NIST Calibration Services for Liquid Volume

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Vern E. Bean, Pedro I. Espina, John. D. Wright, John F. Houser, Sherry D. Sheckels, and Aaron N. Johnson November 24, 2009

U. S. Department of Commerce National Institute of Standards and Technology Gaithersburg, Maryland, 20899

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1. Description of Service.

The National Institute of Standards and Technology (NIST) provides calibration services for metal volume provers for volumes up to 2000 gal (7600 liters[†]). Volume provers with volumes up to 1900 L (500 gal) are normally calibrated gravimetrically; larger volumes are calibrated by volume transfer using provers that have been calibrated gravimetrically. The uncertainty in the volume calibration depends upon the method used as well as the design and volume of the prover. For slicker plate type volume provers, the uncertainty may be as low as 0.004 %. For neck scale type volume provers, the uncertainty is a function of the volume and neck diameter. Typical uncertainties for neck scale provers are 0.015 % + 0.003 gal or 0.015 % + 0.012 L [about 0.3 % for a 1 gal (3.8 L) volume prover and 0.02 % for a 100 gal (380 L) prover].

Customers should consult the web address

<u>http://ts.nist.gov/MeasurementServices/Calibrations/mechanical_index.cfm</u> to find the most current information regarding our calibration services, calibration fees, technical contacts, turn around times, and instrument submittal procedures.

2. Design Philosophy and Theory

There are two common types of volume provers, distinguished by the way their full condition is determined; they are the slicker plate type and the neck scale type. For the <u>slicker plate type</u>, shown in Figure 1, the container is overfilled with water as permitted by the surface tension and then the excess water is sheared off with a flat transparent plate thus defining the volume as that enclosed by the container and the plate. Transparency of the plate enables inspection for voids (i.e., bubbles). For the <u>neck scale type</u>, shown in Figures 2 and 3, the volume is defined by reading a sight-glass-and-scale unit mounted on its neck. Either type of volume prover may be designed to be emptied by pouring out of the top (for the smaller sizes) or through a valve at the bottom. The top pouring style is shown in Figure 2 and the bottom drain type in Figure 3. More recommendations regarding the design of volume provers can be found in NIST Handbook 105-3 [Harris, 1997].

The horizontal cross section of any metal volume prover must be circular and its shape must permit complete emptying and draining. These volume provers must be sufficiently rigid to prevent appreciable distortion when full of water. The inside surface must be corrosion resistant and clean. All inside seams must be smooth to eliminate any traps for air (when being filled) or water (when being drained).

NIST maintains facilities for calibrating volume provers based on two different categories of methods: gravimetric methods and volume transfer methods. In the <u>gravimetric method</u>, the volume of distilled water required to fill a volume prover up to its full reference mark is determined by measuring the mass and the temperature of the water, calculating the density of the water from an appropriate empirical expression, and then calculating the volume from the definition of density. Distilled water is used because its density is well known as a function of temperature. The gravimetric volume calibration technique is a primary calibration method since it is directly traceable to NIST mass and temperature standards.

[†] The US gallon (231 in³, 0.003785412 m³, 3.785412 L) is the common unit of liquid volume used in commerce in the United States. Accordingly, to better communicate with the intended audience, in this publication US gallons are used in descriptions of volume provers for which the manufacturers have used US gallons, rather than the equivalent of gallons expressed in the less familiar m³ of the International Systems of Units (SI). SI units are normally used in publications of the National Institute of Standards and Technology.

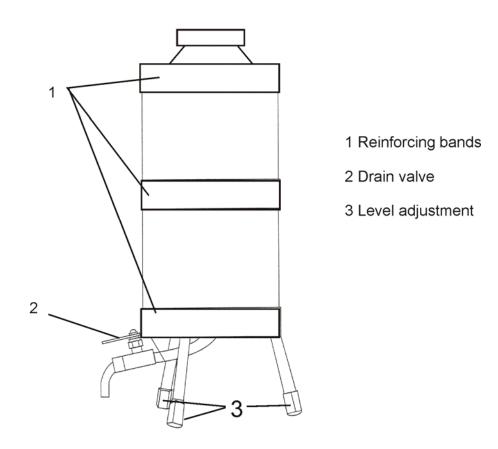


Figure 1. Schematic of slicker plate volume prover with a bottom drain. Top emptying styles are available in the smaller sizes.

In the <u>volume transfer method</u>, a volume prover is calibrated by filling it to its full reference mark with a known volume of tap water determined using working standard volume provers which were previously calibrated by the gravimetric method. Only the thermal expansion over a limited temperature range need be known for the water used for the calibration by transfer, rather than the density as in the gravimetric method. Measurements done by the NIST Fluid Metrology Group have shown that the difference in the thermal expansion of distilled water and tap water is negligible over the temperature range of interest and the use of tap water is far more convenient and less expensive than distilled water. The volume transfer method is used for calibrating volume provers that are too large to fit in the NIST gravimetric facility (usually in excess of 1900 L or 500 gal).

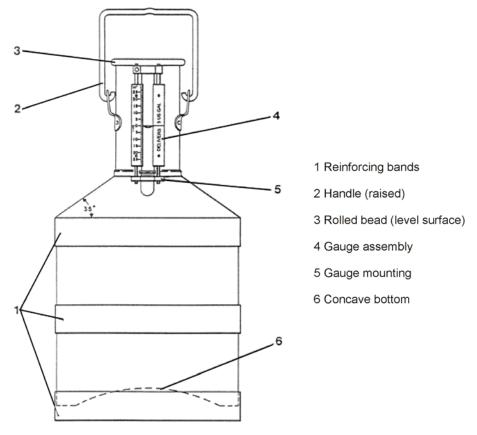


Figure 2. Neck scale volume prover, top emptying style.

Measurements of contained volume and delivered volume are both vital to commerce. <u>Contained volume</u> is the volume of liquid required to fill a dry volume prover to the full reference mark. <u>Delivered volume</u> is the volume of liquid that drains from a volume prover, originally filled to the full reference mark, under specified conditions. For a volume prover with a bottom drain, it is normally the volume that drains from the volume prover during the time from the opening of the valve to the closing of the valve 30 seconds after the cessation of the main flow. For a top pouring volume prover, it is normally the volume emptied from the volume prover from the time of first issue until 10 seconds after the cessation of the main flow with the volume prover held at an angle of 70° with respect to horizontal. Delivered volume is also the volume of water required to fill a volume prover to its full reference mark that has been pre-wetted by being filled to the full reference mark and then drained under the specified conditions. The contained volume is always larger by a few hundredths of a percent than the delivered volume for a given volume prover due to water that clings to the wall of the volume prover after draining.

To assess repeatability of the volume prover, and to check the quality of the calibration results, the methods described herein are normally repeated 5 times and the results analyzed statistically.

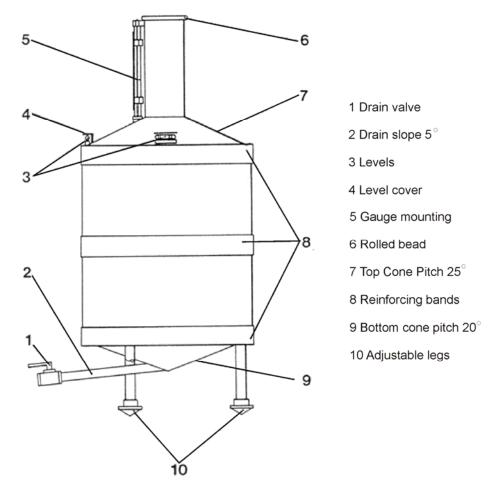


Figure 3. Neck scale volume prover, bottom drain style.

3. Description of NIST Facilities

3.1 Gravimetric Facility

The mass of distilled water required to fill a volume prover is determined using weigh scales. Since downward air currents > 0.15 m/s on the platform of a weigh scale can perturb the mass measurements, careful control of the direction and of the strength of air currents is important. The control of air currents, as well as the ambient temperature, is achieved by locating the gravimetric facility in an isolated laboratory module (a room-within-a-room) with its own ventilation and temperature control systems.

Two weigh scales, of 60 kg and 600 kg capacity, have been installed in the module. The 60 kg weigh scale is calibrated with weights from a 65 kg set which had been calibrated by the NIST Acoustics, Mass, and Vibrations Group. The 600 kg weigh scale is calibrated with a set of twelve 45 kg weights, which are calibrated on the 60 kg weigh scale. Both weigh scales are used in the up-loading cycle only to avoid the consequences of hysteresis. Further details of the calibration of the weigh scales are given in Appendix A.

The direct-weighing gravimetric method (see § 4.1.1 and § 4.1.2) is used for volume provers smaller

than 380 L (100 gal). Typically, the 60 kg weigh scale is used for volume provers of 38 L (10 gal) or smaller, while the 600 kg weigh scale is used for volume provers from 38 L to 380 L (10 gal to 100 gal).

The floor area of the laboratory module is 4.9 m by 6.1 m, and its ceiling is 4.9 m high. In one corner is a mezzanine, 1.8 m by 2.4 m in area, located 2.1 m above the floor, which is designed to support the 600 kg weigh scale with a 456 L container of water such that weighed amounts of distilled water can be drained into volume provers that exceed the capacity of the weigh scale (see gravimetric transfer method, § 4.1.3). This permits gravimetric calibration of volume provers up to 1900 L, the maximum size that can be accomodated by the laboratory module.

The laboratory module is equipped with a 0.2 m diameter floor drain and a crane with a lifting capacity of 1000 kg. The module contains a 9500 L storage tank for distilled water with a plumbing system to distribute the water to 3 convenient sites within the module. Distilled water is supplied by a still located in the adjacent room.

Water and air temperatures are measured with thermistors traceable to the NIST Thermometry Group. Experiments have shown that the mixing during filling of the volume prover with water in a normal calibration cycle results in temperature gradients that are 40 mK or less and this is considered as a component in the uncertainty analysis.

Room temperature, barometric pressure, and room relative humidity measurements are made in order to make air buoyancy corrections to all mass measurements.

3.2 Volume Transfer Facility

The Fluid Metrology Group maintains a volume transfer facility that is used to calibrate volumes between 1900 L (500 gal) and 7600 L (2000 gal) by the volume transfer method (see § 4.2). This facility has a lift with a platform of sufficient capacity to support a filled 380 L (100 gal) volume prover at the appropriate height so as to drain into a volume prover under test located on the floor. Water temperature is measured with thermistors traceable to the NIST Thermometry Group.

4. Calibration Procedures

There are four calibration situations to which the gravimetric facility is applicable and three calibrations situations to which the transfer facility is applicable. Detailed procedures for all seven situations are presented for the sake of completeness, however not all of the methods are routinely applied in our calibration service.

All of the calibration methods share the following initial steps:

- 1. Inspect the volume prover for damage and/or rust. Ensure that the interior of walls of the prover (including the neck and sight glass if applicable) are clean and dry.
- 2. Record the manufacturer's label information: maker, model number, serial number, nominal volume, volumetric coefficient of thermal expansion, maximum and minimum neck scale values, and volume represented by each scale division (if applicable). Also, make a note describing the condition of the drain valve (e.g., new, old, rusted, etc).

Whenever measurements of the neck scale are made, appropriate scale reading aids are used to avoid errors due to parallax.

A bottom drain style volume prover (i.e., with a valve) is drained by opening the valve and leaving it open for 30 seconds after the cessation of the main flow. A top pouring style volume prover is

drained by pouring, with the volume prover held at an angle of approximately 70° with respect to horizontal, including 10 seconds after the cessation of the main flow.

Generally, five measurements of the prover volume are made in order to assess the repeatability of the calibration procedures. The 5 repeated volume measurements also serve as a quality control measure: outliers can be detected (using Chauvenet's criterion [Coleman and Steele, 1999]) and replaced by new data sets.

With the exception of the weigh tank method, all of the methods can be used to determine contained or delivered volume. However, to measure the contained volume, the prover must initially be completely dry. So using the direct weighing method as an example, a single mass of the prover measured when it is dry is used with the 5 subsequent full mass measurements. This is done because it is impractical to dry the prover between repeated volume measurements, but it should be noted that the contained volume is not based on 5 separate dry mass measurements. In the case of volumetric transfer methods, the first filling of the dry prover delivers the contained volume. Five subsequent fillings give 5 measurements of the delivered volume.

In the case of provers with neck scales, the 5 repeated measurements are made close to the zero mark on the neck scale. During the last of the five repeats, the neck is filled to 5 different levels (one of which is nominally zero) in order to perform a neck scale calibration.

4.1 Gravimetric Methods

The four volume calibration situations to which the gravimetric volume facility is applicable are:

- 1. <u>direct weighing of neck scale type</u> volume provers to determine contained and/or delivered volume,
- 2. <u>direct weighing of slicker plate type</u> volume provers to determine contained and/or delivered volume,
- 3. <u>pre-weighing</u> the water before filling neck scale type volume provers to determine contained and/or delivered volume, used for the calibration of volume provers that exceed the limits of the 600 kg weigh scale, and
- 4. emptying a volume prover into a suitable container, which is weighed to determine the delivered volume of a volume prover, known as the <u>weigh tank</u> <u>method</u>.

All of the gravimetric methods require calibration of the weigh scale before its use via the procedure given in Appendix A.

Each of the four gravimetric methods has a separate procedure given below.

4.1.1 Gravimetric Method: Direct Weighing of a Neck Scale Volume Provers

The calibration of a neck scale type volume prover by the direct weighing consists of the following steps [Houser, 1973]:

- 1. Level the volume prover on the platform of the weigh scale.
- 2. Weigh the empty, clean, dry volume prover and record the weigh scale reading.
- 3. Fill the volume prover with distilled water up to an appropriate mark on the neck scale.
- 4. Inspect the volume prover for leaks.

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- 5. Measure the temperature of the water in the volume prover, record the readings, and then remove the temperature sensors.
- 6. Measure and record the room air temperature, atmospheric pressure, and relative humidity.
- 7. Read and record the deviation of the location of the meniscus from zero on the neck scale, in scale divisions.
- 8. Weigh the filled volume prover and record the weigh scale reading.
- 9. Drain the volume prover.
- 10. Lift the volume prover off the weigh scale platform and restore it to nullify hysteresis effects.
- 11. Weigh the drained volume prover and record the weigh scale reading.
- 12. Calculate the air density, ρ_{air} , in kg/m³, via [Jaeger and Davis, 1984]

$$\rho_{\rm air} = \frac{3.4848 \times 10^{-3}}{(T+273.15)} \left\{ P - 6.65287 \times 10^8 U \ e^{\left[-5315.56/(T+273.15)\right]} \right\}$$
(1)

where:

- P is the atmospheric pressure in Pa,
- U is the relative humidity expressed in percent, and
- T is the air average temperature in °C, all measured in step 6.
- 13. Calculate the indicated mass of the empty volume prover, m_e , via equation 3A of Appendix A.
- 14. Calculate the indicated mass of the filled volume prover, $m_{\rm f}$, via equation 3A.
- 15. Calculate the indicated mass of the drained volume prover, $m_{\rm d}$, via equation 3A.
- 16. Calculate the density of the distilled water, $\rho(T_w)$, in kg/m³, via the equation of Patterson and Morris [1994]

$$\rho(T_{\rm w}) = \rho_0 \left\{ 1 - \left[A(T_{\rm w} - T_0) + B(T_{\rm w} - T_0)^2 + C(T_{\rm w} - T_0)^3 + D(T_{\rm w} - T_0)^4 + E(T_{\rm w} - T_0)^5 \right] \right\}$$
(2)

where:

 $\rho_{0} = 999.97358 \text{ kg/m}^{3}$ $A = 7.0134 \text{ x } 10^{-8} (^{\circ}\text{C})^{-1}$ $B = 7.926504 \text{ x } 10^{-6} (^{\circ}\text{C})^{-2}$ $C = -7.575677 \text{ x } 10^{-8} (^{\circ}\text{C})^{-3}$ $D = 7.314894 \text{ x } 10^{-10} (^{\circ}\text{C})^{-4}$ $E = -3.596458 \text{ x } 10^{-12} (^{\circ}\text{C})^{-5}$ $T_{0} = 3.9818 ^{\circ}\text{C}$ $T_{w} \text{ is the average temperature of the water in }^{\circ}\text{C}.$

17. Calculate the contained volume of the volume prover in m^3 at T_w , adjusted to a neck scale reading of zero, via

$$V_{\text{contain}}(T_{\text{w}}) = \frac{m_{\text{f}} - m_{\text{e}}}{\rho(T_{\text{w}}) - \rho_{\text{air}}} - h$$
(3)

where:

h is the deviation of the location of the meniscus from zero (in m³) with the appropriate algebraic sign applied. Values of h above zero are positive; those below zero are negative.

Equation (3) is derived in Appendix B.

18. Calculate the delivered volume of the volume prover in m^3 at the temperature of the water during the test, T_w , adjusted to a neck scale reading of zero, via

$$V_{\text{deliver}}(T_{w}) = \frac{m_{\text{f}} - m_{\text{d}}}{\rho(T_{w}) - \rho_{\text{air}}} - h \tag{4}$$

Equation (4) is derived in Appendix B.

19. Calculate the contained and delivered volumes of the prover at the desired reference temperature requested by the customer, via

$$V(T_{\rm ref}) = C V(T_{\rm w}) [1 - \beta_{\rm t} (T_{\rm w} - T_{\rm ref})]$$
(5)

where:

- V is either the contained or delivered volume,
- C is the appropriate conversion factor from m^3 to the volume unit requested by the customer,
- β_t is the volumetric coefficient of thermal expansion for the volume prover obtained from the volume prover label or from a handbook based on the volume prover material of construction, and
- $T_{\rm ref}$ is the reference temperature specified by the customer. It is normally 15.56 °C (60 °F).

The volumetric coefficient of thermal expansion for the prover is $3 \times$ the linear coefficient of thermal expansion. For the most common material of construction, stainless steel, we use a volumetric coefficient of thermal expansion of 48 parts in 10^6 / °C. Hence for a 10 °C increase in temperature, the contained and delivered volumes for a stainless steel prover will increase by $10 \times 0.000048 = 0.048$ %.

4.1.2 Gravimetric Method: Slicker Plate Volume Provers

The calibration of a slicker plate volume prover by the gravimetric method is done by modifying the procedure for the neck scale type volume prover:

Fill the slicker plate volume prover with distilled water within a few millimeters of the top of the neck. Measure the temperature of the water in the volume prover and record. Finish filling the volume prover such that the water extends above the top of the neck of the volume prover due to surface tension. Shear off the excess by sliding a transparent plate across the top of the neck. Absorb the excess water with towels and discard. Transparency of the slicker plate enables visual inspection for voids under the plate; do not allow bubbles. For a slicker plate volume prover, there is no neck

scale and so $h \equiv 0$.

Omit steps related to measuring the height of the water in the neck and set h equal to 0 in equations 3 and 4.

4.1.3 Gravimetric Transfer Method: Pre-weighed Water

The pre-weighed water method is used to calibrate neck scale volume provers that have such large dimensions that they cannot be placed on the platform of the 600 kg weigh scale or have such capacity that the mass of the volume prover filled with water exceeds the capacity of the 600 kg weigh scale. The method is useful for volume provers with capacities up to 1900 L (500 gal), which is the maximum size that will fit in the volume laboratory module.

It is possible to obtain contained or delivered volumes via this method depending upon whether the volume prover is dry or pre-wetted at the outset of the calibration.

The procedures are:

- 1. Install the 600 kg weigh scale on the mezzanine and calibrate it with reference masses after moving (see Appendix A). Place the 120 gal (456 L) tank on the weigh sale in approximately the center of the scale pan.
- 2. Level the volume prover under test at an appropriate location on the floor so that it can be filled with successive volume transfers from the tank on the mezzanine.
- 3. Provide appropriate plumbing from the drain valve of the 120 gal tank on the weigh scale to the neck of the volume prover under test.
- 4. If the volume prover under test is to be calibrated for contained volume, the inside must be dry at the outset of the calibration. If it is to be calibrated for delivered volume, the inside must be pre-wetted at the outset which is accomplished by filling the volume prover with water up to the full reference mark, allowing the volume prover to drain through the valve, and closing the valve 30 seconds after the cessation of the main flow.
- 5. Fill the 120 gal tank with distilled water.
- 6. Record the weigh scale reading for the filled 120 gal tank.
- 7. Measure and record the room air temperature, atmospheric pressure, and relative humidity.
- 8. Drain the 120 gal tank into the volume prover under test without the loss of any water. It is advisable to place a finger over the opening of the sight glass tube of the volume prover under test to prevent water from jetting up the tube. This procedure is followed without interruption and completed within 3 hours so that loss by evaporation can be considered negligible.
- 9. Lift the 120 gal tank off the weigh scale platform and restore it to nullify hysteresis effects.
- 10. Record the weigh scale reading for the empty 120 gal tank.
- 11. Repeat steps 5 through 10 until the volume prover under test is filled up to the proximity of the zero mark on the neck scale.
- 12. Inspect the volume prover under test for leaks.

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- 13. Read and record the deviation of the location of the meniscus from zero on the neck scale in volume units.
- 14. Measure the temperature of the water in the volume prover under test and record.
- 15. Calculate the air density, ρ_{air} , in kg/m³, via equation 1.
- 16. Calculate the indicated masses of the filled 120 gal tank, m_{1i} , where i is the index tracking the tank refills, via equation 3A of Appendix A.
- 17. Calculate the indicated masses of the drained 120 gal tank, m_{2i} , where i is the index tracking the tank refills, via equation 3A.
- 18. Calculate the density of the distilled water, $\rho(T_w)$, in kg/m³, via equation 2.
- 19. Calculate the volume in m^3 , adjusted to a neck scale reading of zero, from

$$V_{\rm cal}(T_{\rm w}) = \sum_{\rm i} \left[\frac{(m_{\rm li} - m_{\rm 2i})}{\rho(T_{\rm w}) - \rho_{\rm air}} \right] - h$$
(6)

where:

- $V_{cal}(T_w)$ is either the contained volume or the delivered volume depending upon whether the volume prover was dry or pre-wetted at the outset of the calibration, in m³,
 - m_{li} is the indicated mass of the 120 gal tank and the water before draining into the volume prover under test, in kg, and
 - m_{2i} is the indicated mass of the 120 gal tank and the water after draining into the volume prover under test, in kg.
- 20. Calculate the contained and delivered volume at the desired reference temperature requested by the customer via equation 5.

4.1.4 Gravimetric Method: Weigh Tank

The weigh tank technique is used to determine the delivered volume of a prover by filling it with distilled water up to its full reference mark and emptying it into a suitable container that is weighed with and without the water. The weigh tank is usually a light-weight plastic or glass container. The technique is used when the mass of the volume prover filled with water exceeds the capacity of the weigh scale but the mass of the plastic tank and the water is within the capacity of the weigh scale. It is also used for "cubic foot bottles". The procedure is:

- 1. Level the volume prover under test at an appropriate elevation above the floor.
- 2. Provide appropriate plumbing from the drain valve of the volume prover under test to the weigh tank.
- 3. Fill the volume prover under test up to the full reference mark with distilled water.
- 4. Inspect the volume prover under test for leaks.
- 5. Weigh and record the weigh scale reading for the empty weigh tank.

- 6. Measure and record the room air temperature, atmospheric pressure, and relative humidity.
- 7. If possible, measure the temperature of the water in the volume prover under test and record.
- 11. Drain the volume prover under test into the weigh tank, following normal draining procedures.
- 12. Weigh and record the weigh scale reading for the weigh tank with the water.
- 13. If it was not possible to measure the temperature of the water in the volume under test, measure the temperature of the water in the weigh tank and record.
- 14. Calculate the air density, ρ_{air} , in kg/m³, via equation 1.
- 15. Calculate the indicated mass of the empty weigh tank, $m_{\rm e}$, via equation 3A of Appendix A.
- 16. Calculate the indicated mass of the weigh tank and the water, m_f , via equation 3A.
- 17. Calculate the density of the distilled water, $\rho(T_w)$, in kg/m³, via equation 2.
- 18. Calculate the delivered volume at T_{ref} in m³ from

$$V_{\text{deliver}}(T_{\text{ref}}) = \left[\frac{m_{\text{f}} - m_{\text{e}}}{\rho(T_{\text{w}}) - \rho_{\text{air}}}\right] \left[1 - \beta_{\text{t}}(T_{\text{w}} - T_{\text{ref}})\right]$$
(7)

where:

- $m_{\rm f}$ is the mass of the weigh tank and water, in kg, and
- $m_{\rm e}$ is the mass of the empty weigh tank, in kg.

4.2 Volume Transfer Method

Volumes larger than 500 gal and no larger than 2000 gal are calibrated by one of three transfer methods:

- 1. calibrate a neck scale volume prover for contained or delivered volume using a neck scale volume prover as the working standard,
- 2. calibrate a neck scale volume prover for contained or delivered volume using a slicker plate volume prover as the working standard, and
- 3. calibrate a slicker plate volume prover for delivered volume using a neck scale volume prover as the working standard.

It is not possible to calibrate a slicker plate volume prover for contained volume using the transfer method because the process of shearing off the water at the neck to define the full condition discards an unknown volume of the calibrated volume of water delivered by the working standard.

4.2.1 Volume Transfer Method: Neck Scale Volume Prover to Neck Scale Volume Prover

The calibration of a neck scale volume prover, using a neck scale volume prover for the working standard, consists of the following steps, assuming, for simplicity, emptying only once from one working standard is required [Houser, 1973]:

1. Place and level an appropriate working standard volume prover, the volume of which has been previously determined by gravimetric method, on the elevated platform set at the appropriate

height.

- 2. Level the volume prover under test at an appropriate location with respect to the elevated platform.
- 3. Provide appropriate plumbing between the drain of the working standard and the neck of the volume prover under test.
- 4. If the volume prover under test is to be calibrated for contained volume, the inside must be dry at the outset of the calibration. If it is to be calibrated for delivered volume, the inside must be prewet at the outset.
- 5. Fill the working standard with tap water up to a convenient mark on the neck scale.
- 6. Measure the temperature of the water in the working standard, record the readings, and remove the temperature sensors.
- 7. Read and record the deviation from zero of the location of the meniscus on the neck scale for the working standard in volume units.
- 8. Drain the working standard, without the loss of any water, into the volume prover under test, following normal drain procedures. It is advisable to place a finger over the opening of the sight glass tube of the volume prover under test to prevent water from jetting up the tube.
- 9. Read and record the deviation from zero of the location of the meniscus on the neck scale for the volume prover under test in volume units.
- 11. Measure the temperature of the water in the volume prover under test and record.
- 12. Calculate the density of the water in the working standard, $\rho(T_{w,s})$ via equation 2.
- 13. Calculate the density of the water in the volume prover under test, $\rho(T_{w,t})$ via equation 2.
- 14. Calculate the volume of the prover under test, $V_t(T_{w,t})$, adjusted to a neck sale reading of zero via,

$$V_{t}(T_{w,t}) = \frac{\rho(T_{w,s}) (V_{s} + h_{s}) [1 + \beta_{s} (T_{w,s} - T_{ref,s})]}{\rho(T_{w,t})} - h_{t}$$
(8)

where:

- $V_{\rm s}$ is the delivered volume of the working standard at the reference temperature,
- $h_{\rm s}$ is the deviation of the location of the meniscus from zero on the neck scale of the working standard, in volume units, with the appropriate algebraic sign applied,
- β_s is the volumetric thermal expansion coefficient for the working standard,
- $T_{\rm w.s.}$ is the temperature of the water in the working standard,
- $T_{\rm refs}$ is the reference temperature for the working standard,
- $h_{\rm t}$ is the deviation of the location of the meniscus from zero on the neck scale of the volume prover under test, in volume units, with the appropriate algebraic

sign applied,

 $T_{\rm w,t}$ is the temperature of the water in the volume prover under test.

Equation 8 will yield contained volume at $T_{w,t}$ if the inside walls of the prover under test were dry at the outset of the calibration, or delivered volume at $T_{w,t}$ if the inside walls of the prover were pre-wetted at the outset of the calibration. Equation 8 is derived in Appendix C.

Equation 8 shows why tap water can be used rather than distilled water in the volume-bytransfer calibration process. Equation 8 contains the ratio $\rho(T_{w,s})/\rho(T_{w,t})$. Following the form of equation 2, this ratio can be expressed as,

$$\frac{\rho(T_{\rm w,s})}{\rho(T_{\rm w,t})} = \frac{\rho(T_0)f(T_{\rm w,s} - T_0)}{\rho(T_0)f(T_{\rm w,t} - T_0)} = \frac{f(T_{\rm w,s} - T_0)}{f(T_{\rm w,t} - T_0)}$$
(9)

where:

 $\rho(T_0)$ is the density at a specified temperature and is a constant,

$$f(T_{w,s} - T_0)$$
 and $f(T_{w,t} - T_0)$ are the thermal expansion terms for the tap water
at $T_{w,s}$ and $T_{w,t}$ respectively.

Measurements by the NIST Fluid Metrology Group have demonstrated that the thermal expansion coefficients A through E and T_0 of equation 2 also apply to tap water over the temperature range of interest. Hence, equation 2 can be used to calculate water density in equation 8 when tap water is used.

In some cases, calibration by transfer may require several emptyings of more than one working standard. Equation 8 requires the following modifications for this situation

$$V_{t}(T_{w,t}) = \frac{\sum_{i} \left[\rho(T_{w,s,i}) (V_{s,i} + h_{s,i}) \left[1 + \beta_{s,i} (T_{w,s,i} - T_{ref,s}) \right] \right]}{\rho(T_{w,t})} - h_{t}$$
(10)

where $\rho(T_{w,s,i})$, $h_{s,i}$, and $T_{w,s,i}$ may change when the same working standard is used for multiple emptyings, and, in addition, $V_{s,i}$ and $\beta_{s,i}$, will vary if more than one working standard is used. The index i is used to track the number of emptyings.

15. Calculate $V_t(T_{ref})$:

$$V_{t}(T_{ref}) = \frac{\rho(T_{w,s}) (V_{s} + h_{s}) [1 + \beta_{s} (T_{w,s} - T_{ref,s})]}{\rho(T_{w,t}) [1 + \beta_{t} (T_{w,t} - T_{ref})]} - h_{t}$$
(8')

$$V_{t}(T_{ref}) = \frac{\sum_{i} \left[\rho(T_{w,s,i}) (V_{s,i} + h_{s,i}) [1 + \beta_{s,i} (T_{w,s,i} - T_{ref,s})] \right]}{\rho(T_{w,t}) [1 + \beta_{t} (T_{w,t} - T_{ref})]} - h_{t}.$$
 (10')

4.2.2 Volume Transfer Method: Slicker Plate Volume Prover to Neck Scale Volume Prover

When a neck scale volume prover is calibrated using a slicker plate working standard, the procedure of Section 4.2.1. is followed with some modifications.

Fill the slicker plate volume prover with distilled water within a few millimeters of the top of the neck.

Measure the temperature of the water in the volume prover and record. Finish filling the volume prover such that the water extends above the top of the neck of the volume prover due to surface tension. Shear off the excess by sliding a transparent plate across the top of the neck. Absorb the excess water with towels and discard. Transparency of the slicker plate enables visual inspection for voids under the plate; voids must not be allowed to occur.

Omit steps involving reading the level of the water in the neck scale of the working standard and set $h_s \equiv 0$ in equations 8 and 10.

4.2.3 Volume Transfer Method: Slicker Plate Volume Prover, Delivered Volume

It is possible to calibrate the delivered volume of a slicker plate volume prover by emptying it into a neck scale volume prover, which has been calibrated for contained volume, provided one emptying of the slicker plate volume prover will fill the neck scale volume prover up into the neck region such that the neck scale can be read. The procedure is:

- 1. Place and level the volume prover under test on the elevated platform.
- 2. Provide appropriate plumbing between the drain of the volume prover under test and the neck of the working standard volume prover.
- 3. Level the working standard volume prover at an appropriate location with respect to the elevated platform.
- 4. Fill the volume prover under test with tap water within a few millimeters of the top.
- 5. Measure the temperature of the water in the volume prover under test and record.
- 6. Finish filling the volume prover under test to the limit permitted by the surface tension and shear off the excess water with a transparent plate.
- 7. Drain the volume prover under test, without the loss of any water, into the working standard, following normal draining procedures. It is advisable to place a finger over the opening of the sight glass tube of the volume prover under test to prevent water from jetting up the tube.
- 9. Read and record the deviation from zero of the location of the meniscus on the neck scale for the working standard, in volume units.
- 10. Measure the temperature of the water in the working standard and record.
- 11. Calculate the density of the water in the working standard, $\rho_s(T_{w,s})$, via equation 2.
- 12. Calculate the density of the water in the volume prover under test, $\rho_t(T_{w,t})$, via equation 2.
- 13. Calculate the delivered volume of the volume prover under test, $V_{\text{deliver}}(T_{\text{w,t}})$, via

$$V_{\text{deliver}}(T_{w,t}) = \frac{\rho(T_{w,s})(V_s + h_s)[1 + \beta_s(T_{w,s} - T_{\text{ref},s})]}{\rho(T_{w,t})}$$
(11)

4.3 Neck Scale Calibrations

Neck scales can be calibrated by various methods, including:

- 1. *Volumetric Method:* add known volumes of water to the prover under test and observe the change in neck scale reading,
- 2. *Displacement Method:* insert objects of known volumes (such as metal spheres of known diameter) through the neck into the prover and observe the change in neck scale reading,
- 3. *Gravimetric Method:* add water to the prover to attain the desired neck scale readings and observe the changes in mass of the filled prover with a weigh scale.

A more detailed description of the gravimetric method follows.

- 1. Calibrate the appropriate weigh scale, following the procedures given in Appendix A.
- 2. Determine which neck scale increments will be calibrated. For example, for a neck scale that ranges from -100 in³ to 100 in³, one might choose to calibrate the -80 in³, -40 in³, 0 in³, 40 in³, and 80 in³ levels.
- 3. Fill the volume prover with water up to the lowest neck scale reading to be calibrated.
- 4. Read and record the deviation of the location of the meniscus from zero on the neck scale.
- 5. Record the mass indicated by the weigh scale.
- 6. Add distilled water to the volume prover under test such that the water level rises to the next neck scale set point, read and record the meniscus level on the neck scale, record the mass, and repeat this process until all the set points have been measured.
- 7. Measure the temperature of the water and record the value.
- 8. Measure the room air temperature, barometric pressure, and the relative humidity and record the values.
- 9. Drain the prover. Measure and record the drained weight.
- 10. Use equations 4 and 5, with h set equal to zero, to calculate the volume of water in the prover from the mass measurements. The correct neck scale reading can be calculated via

$$V_{\text{neck}} = V_{\text{deliver}} \left(T_{\text{ref}} \right) - V_{\text{nominal}}$$
(12)

where:

 V_{nominal} is the nominal volume of the prover at a neck scale reading of zero. The calculated neck volume V_{neck} can be converted to the desired number of volume units (including the number of neck scale divisions).

Note: if the dry weight of the prover is used instead of the drained weight (equations 3

and 5), the neck scale calibrations will apply to contained volume rather than delivered volume.

5. Viscosity Corrections

Volume calibration is done at ambient laboratory temperatures, normally in the range of 21 °C to 24 °C. Usually, the customer requests that the volume be referenced to some other temperature (often it is 15.56 °C or 60 °F). The calculation of contained volume at the reference temperature is done using the thermal expansion coefficient of the material from which the volume prover is made, as expressed in equation 5. Gravimetric calibrations that we have conducted at room temperature and 15.5 °C have demonstrated this procedure to be correct.

Delivered volume is also a function of the viscosity of the water used. At higher temperatures, the viscosity will be lower and less water will cling to the interior walls of the prover. Thus, more water will drain out during the 30 s drain time, making the delivered volume at room temperature slightly larger than at 15.56 °C.

Theory suggests the difference between contained and delivered volume can be expressed as: [Bird, Stewart, and Lightfoot, 1960]

$$V_{\text{contain}}(T_{\text{w}}) - V_{\text{deliver}}(T_{\text{w}}) = kG \left[\frac{\nu(T_{\text{w}})}{t}\right]^{1/2}$$
(13)

where:

- k is a proportionality constant,
- *G* is a factor due to the geometry of the volume prover,
- t is the 30 second drain time between the cessation of the main flow and the closure of the drain valve,
- $v(T_{\rm w})$ is the kinematic viscosity of water.

Similarly, at T_{ref} ,

$$V_{\text{contain}}(T_{\text{ref}}) - V_{\text{deliver}}(T_{\text{ref}}) = kG \left[\frac{\nu(T_{\text{ref}})}{t}\right]^{1/2}$$
(14)

where:

 $v(T_{ref})$ is the kinematic viscosity of water at the reference temperature.

Solving equations 13 and 14 for $V_{\text{deliver}}(T_{\text{ref}})$:

$$V_{\text{deliver}}(T_{\text{ref}}) = V_{\text{contain}}(T_{\text{ref}}) - \left[V_{\text{contain}}(T_{\text{w}}) - V_{\text{deliver}}(T_{\text{w}})\right] \left[\frac{\nu(T_{\text{ref}})}{\nu(T_{\text{w}})}\right]^{1/2} = V_{\text{contain}}(T_{\text{ref}}) - V_{\nu}$$
(15)

where:

 V_{ν} is the viscosity correction with units of volume.

The kinematic viscosity of water (dynamic viscosity divided by density) in m^2/s is given by:

$$v(T) = 1.76263 \times 10^{-6} - 5.4994 \times 10^{-8} T + 1.04326 \times 10^{-9} T^2 - 9.178 \times 10^{-12} T^3$$
(16)

Equation 16 was obtained by fitting a polynomial to the ratio of dynamic viscosity to density for water, over the temperature range from 10 °C to 30 °C, with values taken from the literature [Kell, CRC].

The viscosity correction is proportional to the difference between the contained and delivered volumes. This difference $V_{\text{contain}}(T_{\text{ref}}) - V_{\text{deliver}}(T_{\text{ref}})$ depends on the size of the prover. Based on results of volume determinations from 80 provers made at an average temperature of 22 °C, $V_{\text{contain}}(T_{\text{ref}}) - V_{\text{deliver}}(T_{\text{ref}})$ is approximately 0.02 % for a 100 gal prover and the difference increases to about 0.05 % for a 5 gal prover. (This is due to the surface area per unit volume being greater for a small prover than for a large prover.)

The viscosity correction in equation 15, $[v(T_{ref})/v(T_w)]^{1/2}$, is approximately 1.013 for a 1 °C temperature change near room temperature. Therefore, using a 100 gal prover at 22 °C as an example, we can expect it to deliver (22 °C – 15.56 °C) × 0.013/°C × 0.0002 = 0.000017 or 17 parts in 10⁶ more liquid due to a smaller viscosity than it would if it were used at 15.56 °C. For a 5 gal prover, the same temperature difference should lead to:

$$(22 \ ^{\circ}C - 15.56 \ ^{\circ}C) \times 0.013 / ^{\circ}C \times 0.0005 = 0.000048$$

or 48 parts in 10^6 increase in delivered volume.

Our data reduction spreadsheets list the uncorrected, as well as, the viscosity corrected values of the delivered volume. Unless otherwise requested by the customer, the text of our calibration report gives only the delivered volume without the viscosity correction and the viscosity correction is treated as an uncertainty component of the volume calibration.

Note that the weigh tank method does not provide enough data to determine the contained volume and hence the viscosity correction cannot be applied to this method.

6. Applying the Volume Calibration Results

Most of the volume provers calibrated at NIST have neck scales. Generally, there are 5 repeated volume determinations made at a nominal neck scale reading of zero and a neck scale calibration process that leads to calibration results at 4 set points spread over the range of the neck scale. Samples of results of this typical calibration are given in Tables 1, 2, and 3 for three different sized provers. Table 4 shows results for a 5 gal slicker plate type prover.

For many customers, the volume calibration is performed to demonstrate that the volume ascribed to the prover is the same as that determined at NIST, within some tolerance. But there are many other possible approaches for applying the calibration results when the prover is subsequently used as a working standard to measure volume. For instance, the calibration allows one to compare the volume determined by NIST to the volume indicated by the prover and to calculate a volume correction,

$$V_{\rm corr}(T_{\rm ref}) = V_{\rm delivered}(T_{\rm ref}) - V_{\rm indicated}(T_{\rm ref}).$$
(17)

In this case, we are determining the correction for delivered volume at the reference temperature. For

the most common calibration performed, there are 9 values for $V_{\rm corr}$, 5 at approximately zero on neck scale and 4 distributed over the range of the neck scale. One can calculate a first order least squares best fit on the 9 corrections in order to obtain the volume correction as a function of the neck scale reading and examples of this approach are shown in Tables 1 through 3. The zeroth order coefficient (intercept) of the linear fit can be added to the nominal prover volume to obtain the delivered volume as calibrated by NIST at a neck scale reading of zero. The first order coefficient (slope) of the best fit line can be used to correct for errors in the neck scale caused by mismatched neck cross sectional area and the length of a scale division.

Using Table 1 as an example, for a zero neck scale reading, the intercept value of -1.67 in^3 (= -4.18 divisions × 0.4 in³ / division) should be added to the nominal volume of 9702 in³ (42 gal) to obtain the NIST measured volume of 9700.33 in³. If the prover is used at a neck scale reading other than zero, the corrected volume of the prover would be calculated via

$$V_{\text{prover}} = V_{\text{nominal}} + \left[a_0 + a_1 N_D V_{\text{div}}\right]$$
(18)

where a_0 and a_1 are the best fit intercept and slope respectively, N_D is the number of scale divisions relative to the neck scale zero (below zero is a negative value), and V_{div} is the volume represented by a single scale division. Alternatively, for a given neck scale reading, the correction (in scale divisions) can be read from a graph as presented in Table 1 or a data table generated by the user.

If a customer chooses to apply viscosity corrections, he should start with the viscosity corrected delivered volume given in the data reduction spreadsheet. Then equation 15 must be rearranged algebraically to give $V_{\text{deliver}}(T_w)$ alone on the left hand side. The resulting equation can be used to calculate the delivered volume with viscosity effects taken into account at the temperature conditions that the customer users the prover. If the customer uses the prover with a liquid other than water, the appropriate values for density and kinematic viscosity should be used in any version of equation 15.

7. Uncertainty

In the following sections we will quantify the uncertainty of the volume calibration results for the methods most commonly used at NIST: 1) direct weighing of neck scale and slicker plate provers and 2) the volume transfer method for neck scale prover to neck scale prover.

It is important to note that the uncertainty analyses given herein are for the volume determinations made by the NIST volume calibration service and do not include components that must be considered by the customer during subsequent use of the prover as a working standard for volume. Some of these sources of uncertainty are: errors in reading the neck scale, viscosity effects caused by temperature or fluid changes, the effects of dirty surfaces in the prover or in the sight glass that cause changes in the draining or changes in the behavior of the meniscus, dents in the prover, poor leveling of the prover, leaks, incorrect relationship between neck scale increments and neck diameter.

The relative uncertainty of the volume measurement process may be expressed as [ISO 1996 and Coleman and Steele, 1999],

$$U_{\rm V} = k \left[\sum_{i=1}^{n} \left(\frac{1}{V} \frac{\partial V}{\partial x_i} u(x_i) \right)^2 + \frac{2}{V^2} \sum_{i=1}^{n} \sum_{j=i+1}^{n-1} \frac{\partial V}{\partial x_i} \frac{\partial V}{\partial x_j} u(x_i) u(x_j) r(x_i, x_j) + \frac{\sigma_{\rm V}^2}{V^2} \right]^{\frac{1}{2}}$$
(19)

where:

- V represents any of the data reduction equations used to calculate the prover volume,
- x_i are the variables in V,
- $u(x_i)$ are the uncertainties in the variables in V,

i and j are indices that are never equal

- n is the number of variables in V,
- σ_V^2 is the variance of replicated determinations of prover volume, and
- *k* is a coverage factor, typically about 2, selected to assure a 95 % confidence interval level for the measurement process and consistent with NIST policy [Taylor and Kuyatt, 1994],
- $r(x_i, x_i)$ is the correlation coefficient between variables x_i and x_j .

The second term on the right hand side of equation 19 is the correlation term used in the estimate of the uncertainty due to bias when any of the terms in a data reduction equation are correlated. For example, correlation can occur when:

- (a) one instrument is used to measure more than one term in an equation for V;
- (b) the same expression is used to calculate more than one term in an equation for V; and
- (c) more than one instrument used to measure terms in an equation for V are calibrated by the same standard.

For the gravimetric methods of volume calibration, the two indicated masses are measured with the same weigh scale and the mass uncertainties have a high degree of correlation. The two masses are subtracted from one another and taking the correlation of their uncertainty into account would have the effect of reducing the combined uncertainty of the volume determination. In the following uncertainty analysis, the mass uncertainties were treated as uncorrelated, resulting in the most conservative estimate of the combined uncertainty.

When the same working standard volume is used repeatedly to fill a larger prover under test via the volume transfer method, the uncertainty of $V_{\text{deliver}}(T_w)$ for the working standard volume is correlated. Because the volumes are added, considering their uncertainty fully correlated is a more conservative approach and that is the approach we will follow in the following uncertainty analysis.

For the volume transfer method, the correlated temperature uncertainties are negligible relative to the uncorrelated ones, and therefore they are treated as completely uncorrelated (most conservative treatment).

7.1 Uncertainty of the Gravimetric Method

Because equation 2 is implicit in these equations for V and its differentiation over the five

temperature dependant terms would be unwieldy, its first order approximation is used in this uncertainty analysis:

$$\rho(T_{\rm w}) = \rho_0 [1 - \beta_{\rm w} (T_{\rm w} - T_0)]$$
⁽²⁰⁾

where

- ρ_0 is the density of the distilled water at the water reference temperature, T_0 of 3.9818 °C, and
- β_{w} is the volumetric thermal expansion coefficient for water.

While the accuracy of equation 20 is inferior to that of equation 2, it is satisfactory for uncertainty analysis.

The complete data reduction equation for the gravimetric determination of $V_{\text{contain}}(T_{\text{ref}})$ is obtained by combining equations 3, 5, and 20. The result is

$$V_{\text{contain}}(T_{\text{ref}}) = \left[\frac{(m_{\text{f}} - m_{\text{e}})}{\rho_0 \left[1 - \beta_{\text{w}} (T_{\text{w}} - T_0)\right] - \rho_{\text{air}}} - h\right] \left[1 - \beta_{\text{t}} (T_{\text{w}} - T_{\text{ref}})\right].$$
(21)

The partial derivatives for equation 21 and their values are listed in Tables 1 through 4 for four volume provers to show example uncertainty analyses. Uncertainties for a customer calibration may be different from those given here, especially those related to the water height in a volume prover with a neck scale. Defined values having zero uncertainty are T_{ref} and T_0 .

The Guide to the Expression of Uncertainty in Measurement [ISO 1996] suggests classifying the uncertainty components as: <u>Type A</u>, uncertainties which are evaluated by statistical methods, and <u>Type B</u>, uncertainties which are evaluated by other means. Once a value for the uncertainty for each component is determined, it receives the identical mathematical treatment in equation 19 whether it is either Type A or B. The sources of uncertainties, and their types, for equation 21 are:

- u(h) is one fourth of the smallest division of the neck scale (read with a magnifier fitted with an anti-parallax device) (Type B),
- $u(m_{\rm f})$, $u(m_{\rm e})$ are based on analysis of calibration records and uncertainty of the calibration process for the weigh scales, normally less than 5 g for the 600 kg weigh scale, and less than 1 g for the 60 kg scale (Type B).
- $u(\rho_0), u(\beta_w)$ are based on the water density equation [Patterson and Morris, 1994] (Type B),
 - $u(\beta_t)$ was provided by the NBS Crystallography Section (Type B),
 - $u(T_w)$ is based on calibration records, the uncertainty of the temperature calibration process within the Fluid Metrology Group, and the normal variation of temperature within the volume prover (Type B),
 - $u(\rho_{air})$ is from the uncertainty of the equation for air density [Jaeger and Davis, 1984] and the uncertainties in the measurement of room temperature, pressure, and relative humidity (Type B),

- u(v) is the uncertainty due to viscosity effects on delivered volume (Type B), and
- $\sigma_{\rm V}^2$ is the variance of replicated determinations of prover volume (Type A).

The expression for delivered volume has an additional uncertainty (that does not apply to the contained volume) due to the effects of temperature on water viscosity and the difference in completeness of draining of the prover at $T_{\rm w}$ and $T_{\rm ref}$. The uncertainty in the delivered volume due to viscosity effects is assumed to have a rectangular distribution with $\pm a = V_v$, so that the standard uncertainty due to the viscosity correction is $V_v / (\sqrt{3})$ [Taylor and Kuyatt, 1994].

The coverage factor, k, in equation 18 is selected to assure a 95 % confidence interval level for the measurement process, consistent with NIST policy [Taylor and Kuyatt, 1994]. Small sample (< 10) statistics states that for a combined standard uncertainty, $U_{\rm V}$, the "effective degrees of freedom"

 $v_{\rm eff}$ of $U_{\rm V}$, which is approximated by appropriately combining the degrees of freedom of its components, should be used to establish the value of the coverage factor. Taylor and Kuyatt [1994] recommend that the Welch-Satterthwaite formula be used to determine the effective degrees of freedom for the measurement process. Based on the value obtained, the appropriate coverage factor, k, can be obtained from the t-distribution for degrees of freedom for a Gaussian distribution with a confidence interval of 95 %.

Tables 1 through 4 show data reduction spreadsheets and uncertainty calculations for four volume provers: 42 gal, 21 gal, 5 gal (all with neck scales), and a 5 gal slicker plate volume prover. Explanatory notes for Table 1 are given below.

- A) Volume prover identification, size, volume per smallest scale division, provided by manufacturer.
- B) Weigh scale calibration coefficients.
- C) Temperature sensor calibration coefficients.
- D) Two water temperatures and their average, used to calculate water density.
- E) Two air temperatures and their average, the barometric pressure, and relative humidity, used to calculate air density for buoyancy corrections to mass.
- F) Weights of the volume prover dry (one measurement entered 5 times), full (5 repeats), and drained (5 repeats).
- G) The neck scale readings for the 5 full weight measurements.
- H) Calculated prover volumes for the 5 repeats at room temperature, adjusted to scale reading of zero, without a viscosity correction.
- I) Prover volumes for the 5 repeats, corrected for thermal expansion to the reference temperature, in various units, contained and delivered.
- J) Viscosity values at the average calibration temperature and reference temperature (for the viscosity correction).
- K) Averages of the 5 repeats, contained and delivered volumes (without and with viscosity correction).
- L) Repeatability of the 5 volume measurements (a Type A component of the calibration uncertainty) and the expanded uncertainty.
- M) Coverage factor and degrees of freedom from the Welch-Satterthwaite analysis.
- N) Values of variables used in the volume calculation needed for the uncertainty analysis.
- O) Analytical expressions and values for the sensitivity coefficients, and the magnitude of the uncertainty for each uncertainty component.
- P) Uncertainty contribution (in parts in 10^6) for each uncertainty component.
- Q) Neck scale readings, correct neck scale divisions (calculated based on delivered volume calibration), and differences between them (corrections), for five liquid levels in the neck scale.
- R) Slope and intercept of a best fit line to correct neck scale readings to calculated delivered volume (in various units).
- S) A plot of neck scale correction versus neck scale reading (in neck scale divisions), both the measured points and the best fit line.

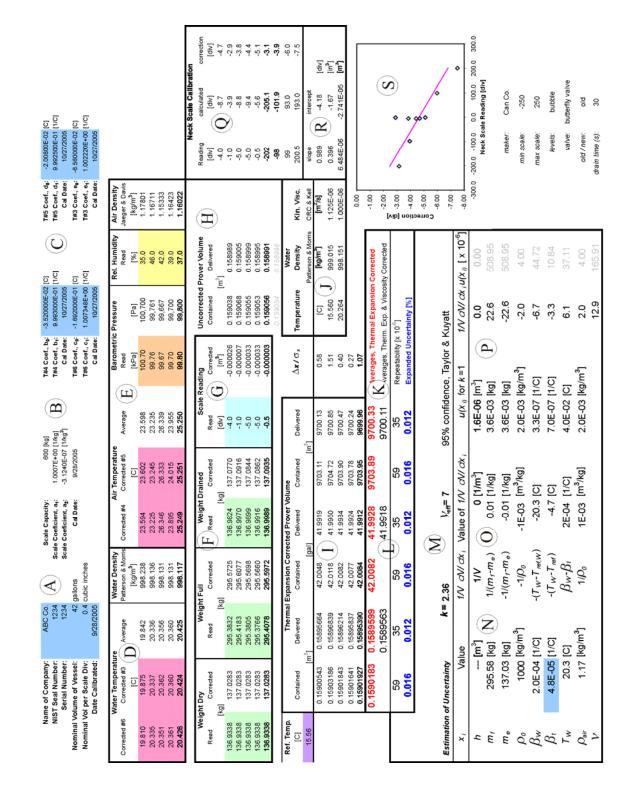


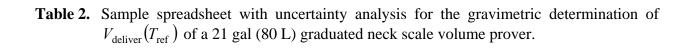
Table 1. Sample spreadsheet with uncertainty analysis for the gravimetric determination of $V_{\text{deliver}}(T_{\text{ref}})$ of a 42 gal (160 L) graduated neck scale volume prover. See text for key.

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42 gal

 c. 200800E-02 [c] e. 9.995500E-01 [1/C] e. 10777005 e. 100777005 r. 1007225E+00 [1/C] e. 100727206 	- 4	Neck Scale Calibration	Reading calculated correction [div] [div] [div]		-1.1-	-0.1 -1.0 -0.9 -1.0 -1.6 -0.6		C.U2-	39.4	slope intercept	-0.78	1.999 -1.56 [in [*]] 3.277E.05 -2.564E.05 [m [*]]						**	*	>> >> >>	•	-40.0	Mack Scale Keading Luny	maker: Can Co.	min scale: -90	max scale: 100	levels: tttached spirit level	va/ve: butterfly valve	o/d / new: old	drain time (s): 30
T#5 Coef., d ₆ : T#5 Coef., d ₁ : Cal Date: T#3 Coef., e ₆ : T#3 Coef., e ₆ : Cal Date: Cal Date:	Air Density Jaeger & Davis [kg/m ³] 1.18573 1.18141 1.17760 1.17747 1.17447								Kin. Visc.	CRC & Kell	[m ² /s]	1.125E-06 9.422E-07		00.00	-0.20		vib] 0	ction	οπe -0.80	-1.00	-1.20	-60.0								
[1] [1/0] [1/0]	Rel. Humidity Read [%] 43.0 43.0 43.0 43.0 43.0 43.0 43.0	Province Maltimum	Uncorrected Prover Volume Contained Delivered	[m ³]	0.079502	0.079491	0.079500	Water	Density	Patterson & Morris	[kg/m [*]]	999.015 007 586			n Corrected	sity Corrected					1/V dV/ dx ; u(x _i) [x 10 ⁻⁶]	0.15	2038.14	2038.14	4.00	56.63	25.71	37.11	4.00	685.57
-3.520000E-02 [C] 9.993000E-01 [1/C] 102772005 -1.092000E-01 [C] 1.007348E+00 [1/C] 102772005	Fressure [Pa] 100,900 100,900 100,900 100,900		Uncorrected Contained		0.079542	0.079528	0.079542	0.07 9004	Temperature		[C]	15.560 22 803	0		mal Expansior	n. Exp. & Visco	10 ^{.6}]	ertainty [%]		(uyatt	1/V dV/ dX i	0.4	45.1	-45.1	-2.0	-7.5	-5.1	6.1	2.0	26.2
T#4 Coef., b ₆ T#4 Coef., b ₁ Cal Date: T#6 Coef., c ₆ T#6 Coef., c ₁ Cal Date: Cal Date:	Barometric Pressure Read [KPa] [Pa] [00.90 100,90 100.90 100,90 100.90 100,90 100,90 100,90 100,90 100,90	Bandina	Scale Reading Corrected	[m³]	-0.000016	-0.000033	-0.00033		$\Delta x / \sigma_x$		0.58	1.27 0.97	0.60	0.87	Averages, Thermal Expansion Corrected	Averages, Therm. Exp. & Viscosity Corrected	Repeatability [x 10 ^{.6}	Expanded Uncertainty [%]		95% confidence, Taylor & Kuyatt	$u(x_{ij} \text{ for } k=1$	[m³]	[kg]	[kg]	[kg/m ³]	[1/C]	[1/C]	[C]	[kg/m ³]	
(g) [A6g] 1/kg ²]	Average 22.091 23.112 23.995 24.725	Carla	Scale Read	[div]	-0.5	0.1- 1.0	-1.0	ſ	Delivered		4849.25	4849.84 4840 13	4849.24	4849.72	4849.44	4849.22	99	0.021		95% confide	n(x)	8.2E-06 [m ³]	3.6E-03 [kg]	3.6E-03 [kg]	2.0E-03 [kg/m ³]	3.3E-07 [1/C]	7.0E-07 [1/C]	4.0E-02 [C]	2.0E-03 [kg/m ³]	
600 [kg] 1.0007E+00 [1/kg] -3.1240E-07 [1/kg ²] 9/28/2005	Air Temperature Corrected #5 [C] 22.084 23.117 23.117 23.995 24.738 24.738		'ained Corrected	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	107.2242	107.2220	107.2256	em	Contained	[in ³]	4851.50	4852.26	4851.59	4852.23	4851.80		85	0.024			' dV/ dx i	0 [1/m ³]	[/kg]	1/kg]	n³/kg]	5	5	1/C]	n ³ /kg]	
Scale Capacity: Scale Coeficient, a ₁ : Scale Coeficient, a ₂ : Scale Coeficient, a ₂ :	Ait Corrected #4 22.098 23.106 23.995 24.711 24.711	Wielshi D.	Weight Drained Read Corre	[kg]	107.1464	107.1470 107.1480	107.1507	Ind Drover Vol	Delivered		20.9924	20.9950 20.9950	20.9924	20.9944	20.9932	20.9923	99	0.021		V _{ett} = 11	Value of 1/V dV/ dx	0	0.01 [1/kg]	-0.01 [1/kg]	-1E-03 [m ³ /kg]	-22.8 [C]	-7.2 [C]	2E-04 [1/C]	1E-03 [m ³ /kg]	
Co S 234 Scale 234 Scale 21 galions 2 cubic inches 005	Water Density Patterson & Morris [kg/m ³] 997.586 997.574 997.571 997.571		Weight Full Corrected	[kg]	186.4242	186.3935 186.4257	186.4062	Thermal Evnansion Corrected Brover Volume	Contained	[gal]	21.0022	21.0055 21.0018	21.0026	21.0053	21.0035		85	0.024		k= 2.20	1/V dV/dx1	1//	1/(m _f -m _e)	$-1/(m_{f}-m_{e})$	-1100	$-(T_W - T_{ref,W})$	$-(T_{W}-T_{ref})$	β_{w} - β_{i}	$1/\rho_o$	
ABC Co. 1234 1234 1234 21 21 21 21	Average 22.587 22.804 22.854 22.867 22.906	- Moleci	Read	_	186.2984	186.2677 186.3000	186.2805	Thermal	Delivered		0.07946496	0.07947469 0.07946292	0.07946486	0.07947260	0.0794680	0.0794644	99	0.021		k=	e	n³]	[6]	[6]	[g/m ³]			5	(g/m ³]	
Name of Company: NIST Seal Number: Serial Number: Serial Number: Nominal Volume of Vessel: Nominal Vol per Scale Div: Date Calibrated:	Water Temperature Corrected #3 [C] 22.594 22.862 22.862 22.862 22.962		t Dry Corrected		107.1846	107.1846 107.1846	107.1846		Contained	_ ۳		0.07951435			0.0795067 0	5	85	0.024		Estimation of Uncertainty	Value	[m ³]	186.42 [kg]	107.18 [kg]	1000 [kg/m ³	2.0E-04 [1/C]	4.8E-05 [1/C]	22.8 [C]	1.18 [kg/m ³]	
Nam NIST Nominal Volt	W Corrected #6 22.580 22.859 22.859 22.811 22.811	delet.	weight Dry Read Co	[kg]	107.1097	107.1097 107.1097	107.1097	Ref Temn		15.56										Estimation o	x,	Ч	m,	m e	ρ_o	β	β	T_W	$ ho_{air}$	7

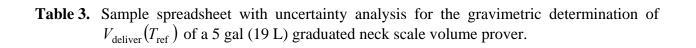


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21 gal

-2.08600E-02 [C] 8.892500E-01 [1/C] 10/27/2005 6.66000E-02 [C] 1.002220E+00 [1/C] 10/27/2005		Neck Scale Callbration g calculated correction	[div]	6.6 0.0		0.2 -20.1	2.6	20.0	intercept	-0.10	05 -1.636E-06 [m ²]		•	*	*		*		*	-10.0 0.0 10.0 20.0 30.0	Neck Scale Keauing (ulv)	maker: Can Co.	cale: -20	cale: 20	levels: across bottom	valve: none	new: none	e (s): 10
T#S Coef., de; 2.03800E-02 T#S Coef., de; -2.03800E-01 T#S Coef., de; -0.2772005 T#S Coef., eg: -6.560000E-02 T#S Coef., eg: -10.2772056 T#S Coef., eg: -10.022054-00 Cal Date: 10.022054-00	Air Density Jaeger & Davis [kg/m ³] 1.16790 1.16827 1.18554 1.18147	Reading	[div]	0.4-	0.0	0.1 •	5.6		el		1.125E-06 1.005 9.419E-07 1.647E-05	0:30	0.20				Correc	-0.50 -	-0.50	-30.0 -20.0	en l	ш.	min scale	max scale	, je	M	old / new:	drain time (s)
[c] [1/c] [c]	Rel. Humidity Read [%] 43.8 44.0 69.0 65.8 65.8 65.0	Uncorrected Prover Volume	Delivered		0.018930	0.018938 0.018935	Water	Density	Patterson & Morris	[m/gx]	999.015 997.583			corrected sity Corrected					1/V dV/ dx ; u(x ;) [x 10 ⁻⁶]	0.67	1158.82	1158.82	4.00	56.70	25.81	37.11	4.00	561.00
 -3.520000E-02 [C] -3.520000E-02 [C] -3.520000E-01 [I/C] -1.692000E-01 [C] -1.692000E-01 [C] 1.007748E+00 [1/C] 1.007748E+00 [1/C] 	Barometric Pressure Read (Press) [Pa] (100.80 100.80 (101.10 101.100 (101.10 101.100 (101.10 101.100 (101.10 101.100	Uncorrected	Contained		0.018930	0.018945 0.018943	0.4401.0.0	Temperature	Ş	[c]	15.560 22.818			Averages, Thermai Expansion Corrected Averages, Therm. Exp. & Viscosity Corrected	x 10 ^{.6} 1	certainty [%]		Kuyatt	1/V dV/ dX i	0.8	34.0	-34.0	-2.0	-7.5	-5.1	6.1	2.0	23.7
T#4 Coef., b ₆ : T#4 Coef., b ₁ : Cal Date: Cal Date: T#6 Coef., c _i : T#6 Coef., c _i : Cal Date: Cal Date:	Barometr Read [kPa] 100.80 101.10 101.10 101.10	Scale Reading	Corrected	-0.000066	0000000000	-0.000002 0.000002		∆ x / g _x		0.45	1.22 0.31	1.33 0.65	000	Averages, In Averages. The	Reneatability fx 10 ⁶	Expanded Uncertainty [%]		95% confidence, Taylor & Kuyatt	$u(x_{ij} \text{ for } k=1$	[m³]	[kg]	[kg]	[kg/m ³]	[1/C]	[1/C]	[<u>C]</u>	[kg/m ³]	
60 [kg] -00 [1kg] -07 [1kg ²] 305	Average 25.956 21.990 22.404 23.174	Scale	Read	[div]	0.0	-0.1 0.1		Delivered	[in ³]	1154.78	1154.57 1154.82	1155.26 1155.08	11E1 00	1154.85	235	0.067		95% confide	n(x ⁱ⁾	4.1E-06 [m ³]	6.4E-04 [kg]	6.4E-04 [kg]	2.0E-03 [kg/m ³]	3.3E-07 [1/C]	7.0E-07	4.0E-02 [C]	2.0E-03 [kg/m ³]	
1.0010E+ 2.9329E 10/4/20	Air Temperature Corrected #5 [C] 25.969 21.980 21.980 23.178 23.178	Weight Drained	Corrected	5.0535 5.0535	5.0502	5.0510 5.0518	olume	ntained	- L	1155.39	1155.13 1155.22	1155.72 1155.58	4466 44	1	211	0.060		= 4	Value of 1/V dV/ dx i	0 [1/m ³]	0.05 [1/kg]	-0.05 [1/kg]	-1E-03 [m ³ /kg]	3 [C]	-7.3 [C]	[1/C]	[m ³ /kg]	
Scale Capacity: Scale Coeficient, a ₁ : Scale Coeficient, a ₂ : Cal Date:	Corrected #4 25.948 25.856 22.001 22.408 23.170	Weight	Read		5.0452	5.0460 5.0467	ected Prover V	Delivered	[gal]	4.9990	4.9981 4.9992	5.0011 5.0003	4 0002	4.9994	235	0.067		$V_{\rm off} = 4$			0.05	-0.05	-1E-03	-22.8 [C]	-7.3	2E-04 [1/C]	1E-03	
gallons cubic inches	Water Density Patterson & Montrie [Kg/m ³] 997.519 997.619 997.612 997.632	ght Full	Corrected	[Kg] 23.8495 24.0047	24.0247	23.9195 23.9209	Thermal Expansion Corrected Prover Volume	Contained	- I	5.0017	5.0006 5.0010	5.0031 5.0025	5 0010	0.00.0	211	0.060		= 2.78	1/V dV/dX _i	1//	1/(m _f -m _e)	-1/(m _f -m _e)	-1/Po	$-(T_W - T_{ref,W})$	$-(T_W-T_{ref})$	β_{W} - β_{t}	$1/\rho_o$	
ABC Co. 1234 1234 5 5 1 10/5/2005	e Average 23.050 23.085 23.085 22.694 22.607	ē	Read		24.UUU5 23.8890	23.8953 23.8967	Thermal	Deli		0.01892343	0.01892000	0.01893134 0.01893833	0.0100264	0.0189247	235	0.067		<i>k</i> =	ue	m_]	[kg]	[kg]	1000 [kg/m ³]	1/C]	1/C]	[]	1.18 [kg/m ³]	
Name of Company: NIST Seal Number: Serial Number: Serial Vumber: Nominal Volume of Vessel: Nominal Vol per Scale Div: Date Calibrated:	Water Temperature Corrected #3 [C] 23.046 23.081 22.644 22.691 22.591	tDry	Corrected		5.0436	5.0436 5.0436		Contained	[m]	0.01893345	0.01892919 0.01893073	0.01893884 0.01893657	0.0100020	0000010.0	211	090.0		f Uncertainty	Value	[m	23.93 [kg]	5.04 [kg]	1000 [2.0E-04 [1/C]	4.8E-05 [1/C]	22.8 [C]	1.18 [
Nam NIST S Nominal Volt Nominal Vol	W Corrected #5 23.054 23.089 22.662 22.618 22.618	Weight Dry	Read	5.0385 5.0385	5.0385	5.0385 5.0385	Ref. Temp.	[0]	15.56				1					Estimation of Uncertainty	x,	4	m,	m _e	ρ_o	β_w	ß	τ_w	$ ho_{ m air}$	Λ



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5 gal

-2.008005-02 [C] 9.9925005-01 [1/C] 102272005 6.690005-02 [C] 1.0022205+00 [1/C] 1.022205+00 [1/C]				maker: Can Co.	min scale: -20	max scale: 20	levels: across bottom	valve: none	old / new: none drain time (s): 10
T#5 Coef, do: - T#5 Coef, d; 9 Cal Date: T#3 Coef, e, -9 T#3 Coef, e, 1 T#3 Coef, e, 1	Air Density [kg/m ³] 1.17249 1.17249 1.17392 1.17392 1.17348 1.17348 1.17348 1.17348 1.17348 1.17348 1.17348 1.1756-06 9.057E-07 9.057E-07								ġ
[1/C] [1/C] [1/C]	e	1/V c/V/ c/x ; u(x _i) [x 10 ⁻⁶]	0.00 1159.01	1159.01	4.00	65.59	39.53	37.11	4.00 559.08
	Barometric Pressure Rei Rei [k=a] [Pa] [Pa] [%] [k=a] [Pa] [%] [%] [100.80 100.800 26.5 [%] 100.80 101.100 26.5 [%] 101.10 101.100 33.2 26.5 101.10 101.100 33.2 26.4 101.10 101.100 33.2 26.4 101.10 101.100 33.2 26.4 011.10 101.100 33.2 26.4 011.10 0.18956 0.018949 26.018949 0.000000 0.018957 0.018956 0.018956 0.000000 0.018957 0.018956 0.018956 0.000000 0.018957 0.018956 0.018956 0.000000 0.018957 0.018956 0.018956 0.000000 0.018957 0.018956 0.018956 0.000000 0.018957 0.018956 0.018956 0.0000000 0.018957 0.018956	1/V dV/ dX ji	0.0 34.0	-34.0	-2.0	-8.1	-6.3	6.1	2.0 23.6
T#4 Coef., b ₆ : T#4 Coef., b ₁ : Cal Date: T#6 Coef., c ₆ : T#6 Coef., c ₁ : Cal Date: Cal Date:	Average Barometric Pressure Average Read [Pa] 25.464 100.80 100,800 25.730 101.10 101,100 25.731 101.10 101,100 25.730 101.10 101,100 25.731 101.10 101,100 25.731 101.10 101,100 25.730 101.10 101,100 25.731 101.10 101,100 25.730 101.10 101,100 25.774 101.10 101,100 25.730 0.0100000 0.018955 0.0 0.000000 0.018955 0.0 0.000000 0.018955 0.0 0.000000 0.018955 1155.84 1.11 1.07 1155.82 0.57 74.65 1155.92 0.57 75.661 1155.92 0.57 75.661 1155.84 Averages. Thermal Expan 1155.83 0.57 24.52 0.014 Expande	$u(x_{ij} \text{ for } k=1$	m³] kal	[g]	kg/m ³]	1/C]	1/C]	C	kg/m³]
60 [kg] +00 [1/kg] -07 [1/kg ¹] 205	re Average 25.464 25.545 25.778 25.778 25.774 25.774 25.774 25.774 25.774 25.578 25.774 25.578 25.774 25.578 25.774 25.578 26.778 27.7787 27.778 27.7777777777	u(x _{i)} 1	0.0E+00 [m ³] 6.4E-04 [ka]	6.4E-04 [kg]	2.0E-03 [kg/m ³]	3.3E-07 [1/C]	7.0E-07 [1/C]	4.0E-02 [C]	2.0E-03 [kg/m ³]
1.0010E 2.9329E 10/4/2	mperatumer	Value of 1/V dV/ dX_i	0 [1/m ³] 0.05 [1/ka]	-0.05 [1/kg]	-1E-03 [m ³ /kg]	[0]	-9.0 [C]	[1/C]	[m³/kg]
Scale Capacity: Scale Coefficient, a; Scale Coefficient, a; Cal Date:	W Corrected #4		0.05	-0.05	-1E-03	-24.5 [C]		2E-04 [1/C]	1E-03
gallons cubic inches	Rage Patterio & Months Patterio & Months (RyUm ³) Corrected #4 Ail Te corrected #4 050 997.117 256.452 2 387 997.117 256.452 2 387 997.117 256.452 2 387 997.1194 256.452 2 387 997.1194 256.737 2 387 987.1199 257.73 2 387 25.1324 9.252.03 9 0005 28.1346 9.252.03 9 0005 28.1346 9.252.03 9 0005 28.1346 9.252.03 9 0005 28.1346 9.252.03 9 0005 28.1365 9.252.03 9 0005 28.1366 9.252.03 9 0005 28.1366 9.252.03 9 0005 28.1366 9.252.03 9 0005 28.1366 9.252.03 9 0005 28.1366 9.252.04 11 </td <td>1/V dV/ dX_i</td> <td>1/V 1/(m,-m)</td> <td>-1/(m_f-m_e)</td> <td>-1/Po</td> <td>$-(T_W-T_{ref,W})$</td> <td>$-(T_W-T_{ref})$</td> <td>β_{W}-β_{t}</td> <td>1<i>I</i>Do</td>	1/V dV/ dX _i	1/V 1/(m,-m)	-1/(m _f -m _e)	-1/Po	$-(T_W-T_{ref,W})$	$-(T_W-T_{ref})$	β_{W} - β_{t}	1 <i>I</i> Do
ABC Co. 1234 1234 5 5 10/5/2005	Ave 25 24 24 24 28 38 38 1 0 0 0 0 0 0 0 0 0	ne	[m ³] [ka]	[kg]	[kg/m ³]	[1/C]	[1/C]	[<u>C</u>]	[kg/m ³]
Name of Company: NIST Seal Number: Serial Number: Serial Volume of Vesei: Nominal Vol per Scale Div Date Calibrated:	Mater Temperature Corrected #5 Water Temperature 256.042 256.058 24.482 24.485 24.482 24.485 24.400 24.369 24.400 24.369 24.400 24.369 24.400 24.369 24.400 24.369 24.400 24.369 9.24540 9.2647 9.24540 9.2647 9.24540 9.2647 9.24540 9.2647 9.24540 9.2647 9.24540 9.2647 9.247 9.2647 9.247 9.2647 9.247 9.2647 9.247 9.2647 9.247 9.2647 9.247 9.2647 9.247 9.2647 9.247 9.2647 9.2647 9.2647 9.2647 9.2647 9.2647 9.2647 9.2647 9.2647 9.2647 9.2647 9.2647 <td>Value</td> <td> 28.14 </td> <td></td> <td>1000</td> <td>2.0E-04 </td> <td>4.8E-05</td> <td>24.5</td> <td>1.17 </td>	Value	 28.14		1000	2.0E-04	4.8E-05	24.5	1.17
Narr NIS: Nominal Vol Nominal Vol D	Water Water Corrected #5 Corr 25.042 2 24.162 2 24.162 2 24.160 2 24.160 2 24.160 2 24.400 9 24.540 9 9.245	x_i	ų,	m,	ρ_o	β_w	ß	τ_w	$\rho_{\rm air}$ V

Table 4. Sample spreadsheet with uncertainty analysis for the gravimetric determination of $V_{\text{deliver}}(T_{\text{ref}})$ of a 5 gal (19 L) slicker plate volume prover.

5 gal slicker

7.2 Uncertainty of the Volume Transfer Method

In this section, we will analyze the uncertainty of the volume transfer method using the example of the calibration of a 450 gal (1700 L) prover with a 100 gal (378 L) working standard prover (transferred 4 times) and a 50 gal (189 L) working standard (transferred once). The basis equation for the uncertainty analysis is equation 10' with the water density approximation of equation 20.

The component uncertainties, and their types, are:

- $u(h_{t}), u(h_{A}), u(h_{B})$ are one fourth of the smallest division of the neck scale of the prover under test and of the two working standard provers (Type B),
 - $u(V_{\rm A}), u(V_{\rm B})$ are based on the calibration records and uncertainty of the calibration process for the working standard volume provers (Type B),
- $u(\rho_{\rm t}), u(\rho_{\rm A}), u(\rho_{\rm B}), u(\beta_{\rm w})$ are from the water density equation [Patterson and Morris, 1994] and uncertainties in the measurement of temperature (Type B),
 - $u(T_t), u(T_A), u(T_B)$ are based on calibration records, the uncertainty of the temperature calibration process within the Fluid Metrology Group, and the normal variation of temperature within the volume prover (Type B),
 - $u(\beta_t)$ was provided by the NBS Crystallography Section (Type B),
 - $u(\rho_0), u(\beta_w)$ are based on the water density equation [Patterson and Morris, 1994] (Type B),
 - u(v) is the uncertainty due to viscosity effects on delivered volume (Type B), and
 - $\sigma_{\rm V}^2$ is the variance of replicated determinations of prover volume (Type A).

Tables 5 and 6 show sample calculations for the volume transfer method. Table 5 shows the summation of working standard volumes for one of the five repeats. Table 6 summarizes the results for all five repeats, including averaging, statistical calculations, and the uncertainty calculation. Five values for the contained volume are calculated even though only one volume transfer was done with the prover dry: the difference between contained and delivered volume from an initial, dry run is added to the subsequent delivered volume to obtain the final four contained volumes.

Differentiation of equation 10' and elimination of terms that are small compared to unity leads to the normalized sensitivity coefficients listed in Table 6. The coefficients of thermal expansion for all three provers were assumed to be equal (β_t) in this uncertainty analysis. For the example in Table 6, a simplified uncertainty analysis that considered only the components due to V_A , V_B , h_t , and the test repeatability would give a good approximation (0.033 % versus 0.035 %). However, in cases with larger temperature uncertainty, the temperature components will dominate and they should not be ignored.

Explanatory notes for Tables 5 and 6 are given below.

- A) Volume prover identification, size, volume per smallest scale division.
- B) Temperature sensor calibration coefficients.
- C) Water temperatures for each of the volume working standards before transfer to volume prover under test, used to calculate water density. Last row is the temperature of the prover under test when full.
- D) Water densities for working standards and prover under test.
- E) Volume, reference temperature, etc. for the working standard provers.
- F) Neck scale readings for the working standards and the prover under test.
- G) Volumes and masses for the working standards and the total transferred to the prover under test.
- H) A single volume determination result for the prover under test at test temperature and at the reference temperature.
- I) Results for five individual volume determinations for the prover under test.
- J) The average for the repeated measurements, their standard deviation, and the uncertainty of the calibration (based on calculations shown below).
- K) Coverage factor and effective degrees of freedom.
- L) Values of variables used for the uncertainty analysis.
- M) Analytical expressions and values for the sensitivity coefficients, and the magnitude of the uncertainty for each uncertainty component.
- N) Uncertainty contribution (in parts in 10^6) for each uncertainty component.

-	•	

		=1 Volume per Div. Iin ³ /div 1			5 2.000	5 2.000	0 1.000														
		Uncertainty, k=1 [+m ³]	0.00003295	0.00003295	0.00003295	0.00003295	0.00002660														
	sures	Therm. Exp. Coef. [1/°C]	4.8E-05	4.8E-05	4.8E-05	4.8E-05	4.8E-05														
ci Tice B	Standard Test Measures	E Ref. Temp.	15.56	15.56	15.56	15.56	15.56		Vessel	Therm. Exp. Coef.		[1/°C]	4.8E-05								
0.000E+00 [C] 1.000E+00 [1/C] 5/10/2004	N.	Ref. Volume Im ³ 1	0.37850714	0.37850714	0.37850714	0.37850714	0.18919155		Water Ref. Properties	Density	Patterson & Morris	[kg/m ³]	999.015					ef. Temp.	Delivered	[r]	1700.46
T#6 Coef., cg: T#6 Coef., c-; Cal Date:		Cal. Date	6/23/2004	6/23/2004	6/23/2004	6/23/2004	6/28/2004		Water Re	Temperature		[.c]	15.56				Final	Vessel Volume @ Ref. Temp.	Delivered	[gal]	449.214
Co. 234 1.7 [m ³] 5.04 [m ³] 004		NIST Prop. No.	NBS 152550	NBS 152550	NBS 152550	NBS 152550	NBS 62069	Final	livered	Mass	[kg]	37	375.6370	377.4845	377.4560	188.7593	1694.9845	Vesse	Delivered	[m]	1.70046
ABC 1 1 2.500 7/11/2	Water Density	Patterson & Morris Ikn/m ³ 1	996°890	996.877	996.932	996.903	996.787	996.888	Water Delivered	Volume	رت [m]	0.37663902	0.37663246	0.37846781	0.37844815	0.18927349	Final		H Delivered	D 0	1701.28
Name of Company: NIST Seal Number: Serial Number: Nominal Volume of Vessel: Nominal Vol per Scale Div: Date Calibrated:	Water Temperature	Corrected Ave.	25.600		C 25.440	25.550	25.990	25.610	Scale Reading	Corrected	[m ³]	F) -0.00186812	-0.00187468	-0.00003933	-0.00005899	0.00008194	-0.00100000	Vessel Volume @ Temp.	_	[gal]	449.430
	Ň	Read @ #6	25.600	25.650	25.440	25.550	25.990	25.610		Read	[div]	-57.0	-57.2	-1.2	-1.8	5.0	-4.0		Delivered	[m°]	1.70128

Table 5. Sample of the worksheet that totalizes the mass for the volume transfer method, 4×100 $gal + 1 \times 50 gal \approx 450 gal$. See text for key.

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		Kin. Visc.	CRC & Kell	[m ² /s]	1.125E-06	8.829E-07																				
	Water	Density	Patterson & Morris	[kg/m ³]	999.015	996.869			corrected	y Corrected					1351.64	0.93	59.47	244.86	6010.76	849.21	30.42	1927.46	32.15	0.01	4.00	305.64
Ref. Temp. [C] 15.56		Temperature		[c]	15.560	25.680			Averages, Thermal Expansion Corrected	Averages, Therm. Exp. & Viscosity Corrected	Repeatability [x 10 ⁻⁶]	Expanded Uncertainty [%]	k Kuyatt	1/V ////// dx, [x 10 ⁶]	37	-	8	16	N 78	29	9	44	9	0	2	-17
		DX/Sx		1.45	0.08	0.30	0.67	1.16	Averages	Averages	Repeatab	Expander	95% confidence, Taylor & Kuyatt	dx, for k=1	6.25E-05 [m ³]	1.64E-06 [m ³]	3.28E-06 [m ³]	2.66E-05 [m ³]	3.29E-05 [m ³]	2.0E-01 [C]	2.0E-01 [C]	2.0E-01 [C]	7.0E-07 [1/C]	2.0E-06 [1/C]	2.0E-03 [kg/m ³]	
# of Tranfers NA NB		Contained Delivered	[1]	1700.86 1700.46	-	-		1/01.40 1/01.00	1701.16 1700.76	1700.71	121 121	0.035 0.035	V ₆₁₁ = 12	Value	5.88E-01 [1/m ³]	5.88E-01 [1/m ³]	2.35E+00 [1/m ³]	5.88E-01 [1/m ³]	2.35E+00 [1/m ³]	1.46E-04 [1/°C]	2.76E-05 [1/°C]	2.20E-04 [1/°C]	8.10E+00 [°C]	3.89E-02 [°C]	1E-03 [m ³ /kg]	
ی ۲	Thermal Expansion Corrected Prover Volume	Delivered	[gal]	449.214	T 449.289	L 449.277	449.330	449.357	T 449.294	449.280	121	0.035	B (K)	1/V aV/ax,	1M _t	N _B N	NAN	N _B Nt	NAN,	$(B_i + B_{ii})N_i$	$[N_B V_B (\beta + \beta) N_i$	$[N_A V_A (\beta_A + \beta_A) N_A$	$(N_A V_A (-T_t + T_{ref} + T_A - T_{CA}) + N_B V_B (-T_t + T_{ref} + T_B - T_{CB}))N_t$	$(N_AV_A(T_A-T_t)+N_BV_B(T_B-T_t))N_t$	-11Po	
ABC Co. 1234 1.700 [m ³] 2.50E-04 [m ³]	Thermal E	Contained		449.214	449.289	449.277	449.330	449.30/	449.2936		121	0.035	k= 2.18	Value	0.00 [m ³]	0.00 [m ³]	0.00 [m ³]	ز [m³]	i [m³]	[c]	[c]	[C]	_	[1/C]	1000 [kg/m ³]	
Name of Company: NIST Seal Number: Serial Number: Serial Number: Nominal Volume of Vessel: Nominal Vol per Scale Div: Date Calibrated:		Delivered	[m ³]	1.70046	1.70074	1.70070	1.70090	1./0100	1.70076	1.70071	121	0.035	Estimation of Uncertainty	\$	0.0	0.0	0.0	0.1893 [m ³]	0.3766 [m ³]	25.68 [°C]	25.91 [°C]	25.70 [°C]	4.8E-05 [1/C	2.0E-04 [1/C	1000	
Nam NIST Nominal Volt Nominal Vol		Contained	<u> </u>	1.70086	1.70114	1.70110	1.70130	1./0140	1.70116		121	0.035	Estimation	×	Ĕ	h _B	Å	< B	>	ŗ	T _B	τ _A	$eta_{ m c}$ (prover)	$eta_{ m w}$ (water)	Po	Л

Table 6. Summary of the five repeated measurements, averages, and sample uncertainty analysis for the volume transfer method. See text for key.

8. References

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Appendix A. Calibration of Weigh Scales

The traceability of liquid volume measurements to the national standards of mass is through a 65 kg set of weights calibrated by the NIST Acoustics, Mass, and Vibrations Group. Weights from the 65 kg set are used to calibrate the 60 kg weigh scale. Weights from the 65 kg set and the 60 kg weigh scale are used to calibrate a set of 45 kg weights, which in turn, are used to calibrate the 600 kg weigh scale. The process for calibrating the 45 kg weights is given below. Following that are the steps necessary for calibrating the 60 kg and 600 kg weigh scales with the reference masses.

Calibration of the 45 kg Reference Masses

- 1. Measure the ambient air temperature, the barometric pressure, and the relative humidity. Calculate the air density, ρ_{air} , using equation 1.
- 2. Set the 60 kg weigh scale to zero.
- 3. Load 45 kg mass, m_{std} , from the 65 kg weight set on the weigh scale platform and record the reading as O_1 . The reading of the weigh scale is the difference of the downward force due to gravity and the upward force due to air buoyancy.

$$O_1 g = m_{\rm std} g - V_{\rm std} \rho_{\rm air} g = m_{\rm std} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm std}} \right) g \tag{1A}$$

where:

g is the local acceleration due to gravity,

 $V_{\rm std}$ is the volume of $m_{\rm std}$, and

 $\rho_{\rm std}$ is the density of the metal from which $m_{\rm std}$ is made.

Since g appears in all terms, we have, by dividing by g

$$O_1 = m_{\rm std} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm std}} \right) \tag{2A}$$

The double substitution weighing design requires three more weighings and three more equations, analogous to equation 1A, to describe them. Since g is a common factor in all terms of all three equations, the equations are written the form analogous to equation 2A where division by g is understood.

4. Remove m_{std} , reset the weigh scale to zero, load a 45 kg weight to be calibrated, m_{45} , and record the reading as O_2 ,

$$O_2 = m_{45} \left(1 - \frac{\rho_{\text{air}}}{\rho_{45}} \right)$$

where ρ_{45} is the density of the metal from which the 45 kg weights are made,

5. Add a 0.2 kg sensitivity weight, m_s , and record the reading as O_3 ,

$$O_3 = O_2 + m_{\rm s} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm s}} \right)$$

where $\rho_{\rm s}$ is the density of the metal from which the sensitivity weight is made,

6. Remove m_{45} , reset the weigh scale to zero, load m_{std} , and record the reading for m_{std} and m_s as O_4 ,

$$O_4 = O_1 + m_{\rm s} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm s}} \right)$$

By adding and subtracting the last four equations, we obtain

$$\frac{(O_2 + O_3 - O_1 - O_4)}{2} \times \frac{m_{\rm s} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm s}}\right)}{(O_3 - O_2)} = m_{45} \left(1 - \frac{\rho_{\rm air}}{\rho_{45}}\right) - m_{\rm std} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm std}}\right)$$

where the term on the left hand side has been multiplied by 1 in order to include the measurements involving the sensitivity weight, i.e.,

$$1 = \frac{m_{\rm s} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm s}}\right)}{\left(O_3 - O_2\right)}$$

The calibration equation for the 45 kg weights is obtained by solving for m_{45} ,

$$m_{45} = \frac{\frac{(O_2 + O_3 - O_1 - O_4)}{2(O_3 - O_2)}m_s\left(1 - \frac{\rho_{\text{air}}}{\rho_s}\right) + m_{\text{std}}\left(1 - \frac{\rho_{\text{air}}}{\rho_{\text{std}}}\right)}{\left(1 - \frac{\rho_{\text{air}}}{\rho_{45}}\right)}$$

Calibration of the 60 kg and 600 kg Weigh Scales

The 60 kg weigh scale is calibrated by placing weights from the 65 kg set on the platform in 5 kg increments for the up-loading cycle. The down-loading increments are done by removing 10 kg and restoring 5 kg per step in order to nullify the effects of hysteresis.

The 600 kg weigh scale is calibrated by placing 45 kg weights on the platform, one weight per increment for the up-loading cycle. The down-loading cycle is done by removing 90 kg and restoring 45 kg per increment in order to nullify the effects of hysteresis.

The calibration process for a weigh scale generates a series of weigh scale readings, O, for a series of calibrated mass values, m. The calibration equation for either weigh scale is obtained by fitting the mass values, adjusted for air buoyancy, as a function of the weigh scale readings,

$$m\left(1-\frac{\rho_{\rm air}}{\rho_{\rm m}}\right) = A + BO + CO^2 + \dots$$

Thus the indicated mass, m_{ind} , (not air buoyancy adjusted) for an object being weighed on a calibrated weigh scale is

$$m_{\rm ind} = A + BO + CO^2 + \dots \tag{3A}$$

The step-by-step procedure is:

- 1. Measure and record the initial room air temperature, atmospheric pressure, and relative humidity.
- 2. Place the first reference mass on the weigh scale near the center of the weigh scale pan. (The order in which the reference masses are applied to the scale is indicated on the data collection worksheet.) Wait approximately 10 seconds for stability of the mass indicated by the weigh scale and record the indicated mass.
- 3. Add the subsequent reference masses, one by one, near the center of the weigh scale, recording the readings of the weigh scale at each step.
- 4. Measure and record the final room air temperature, atmospheric pressure, and relative humidity.
- 5. Process the calibration data. Apply buoyancy corrections (using equation 1 for air density) to calculate the apparent masses for the reference masses. Perform a 2nd order least squares fit to obtain a polynomial that calibrates the weigh scale readings. This polynomial is applied to the readings of the weigh scale gathered during calibration of the prover volume.

Appendix B. Derivation of Equations for Gravimetric Method for Neck Scale Provers

In the gravimetric procedures for neck scale volume provers listed in Section 4.1.1, the weigh scales readings for the dry volume prover, O_e , the filled volume prover, O_f , and the drained volume prover, O_{ed} , are recorded in steps 6, 11, and 14, respectively. These readings are converted to indicated masses m_e , m_f , and m_d in steps 16-18 via equation 3A.

The indicated mass for the dry measure is

$$m_{\rm e} = M_{\rm e} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm e}} \right) \tag{1B}$$

where:

 $M_{\rm e}$ is the mass of the dry measure,

 $ho_{\rm air}$ is the density of the air, and

 $\rho_{\rm e}$ is the density of the dry measure.

For the measure filled with water up to the zero reference mark, the indicated mass is

$$m_{\rm f} = M_{\rm e} \left(1 - \frac{\rho_{\rm air}}{\rho_{\rm e}} \right) + M_{\rm w, \, contain} \left(1 - \frac{\rho_{\rm air}}{\rho(T_{\rm w})} \right) = m_{\rm e} + M_{\rm w, \, contain} \left(1 - \frac{\rho_{\rm air}}{\rho(T_{\rm w})} \right)$$
(2B)

where :

 $M_{\rm w.\,contain}$ is the mass of the contained water and

 $\rho(T_{\rm w})$ is the density of the water at temperature $T_{\rm w}$.

Solving equation 2B for $M_{\rm w, \, contain}$,

$$M_{\rm w,contain} = \frac{(m_{\rm f} - m_{\rm e})\rho(T_{\rm w})}{\rho(T_{\rm w}) - \rho_{\rm air}}$$
(3B)

From the definition of density,

$$V_{\text{contain}}(T_{\text{w}}) = \frac{M_{\text{w,contain}}}{\rho(T_{\text{w}})} = \frac{m_{\text{f}} - m_{\text{e}}}{\rho(T_{\text{w}}) - \rho_{\text{air}}} - h$$
(4B)

where h is the deviation of the meniscus from the zero mark on the neck scale, in volume units. The indicated mass for the drained measure is

$$m_{\rm d} = m_{\rm e} + M_{\rm w, residual} \left(1 - \frac{\rho_{\rm air}}{\rho(T_{\rm w})} \right)$$
(5B)

where $M_{\rm w, residual}$ is the water remaining in the measure after the valve is closed at the end of the specified drain time.

For the measure filled with water up to the zero reference mark,

$$m_{\rm f} = m_{\rm e} + M_{\rm w,residual} \left(1 - \frac{\rho_{\rm air}}{\rho(T_{\rm w})} \right) + M_{\rm w,deliver} \left(1 - \frac{\rho_{\rm air}}{\rho(T_{\rm w})} \right) = m_{\rm d} + M_{\rm w,deliver} \left(1 - \frac{\rho_{\rm air}}{\rho(T_{\rm w})} \right)$$
(6B)

Solving for $M_{\rm w, \, deliver}$ and combining with the definition of density, we obtain

$$V_{\text{deliver}}(T_{\text{w}}) = \frac{m_{\text{f}} - m_{\text{d}}}{\rho(T_{\text{w}}) - \rho_{\text{air}}} - h.$$
(7B)

Appendix C. Derivation of Equation for the Volume Transfer Method

The transfer method of volume calibration is accomplished by emptying a known volume of water from a working standard measure into the measure to be calibrated. For the present purpose, it is assumed that:

- 1. The working standard is a neck-scale measure.
- 2. The delivered volume of the working standard, V_s , has been determined by the gravimetric

method at $T_{w,c}$ via equation 5.

3. The measure under test is a neck-scale measure of the same nominal capacity as the working standard so that only one emptying of the working standard is required.

The volume of the water in the working standard is

$$(V_{s} + h_{s})[1 + \beta_{s}(T_{w,s} - T_{ref,s})] = \frac{m}{\rho(T_{w,s})}$$
(1C)

where:

- $V_{\rm s}$ is the volume of the working standard filled up to the proximity of the zero reference mark,
- $h_{\rm s}$ is the deviation from zero of the neck scale reading of the working standard, in volume units, with the appropriate algebraic sign applied,
- $\beta_{\rm s}$ is the volumetric thermal expansion coefficient of the working standard,
- $T_{\rm w,s}$ is the temperature of the water in the working standard,
- $T_{\rm ref.s}$ is the temperature at which the working standard was calibrated,
 - m is the mass of the water transferred, and

 $\rho(T_{w.s})$ is the density of the water in the working standard.

After the transfer, the volume of the water in the measure under test, $V_{\rm t}$, is

$$\left(V_{t}+h_{t}\right)=\frac{m}{\rho_{w,t}}$$
(2C)

where:

 $h_{\rm t}$ is the neck scale reading of the measure under test, in volume units, with the appropriate algebraic sign applied,

 $T_{\rm w,t}$ is the temperature of the water in the measure under test, and

 $\rho(T_{\rm w,t})$ is the density of the water in the working standard.

Since mass is conserved in the transfer process, equations 1C and 2C are solved for m and the resulting expressions are equated and solved for V_t .

$$V_{t}(T_{w,t}) = \frac{\rho(T_{w,s})(V_{s} + h_{s})[1 + \beta_{s}(T_{w,s} - T_{ref,s})]}{\rho(T_{w,t})} - h_{t} .$$
(3C)

This expression will yield contained volume at $T_{w,t}$ if the inside walls of the measure under test were dry at the outset of the calibration, or delivered volume at $T_{w,t}$ if the inside walls of the prover were pre-wetted at the outset of the calibration.

REPORT OF CALIBRATION

FOR

A ONE HUNDRED (100) GALLON VESSEL (Graduated Neck Type)

April 28, 2005

Manufacturer: Test Measure Co. Gaithersburg, MD NIST Seal Number: 1234 Material: Stainless Steel Maker Number: ABC123

submitted by

Test Measure Co. 123 West St. Gaithersburg, MD 20877

(Reference: Purchase Order Number ABC123, April 1, 2005)

The internal volume of the vessel described above has been determined by the gravimetric method [1]. The gravimetric method requires weighing the vessel dry and empty and reweighing it when filled with a fluid of known density. The internal or contained volume was determined in this way and the value is given in Table 1 using the requested units. The fluid used was water and the vessel was leveled before determining the volume.

To determine the delivered volume, the contained volume is poured from the vessel by opening the valve at the bottom of the vessel. When this flow finishes, the valve is held open for 30 seconds to complete the drain procedure. Subsequent re-weighing completes the gravimetric procedure and enables calculation of the delivered volume, also given in Table 1. Both the contained and delivered volumes are given for the scale reading of zero (0) and have been corrected for the reference temperature of 15.56 °C (60 °F) assuming a volumetric coefficient of expansion of 0.0000477 per °C (0.0000265 per °F).

^[1] Bean, V. E., Espina, P. I., Wright, J. D., Houser, J. F., Sheckels, S. D., and Johnson, A. N., "NIST Calibration Services for Liquid Volume", NIST Special Publication 250-72, National Institute of Standards and Technology, November 25, 2009.

REPORT OF CALIBRATION Test Measure Co.

	Volume Contained	Volume Delivered
gal at 60 °F	99.9924	99.9656
in ³ at 60 °F	23098.25	23092.07

Table 1. Contained and delivered volumes for the tested vessel for a scale reading [2] of zero.

The expanded uncertainty in the measured volume is ± 0.011 % and the repeatability of the 5 measurements was 39 parts in 10^6 . The uncertainty was calculated according to References [1] and [3] with a 95 % confidence level [4] and is traceable to NIST mass, temperature, pressure, and humidity standards, and a NIST water density determination.

Below are pictures of the identification plate of the calibrated vessel and its drain valve. Enclosed at the end of this report is a spreadsheet outlining all the measurements made during this calibration and the computed results.

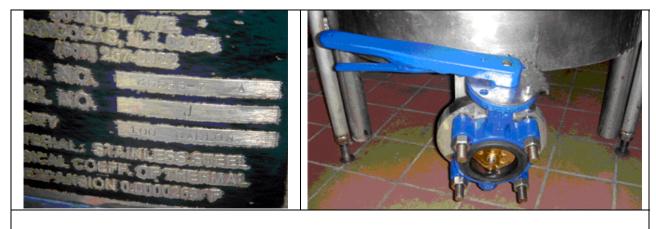


Figure 1. Photographs of the identification plate of the calibrated prover and its drain valve.

^[2] The scale reading is determined by the intersection of the horizontal plane, tangent to the bottom of the meniscus on the gauge tube. For this prover, the neck scale range was from -225 to +200 and each division is labeled by the manufacturer to be equivalent to 5 in^3 .

^[3] Taylor, B. N., and Kuyatt, C. E., "Guidelines for Evaluating and Expressing Uncertainty of NIST Measurement Results," NIST Technical Note 1297, National Institute of Standards and Technology, January, 1994.

^[4] Coverage factor, k of 2.26 for 9 effective degrees of freedom.

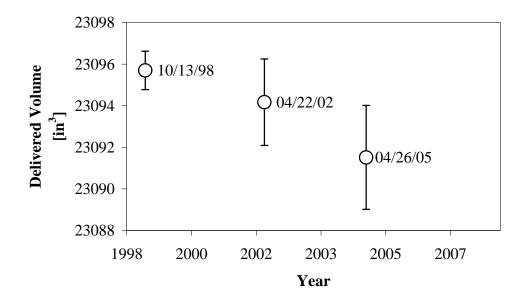


Figure 2. Calibration control chart for 100 gal graduated neck volume prover SN ABC123.

Date	Delivered Volume [in ³]	Difference from Prior [in ³]	Degree of Equivalence
04/26/05	23092.07	-2.10	0.36
04/22/02 10/13/98	23094.17 23095.70	-1.53	0.26

Table 2. Results of prior calibrations for the delivered volume.

For the Director, National Institute of Standards and Technology

Mnight

Dr. John D. Wright Project Leader, Fluid Metrology Group Process Measurements Division Chemical Science and Technology Laboratory National Institute of Standards and Technology

herry Secles

Sherry Sheckels Calibration Technician, Fluid Metrology Group Process Measurements Division Chemical Science and Technology Laboratory National Institute of Standards and Technology

sample report.xls

1.813000E-02 [C] 1.000810E+00 [1/C] 10/7/2004 6.348000E-02 [C] 9.97479E-01 [1/C]																									
T#5 Coef., d ₆ : T#5 Coef., d ₆ : Cal Date: T#3 Coef., e ₆ : T#3 Coef., e ₆ : Cal Date:	Air Density ref. 3 in SP-250 [kg/m ³] 1.17532 1.17661 1.17534 1.17534 1.17532																								
[1] [1/C] [2]	Rel. Humidity Read [%] 36.1 36.0 37.5 35.9 34.1	ume	Delivered	0.378508 0.378497	0.378516 0.378483	0.378491	0.378499		Kin. Visc.	CRC & Kell	[m ² /s] 1.125E-06	9.964E-07		c <mark>ted</mark> ected				468.51	121.94	121.94	4.00	45.43	11.60	14.50	1.00 283.99
3.330006-02 [C] 1.000755E+00 [1/C] 1.077204 -1.692002-01 [C] 1.007348E+00 [1/C] 2/2372005	Barometric Pressure ad [F Hg] [Pa] 80 99,565 60 99,565 99,565 20 99,525 20 99,485	Vessel Volume	Contained [m ³]	0.378609 0.378598	0.378619 0.378584	0.378593	0.378600	Water	Density	Patterson & Morris	[kg/m ³] 999.015	998.117		Averages, Thermal Expansion Corrected Averages, Therm. Exp. & Viscosity Corrected	10 ⁻⁶] ertaintv. [%]		1/V dV/ dX , dX , [x10 ⁶]	21.6	11.0	-11.0	-2.0	-6.7	-3.4	3.8	1.0 -16.9
T#4 Coef., b ₀ T#4 Coef., b ₁ : Cal Date: T#6 Coef., c ₀ T#6 Coef., c ₁ Cal Date: Cal Date:	Barome Read [mm of Hg] 746.60 746.60 746.50 746.20 746.20	Scale Reading	Corrected	0.000172 -0.000123	0.000090	0.000410			Temperature		[C] 15.560	20.426		Averages, Ther Averages, Thern	Repeatability [x 10 ⁻⁶] Expanded Uncertainty. [%]	ref. 8 In SP-250	dx ; for k=1	[m ³]	[kg]	[kg]	2.0E-03 [kg/m ³]	[1/C]	[1/C]		1.0E-03 [kg/m3]
600 [kg] +00 [1/kg] 5-07 [1/kg ²] 1005	Te Corrected 20.670 20.693 21.123 21.253	Scale F	Read [div]	-1.5	1.1	5.0			Delivered	[in]	23092.79 23092.12	23093.07 23091.01	23091.36	23092.07 23091.68	38 0.011	95% confidence, ref. 8 In SP-250	dx _i fo	8.2E-06 [m ³	4.2E-03 [kg]	4.2E-03 [kg]	2.0E-03	3.3E-07 [1/C]	7.0E-07 [1/C]	2.5E-02 [C]	1.0E-03
1.0008E -3.2489E 4/21/2	Air Temperature Read @ #5 [C] 20,529 20,558 20,858 21,084 21,217	Weight Drained	Corrected [ka]	168.4591 168.4591	168.4615 168.4593	168.4605		Volume	Contained		23098.92 23098.25	23099.36 23097.16	23097.58	23098.25	39 0.011	I .	Value	3 [1/m ³]	0.00 [1/kg]	0.00 [1/kg]	-1E-03 [m ³ /kg]	[0]	0	[1/C]	[m7/kg]
Scale Capacity: Scale Coeficient, a; Scale Coeficient, a; Scale Coeficient, a; Cal Date:	Read @ #4 20.535 20.727 20.844 21.078 21.205	Weight	Read	168.3387 168.3387	168.3411 168.3389	168.3401		rrected Prover	Delivered	[gal]	99.9687 99.9658	99.9700 99.9611	99.9626	99.9656 99.9640	38 0.011	Verr= 11	Va	e	00.00	00.0	-1E-03	-20.4 [C]	-4.9 [C]	2E-04 [1/C]	1E-03
div.]	Water Density ref. 4 in SP-250 [kg/m ³] 998.146 998.113 998.113 998.103 998.074	it Full	Corrected	545.9915 545.6873	545.9079 545.8288	546.1866		Thermal Expansion Corrected Prover Volume	Contained	<u>[</u>]	99.9953 99.9924	99.9972 99.9877	99.9895	99.9924	39 0.011	k= 2.20	1/V dV/dk ;	1۷	1/(m _f -m _e)	-1(m _F m _e)	-1/Q	-(Tw-T _{ref.W})	-(T _w -T _{ref})	Bw-Br	1/0
st Measure Co. 1234 ABC123 0.3785412 [m ³] 5.000 [in ³ /)	e Corrected Ave. 20.286 20.278 20.445 20.491 20.628	Weight Full	Read	545.6682 545.3641	545.5846 545.5055	545.8632		Thermal	Delivered	5	0.37842287 0.37841193	0.37842758 0.37839381	0.37839948	0.37841113 0.37840477	38 0.011		en	[m ³]	[kg]	[kg]	1000 [kg/m ³]	[1/C]	[1/C]		1.18 [kg/m3]
Name of Company: st Measure Co. NIST Seal Number: 1234 Serial Number: ABC123 Volume of Vessel: 0.3785412 Volume per Scale Division: 5,000 Date Calibrated: 4/26/2005	Water Temperature Read @ #3 (C) [C] 20.287 20.246 20.446 20.492 20.628	it Dry	Corrected	168.3588 168.3588 168.3588	168.3588 168.3588	168.3588			Contained	[m]	0.37852342 0.37851248	0.37853054 0.37849456	0.37850144	0.37851249	39 0.011	Estimation of Uncertainty	Value	[m]	545.92 [kg]	168.36 [kg]	1000	2.0E-04 [1/C]	4.8E-05 [1/C]	20.4 [C]	1.18
Nam NIST NIST Volume per S Da	Wa Read @ #6 20.285 20.243 20.490 20.627	Weight Dry	Read	168.2385 168.2385	168.2385 168.2385	168.2385		Ref. Temp.	0	15.56						Estimation	X /	٩	ŕ	a L	ρ_0	βw	В	τw	\mathcal{V}_{air}

REPORT OF CALIBRATION

Test Measure Co.

NIST Seal No.: 1234 Purchase Order No. ABC123