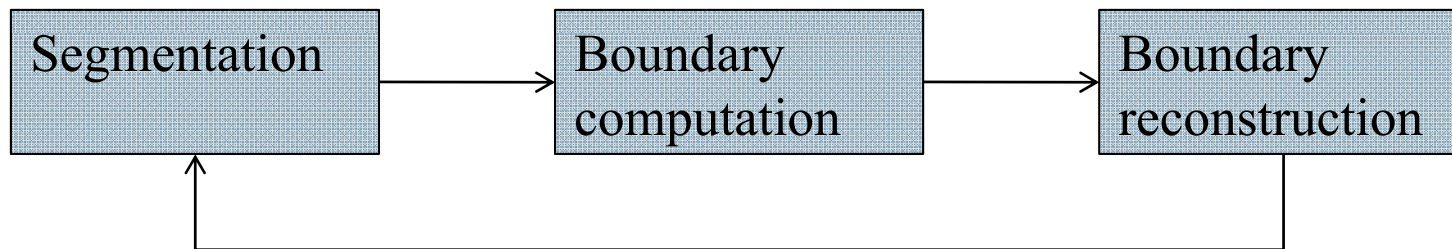
Intermediate reconstruction



Final reconstruction (3 iterations)



Original image



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# DART from few projections



Original image



Discrete tomography, 5 projections

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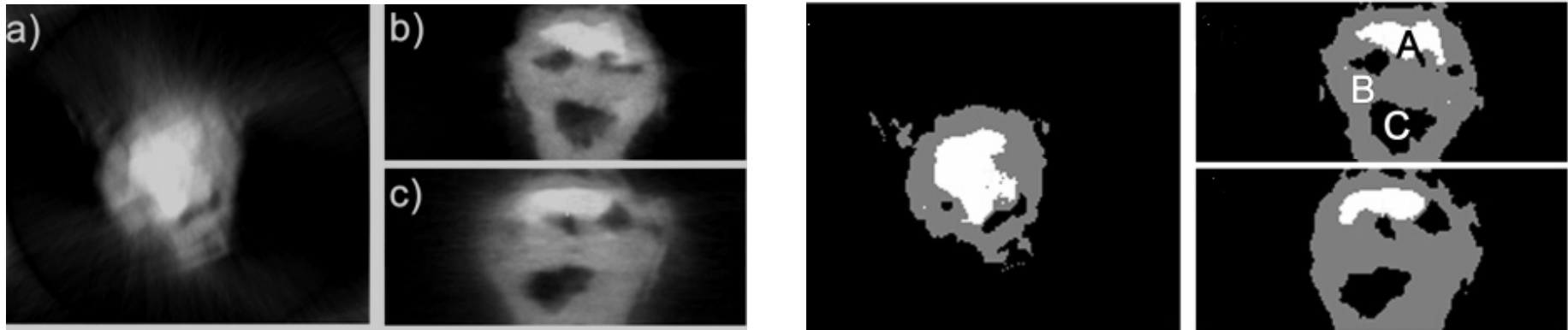
# Example: electron tomography of a nanoparticle

HAADF STEM imaging, FEI Titan microscope



# Example: electron tomography of a nanoparticle

HAADF STEM tomography, FEI Titan



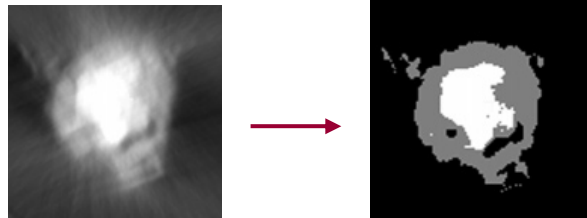
Classical reconstruction,  
using the SIRT algorithm

DART reconstruction

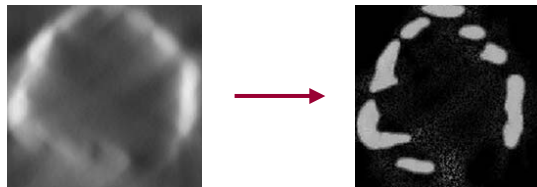
*S. Bals, K.J. Batenburg et al., Nano Letters 7(12), 3669-3674 (2007)*

*K.J. Batenburg, S. Bals et al., Ultramicroscopy 109(6), 730-740 (2009)*

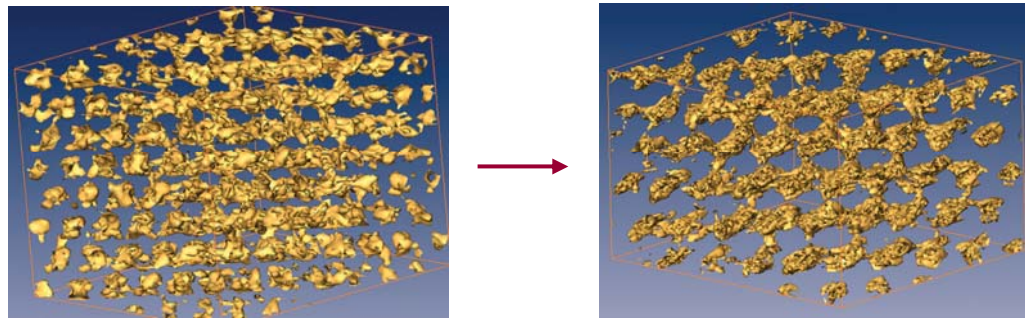




S. Bals, K.J. Batenburg et al.,  
*Nano Letters*,  
7(12), 3669-3674, 2007



S. Turner, S.M.F. Tavernier et al.,  
*J. Nanoparticle Research*,  
12(2), 615-622, 2009



S. Bals, K.J. Batenburg et al.,  
*J. Am. Chem. Soc.*,  
131(13), 4769-4773, 2009

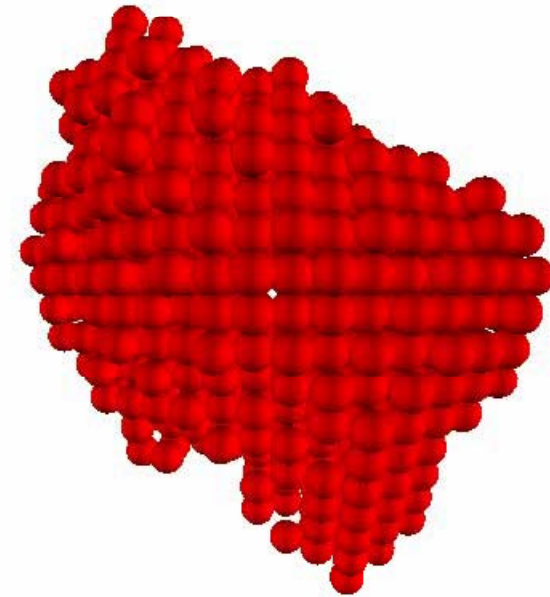
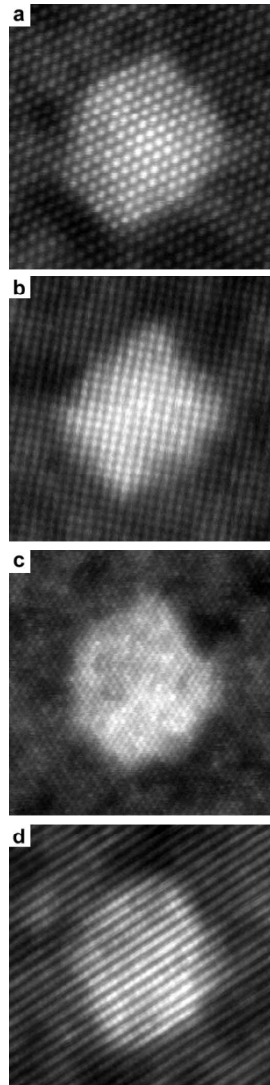
Conventional  
reconstruction

Discrete  
Tomography

- By exploiting prior knowledge, more accurate reconstructions can be computed from *the same* measured data.

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# Tomography at all scales: atomic resolution



S. Van Aert, K.J. Batenburg et al.,  
Three-dimensional atomic imaging of crystalline  
nanoparticles, *Nature* 470, 374-377 (2011).

Light year

km

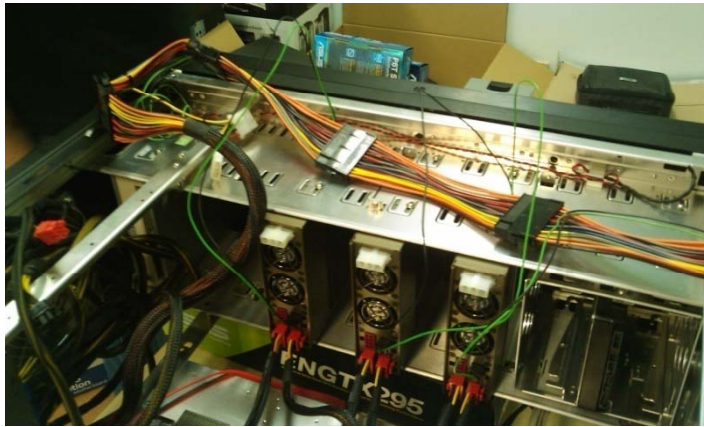
mm

$\mu\text{m}$

nm

sub-Å

# Supercomputing for tomography



- **FASTRA II: 12 TFLOPS supercomputer on your desk**
- **13 NVIDIA GPUs**
- **<http://fastra2.ua.ac.be>**

- **For effective nanometrology, the 3<sup>rd</sup> dimension is crucial**
- **Electron tomography is a versatile tool for 3D nanometrology**
- **New instruments and computational models can overcome traditional limitations**
- **Discrete tomography allows accurate imaging at the nanoscale, up to the atomic level**

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# TY for your attention



## Acknowledgements

- **CWI, Amsterdam**
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- **Fraunhofer, KIT, DiamCAD, Skyscan, NVIDIA, ...**