

# Optical Characterization in Microelectronics Manufacturing

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To successfully construct semiconductor devices, the semiconductor industry must measure fundamental material parameters, especially when developing new materials; measure the quality of the material as it is grown; accurately determine the details of thin films, quantum wells, and other microstructures that control or affect device performance; and measure properties of the devices themselves. Properties that need to be determined, therefore, include basic band structure and transport parameters, such as energy gap values and carrier scattering times; the presence and concentration of impurities and defects; alloy parameters; layer thicknesses; the distribution of materials in complex structures; and many others. This process of determining a wide range of material, structural, and device parameters is called characterization. The semiconductor industry uses many characterization methods which draw on electrical, chemical, and other approaches. Among these, optical characterization techniques, defined as those using electromagnetic radiation from the ultraviolet to the far infrared, stand out because they are nondestructive and require minimal sample preparation since no contacts are needed. These features are of great importance

for production use or to examine finished devices. Another benefit is that, unlike electrical methods which require fixed contacts, optical techniques can give two- or three-dimensional maps of properties over the extent of a semiconductor wafer. The six techniques described in this paper (ellipsometry, infrared spectroscopy, microscopy, modulation spectroscopy, photoluminescence, and Raman scattering) were chosen because they are currently or potentially widely used in the industry; they measure a broad array of semiconductor parameters; and they operate in different regions of the electromagnetic spectrum. The discussion of each technique indicates the basic semiconductor quantities measured, gives the scientific basis of the technique, and indicates how the measurement is made. Illustrative examples from the literature are discussed in detail, showing applications to important semiconductor materials. More information can be obtained from the detailed list of references included.

**Key words:** ellipsometry; infrared spectroscopy; modulation spectroscopy; optical microscopy; photoluminescence; Raman scattering.

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## 1. Introduction

To successfully construct semiconductor devices, the microelectronics industry must measure fundamental material parameters, especially when developing new materials; measure the quality of the material as it is grown; accurately determine the structural details of thin films, quantum wells, and other microstructures at the heart of devices; and measure properties of the devices themselves. Properties that need to be determined, therefore, include basic band structure and transport parameters, such as gap values and carrier scattering times, the presence and concentration of impurities and defects, alloy parameters, layer thicknesses, the distribution of materials in complex structures, and many others.

The semiconductor industry uses many characterization methods which draw on electrical, chemical, and other approaches. Among these, optical characterization techniques, defined as those using electromagnetic radiation from the ultraviolet to the far infrared, stand out because they are nondestructive and require minimal sample preparation, since no contacts are needed. These features are of great importance for production use, for on-line applications, and for examination of finished devices. Another benefit is that optical techniques can give two- or three-dimensional maps of properties over the extent of a semiconductor wafer without requiring fixed contacts.

Six techniques are described in this paper (ellipsometry, infrared spectroscopy, optical microscopy, modulation spectroscopy, photoluminescence, and Raman scattering). They were chosen because they are currently widely used in the industry and because they measure a broad array of semiconductor parameters. The discussion of each technique indicates the basic semiconductor quantities measured (see Table 1), the physical basis of the technique, and how the measurement is made. Illustrative examples from the literature are discussed, showing applications to important semiconductor material systems. A more detailed review of infrared, Raman and photoluminescence spectroscopies is given in a book by Perkowitz [1]. A recent review of the optical properties of semiconductors is given by Amiritharaj and Seiler [2].

### 1.1 A Note on Units

Some regions of the electromagnetic spectrum, and some optical methods, refer to wavelength as a

matter of usage; others use wavenumbers, or photon energy. Each section here uses the most common units for that technique, including wavelength in nanometers (nm) and micrometers ( $\mu\text{m}$ ); wavenumber in  $\text{cm}^{-1}$ ; and photon energy in electron volts (eV). Table 2 shows conversion factors for the main units of measure usually encountered.

Table 1. Semiconductor quantities (horizontal rows) and optical characterization methods (vertical columns, labeled as follows: ELL, ellipsometry; IR, infrared spectroscopy; MIC, microscopy; MOD, modulation spectroscopy; PL, photoluminescence; and RAM, Raman scattering). A bullet at the intersection of a given row and column means that the parameter can be determined by that technique using conventional methodology. Further details are given in the discussion

	ELL	IR	MIC	MOD	PL	RAM
Carrier density	• <sup>a</sup>				• <sup>a</sup>	
Carrier mobility		• <sup>a</sup>				• <sup>a</sup>
Carrier scattering time	•			• <sup>b</sup>		
Composition	•	•	•	•	•	•
Crystal orientation						•
Crystallinity	•	•			•	•
Defects		•	•		•	•
Energy gap		•		•	•	
Film thickness	•	•	•			
Impurities		•	•	•	•	•
Resistivity		•				•
Stress	•	•		•	•	•

<sup>a</sup> If the effective mass is known.

<sup>b</sup> Time resolved.

Table 2. Conversion factors for units of measure

$\lambda/\text{nm}$	$= 10^3\lambda/\mu\text{m}$
$E_\lambda/\text{eV}$	$= 1.2397/(\lambda/\mu\text{m})$
	$= 1.2397 \times 10^{-4}\lambda^{-1}/\text{cm}^{-1}$
$\lambda^{-1}/\text{cm}^{-1}$	$= 10^4/(\lambda/\mu\text{m})$

### 1.2 References

- [1] S. Perkowitz, *Optical Characterization of Semiconductors: Infrared, Raman, and Photoluminescence Spectroscopy*, Academic Press, London (1993).
- [2] P. Amiritharaj and D. G. Seiler, *Optical Properties of Semiconductors*, Chapter in *Handbook of Optics*, McGraw-Hill, to be published.

## 2. Ellipsometry

### 2.1 Introduction

Ellipsometry is a technique widely used to measure the thicknesses of films important to semiconductor technology, such as SiO<sub>2</sub> on Si. Thicknesses measured are typically in the range of several nm to several hundred nm. Surface cleanliness of semiconductor wafers during processing can also be determined. In spectroscopic ellipsometry, the ellipsometric data are obtained as a function of wavelength. Then appropriate modeling and fitting can yield the dielectric functions and thicknesses of the layers in complex semiconductor/oxide multilayer systems, such as SIMOX (Separation by IM-planting OXYgen), a silicon-on-insulator material formed by high-energy oxygen ion implantation in silicon. The dielectric functions give a complete picture of composition for the entire layered structure.

### 2.2 Physical Basis

Ellipsometry is based on the polarization transformation that occurs when a beam of polarized light is reflected from (or transmitted through) an interface or film. For example, if plane- or linearly-polarized light impinges on the surface of an absorbing medium, the reflected light usually becomes elliptically polarized because the reflection process differently affects the in-plane component of the incident electric field  $E_p$ , relative to the perpendicular electric field component  $E_s$ . Each component is reflected with new values of amplitude and phase. The key parameters obtained from an ellipsometric measurement are the ellipsometric angles  $\psi$  and  $\Delta$ . These appear in the complex reflection ratio  $\rho$ , defined as

$$\rho = \frac{r_p}{r_s} = \tan(\psi)e^{i\Delta}, \quad (1)$$

where the amplitude reflection coefficients  $r_p$  and  $r_s$  are

$$r_p = \frac{E_p(\text{reflected})}{E_p(\text{incident})} \quad (2)$$

$$r_s = \frac{E_s(\text{reflected})}{E_s(\text{incident})}. \quad (3)$$

The ellipsometric angles are defined as  $\psi = \tan^{-1}|\rho|$ , and  $\Delta$  is the difference in phase between the p and s components.

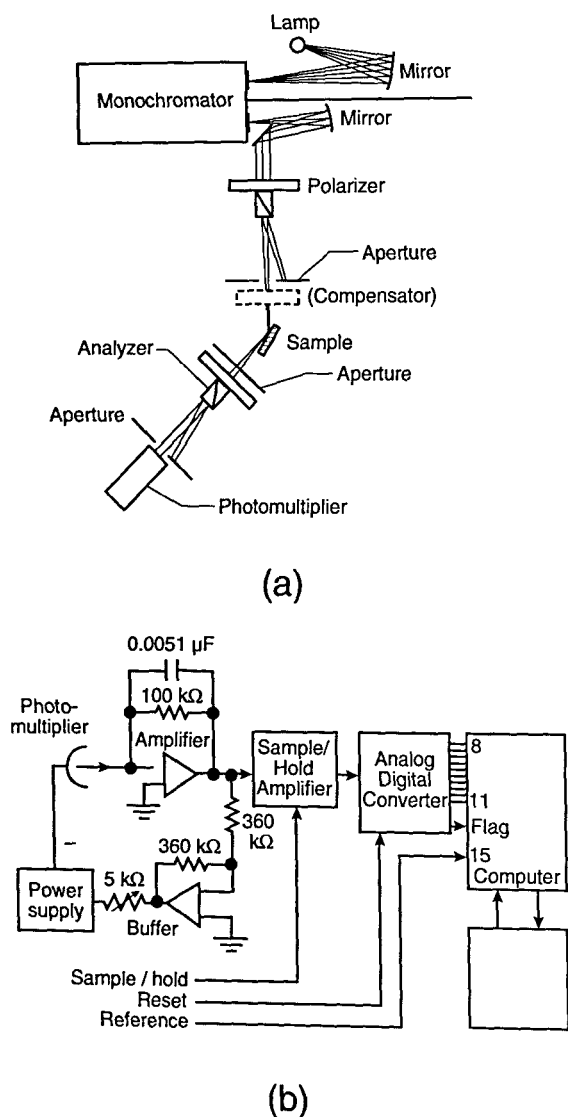
### 2.3 Experimental and Technical Details

Ellipsometric measurements start with light of known polarization incident on the sample. The polarization of the reflected light is determined, from which further analysis gives the parameters such as refractive index and film thickness which determine the interaction between light and sample.

In its simplest form, single-wavelength ellipsometry requires a manual nulling to gather data. Light from the source (usually a laser for single-wavelength work) passes through a linear polarizer, then through a compensator which elliptically polarizes the light. The light continues to the sample, is reflected, passes through a polarization analyzer, and is finally detected. The null technique works by adjusting the angle of the polarizer with respect to compensator, sample, and analyzer until the reflection process just cancels the ellipticity the light gained from the compensator. Then the reflected light is linearly polarized and can be extinguished by choosing the appropriate angle for the analyzer, that is, until the photomultiplier shows a minimum signal. The two values of the angles yield  $\rho$ .

This null process is too slow for real-time measurements, or for spectroscopic ellipsometry. Three types of automatic ellipsometry (self-compensating, rotating element, and polarization-modulated), together with dedicated computers, allow rapid measurement and analysis. In the automatic self-compensating system [1], the angles of the linearly polarized light leaving the polarizer, and entering the analyzer, are rotated by Faraday or Pockels cells, until the null is achieved. This type of instrument can give fixed wavelength data within 1 ms, and spectroscopic data over a wide wavelength range in 3 s.

The optical layout of the rotating element system (Fig. 1) is like that of the self-compensating system with the compensator omitted [1]. The polarization analyzer rotates around the axis of the reflected light beam at a fixed angular velocity, typically corresponding to 50 Hz to 100 Hz. The rotating analyzer would produce a sine-squared signal with two maxima and two true zero minima every rotation, if the light were linearly polarized. For elliptically polarized light, the signal is also of sine-squared form, but with smaller maxima, and nonzero minima, which depend on the ellipticity of the reflected light. A Fourier analysis of the output of the rotating analyzer gives  $\rho$  and hence the angles  $\psi$  and  $\Delta$ . For an analyzer rotating at 100 Hz, the measurement at a single wavelength can be completed in 5 ms.



**Fig. 1.** Schematic diagrams of (a) optical elements and (b) signal processing system for a rotating analyzer spectroscopic ellipsometer designed for high-precision measurements of the optical properties of solids. (See Sec. 2.5, General Refs., Collins (1990), fig. 3, p. 2032.)

The fastest type of system is the polarization-modulated ellipsometer [1], where the compensator in the manual null system is replaced by a birefringent phase modulator (a piezobirefringent plate or a Pockels cell). In the phase modulator, the ellipticity imparted to the linearly polarized light varies sinusoidally with time, rather than remaining constant as in the self-compensating system. The signal which results at the detector can be Fourier analyzed or analyzed by a phase-sensitive detector to

give  $\rho$ . A piezobirefringent modulator is a fast device, which can operate at 100 kHz or more; hence, this system can obtain data in an interval of 10 ms per wavelength measurement, which means that full scans over the range 400 nm to 700 nm can be obtained in a few seconds or less.

Of the three automatic systems, the polarization-modulated spectrometer is best for real-time rapid data acquisition. However, in the self-compensating and polarization-modulation cases, the compensator or modulator must be tuned for each wavelength; hence, these are more complex and can be less accurate than the rotating analyzer system.

For spectroscopic ellipsometry, a stable xenon lamp with output covering the near ultraviolet to near infrared is a commonly used source. The sample is mounted on a high-accuracy stage to allow careful angle alignment. Usually an autocollimator and apertures are used to control collimation and alignment. In general, available equipment gives good results over the near infrared to the near ultraviolet. The ellipsometric angles  $\Delta$  and  $\psi$  can be measured to within millidegrees, resulting in uncertainties of less than one part in  $10^3$  for the index of refraction and tenths of a nanometer for the corresponding thicknesses.

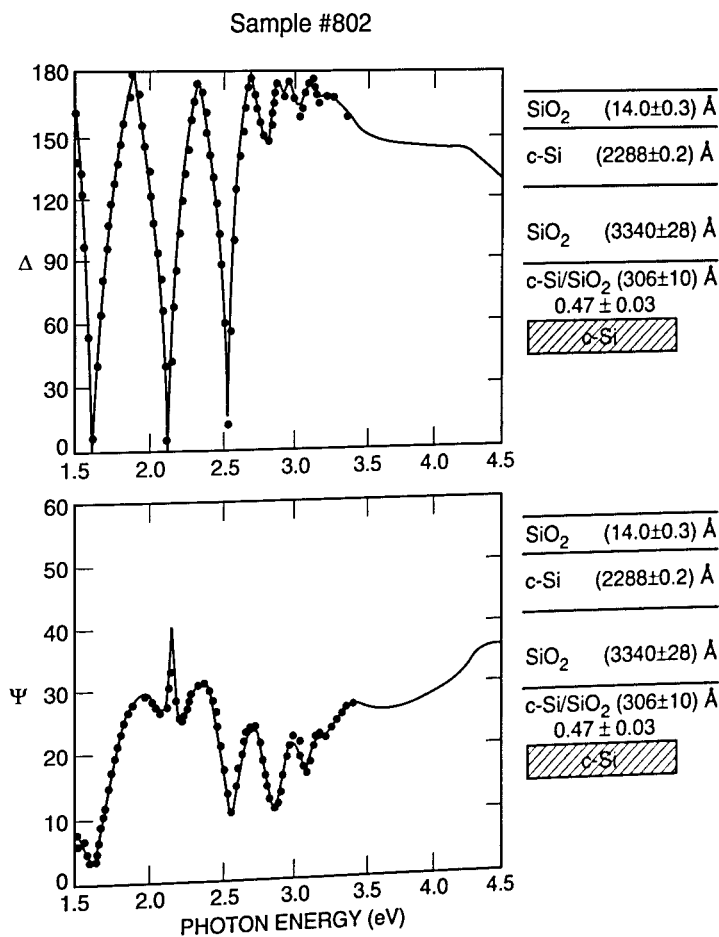
Parameters for a complex semiconductor/oxide system examined by ellipsometry are determined by sophisticated computer software [1–2]. These fit the measured ellipsometric parameters versus wavelength, by assuming appropriate dielectric functions for each layer, and layer thicknesses. Commercial systems include appropriate software, and fitting routines are also available from other sources.

## 2.4 Illustrative Applications

An example of the kind of semiconductor analysis that can be achieved with spectroscopic ellipsometry is shown in Fig. 2 for a sample of SIMOX, an important silicon-on-insulator system. The ellipsometric angles  $\Delta$  and  $\psi$  show complex spectra over the range 1.5 eV to 4.5 eV, with the large oscillations related to interference effects. Multiparameter regression analysis yields the fits displayed in the plots, which determine the sample's structural details as shown.

Table 3 presents typical sensitivities of quantities obtained by ellipsometry, such as thicknesses, composition, and temperature. For more specific details, the reader can refer to the citations given in the table.





**Fig. 2.** Ellipsometric angles  $\Delta$  and  $\psi$  versus photon energy for a SIMOX sample. Individual points, data obtained from rotating element spectroscopic ellipsometer. Solid line, fit obtained by regression analysis assuming structural layer thickness and composition shown on the right. The layer immediately below the 334 nm  $\text{SiO}_2$  layer is modeled as a granular mixture of crystalline Si (c-Si) and  $\text{SiO}_2$ , with 47% volume fraction c-Si, using effective medium theory. Shown to the right of the figures are the thicknesses of the layers. The calculated uncertainties of the model parameters are set to one standard deviation as determined by the regression analysis. (After D. Chandler-Horowitz et al. (1991), unpublished data, National Institute of Standards and Technology.)

**Table 3.** Spectral ellipsometry sensitivity. Given are sensitivities for the measurement of thicknesses, composition, damage profile, and temperature in a number of systems. The notations used for the measured quantity column are the complex reflection ratio,  $\rho$ ; the amplitude ratio,  $\psi$ ; and the phase shift,  $\Delta$

Method	Matrix	Quantity	Measured quantity	Conversion	Sensitivity <sup>a</sup>	Ref. (see below)
SE	SiO <sub>2</sub> /Si	SiO <sub>2</sub> thickness	$\rho$	Fresnel Equations <sup>[1]</sup> and Estimator <sup>[2]</sup> (FE&E)	$\pm 0.2 \text{ \AA}$ to $\pm 0.6 \text{ \AA}$ @ 1000 $\text{\AA}$ to 2300 $\text{\AA}$	3
SE	SiO <sub>2</sub> /SiO <sub>2</sub> + Si/Si	Interfacial SiO <sub>2</sub> + Si thickness	$\rho$	FE&E and EMA <sup>[4]</sup>	$\pm 2 \text{ \AA}$ @ 7 $\text{\AA}$	4
SE	SiO <sub>2</sub> /SiO <sub>2</sub> + Si/Si	SiO <sub>2</sub> thickness	$\rho$	FE&E and EMA	(112.1 $\pm$ 0.2) $\text{\AA}$ and (276.9 $\pm$ 0.2) $\text{\AA}$	5
SE	SiO <sub>2</sub> /a-Si/c-Si + SiC/SiC/c-Si	Layer thicknesses	$\rho$	FE&E and EMA	$\pm 2 \text{ \AA}$ to $\pm 25 \text{ \AA}$	6
SE	Polysilicon	Polysilicon composition (e.g., void + c-Si + a-Si)	$\rho$	FE&E and EMA	c-Si: 0.14 $\pm$ 0.02 void: 0.25 $\pm$ 0.06	7
SE	Si	Damage profile	$\rho$	FE&E and EMA	Damage range (170 $\pm$ 50) $\text{\AA}$ to (320 $\pm$ 20) $\text{\AA}$	8
SE	SiO <sub>2</sub> /polysilicon/SiO <sub>2</sub> /Si	Polysilicon and SiO <sub>2</sub> thicknesses	$\rho$	FE&E and EMA	Native oxide (15 $\pm$ 0.3) $\text{\AA}$ ; Poly $\pm$ 0.3 $\text{\AA}$ to $\pm$ 3.9 $\text{\AA}$ @ (240 to 1030) $\text{\AA}$ ; Oxide $\pm$ 0.4 $\text{\AA}$ to $\pm$ 1.7 $\text{\AA}$ @ (50 to 130) $\text{\AA}$	9
SE	SiO <sub>2</sub> /Si/SiN/Si	Native oxide, Si, and nitride thickness	$\rho$	FE&E and EMA	—	10
SWE	SiO <sub>2</sub> /Si	Temperature	$\psi, \Delta$	polynomial	$\pm 10 \text{ }^\circ\text{C}$	11
VASE	Oxide/GaAs/ Al <sub>x</sub> Ga <sub>1-x</sub> As/ GaAs	Thicknesses and AlGaAs composition	$\rho$	FE&E and EMA	Oxide (34 $\pm$ 3) $\text{\AA}$ GaAs (159 $\pm$ 8) $\text{\AA}$ AlGaAs (865 $\pm$ 14) $\text{\AA}$ AlGaAs, $x = 0.35 \pm 0.02$	12
VASE	Oxide/GaAs/ Al <sub>x</sub> Ga <sub>1-x</sub> As/ GaAs/Al <sub>x</sub> GaAs <sub>1-x</sub> /GaAs	Thicknesses and AlGaAs composition	$\rho$	FE&E and EMA	Oxide (26 $\pm$ 1) $\text{\AA}$ GaAs (435 $\pm$ 8) $\text{\AA}$ AlGaAs (413 $\pm$ 14) $\text{\AA}$ AlGaAs, $x = 0.37 \pm 0.005$ GaAs (142 $\pm$ 10) $\text{\AA}$ AlGaAs/GaAs SLS 5 @ (470 $\pm$ 20) $\text{\AA}$ AlGaAs/GaAs SLS $x = 0.32 \pm 0.001$	13
SE	Al <sub>x</sub> Ga <sub>1-x</sub> As/GaAs	AlGaAs composition and thickness <i>in situ</i>	$\rho$	Trajectories in $\epsilon_1$ and $\epsilon_2$	$x = 0.2 \pm 0.03$ ( $x > 0.2$ )	14

<sup>a</sup> Typically calculated as the 90 % confidence interval from the mean square deviation and covariance matrix.

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### 3. Infrared Spectroscopy

#### 3.1 Introduction

Infrared (IR) spectroscopy in the range from  $10\text{ cm}^{-1}$  to  $10,000\text{ cm}^{-1}$  can be used to determine impurity type and concentration in semiconductor materials, film thickness, semiconductor alloy composition, carrier density and scattering time. These determinations can be made for bulk, film, and microstructure systems. One application in Si measures the amount of interstitial oxygen, whose concentration is critical; correct values provide gettering action, reducing the level of other impurities, and hence, producing material with low leakage currents. Concentrations of oxygen in silicon and other impurities can be determined by infrared spectroscopic evaluation during processing.

#### 3.2 Physical Basis

Infrared radiation interacts with semiconductor lattices, carriers, and impurities, and is affected by semiconductor layer thickness. Binary semiconductors like GaAs have vibrational lattice transverse optical (TO) modes which couple to infrared radiation, with resonant absorption when the incoming frequency matches the TO frequency. Ternary alloys like  $\text{Al}_x\text{Ga}_{1-x}\text{As}$  display two TO modes, whose strength and frequency vary with  $x$ .

Semiconductor impurities can absorb infrared energy by photoionization of their bound carriers, or may modify their immediate lattice environment to produce a so-called local vibrational mode (LVM). In the case of photoionization, the impurity must be in a populated or ground state; hence, this absorption process is normally observed at cryo-

genic temperatures. Local vibrational modes occur when an impurity atom is lighter than the host lattice. Impurities important to semiconductor processing such as oxygen and carbon in Si produce LVM absorptions in the infrared region. If a semiconductor film is not too highly absorbing (device grade material is often highly conductive, and, therefore, absorbing), interference between infrared radiation reflected from the front surface, and that reflected from the back, can produce fringes whose spacing is related to the film thickness. Finally, free charge carriers in a semiconductor also absorb electromagnetic radiation. The absorption increases with wavelength; hence, absorption can be significant at infrared wavelengths even for low carrier concentrations.

An important feature of optical processes such as those occurring in the IR region is that quantitative measurements can be made based on absorption, reflection, or transmission data, and then accurately described by simple theory. The infrared properties are specified by the complex dielectric function  $\epsilon(\omega) = \epsilon_1(\omega) + i\epsilon_2(\omega)$ , which is related to the complex refractive index  $\tilde{n}(\omega) = n(\omega) + ik(\omega)$  by

$$\begin{aligned} n^2 - k^2 &= \epsilon_1(\omega) \\ 2nk &= \epsilon_2(\omega) \end{aligned} \quad (4)$$

If  $\tilde{n}(\omega)$  is known, then the reflection and transmission properties can be calculated. For instance, a semiconductor film has at normal incidence a front-surface reflection coefficient  $R$ ,

$$R = \frac{[(n-1)^2 + k^2]}{[(n+1)^2 + k^2]} \quad (5)$$

and a transmission coefficient,

$$T = \frac{(1-R)^2 e^{-\alpha d}}{(1-R^2 e^{-2\alpha d})}, \quad (6)$$

where  $\alpha$  is the absorption coefficient ( $= 4\pi k/\lambda$ ) and  $d$  is the film thickness. These expressions apply only when interference effects can be neglected, i.e., when noncoherent light is used.

For absorption due to lattice vibrations, or due to local impurity vibrational modes, the dielectric function  $\epsilon$  is

$$\epsilon(\omega) = \epsilon_\infty + \frac{S\omega_R^2}{\omega_R^2 - \omega^2 - i\omega\Gamma} \quad (7)$$

In this well-known Lorentzian form,  $\epsilon_\infty$  is the high-frequency limit of  $\epsilon(\omega)$ ;  $S$  is the oscillator strength;  $\Gamma$  is a damping term; and the resonant frequency  $\omega_R$  is the TO frequency for a lattice oscillation, or characteristic fingerprint frequency for an impurity vibrational mode. For a ternary semiconductor like  $\text{Al}_{1-x}\text{Ga}_x\text{As}$ , each TO mode is represented by a resonant term like that in Eq. (7), whose parameters depend on  $x$ .

If there are free carriers present,  $\epsilon$  has an additional term  $-\epsilon_\infty \omega_p^2/[\omega(\omega - i/\tau)]$ , where  $\tau$  is the carrier scattering time, and  $\omega_p^2$  is the plasma frequency  $4\pi Ne^2/m^* \epsilon_\infty$ , with  $N$  the carrier concentration and  $m^*$  the carrier effective mass. Hence,  $N$  and the drift mobility  $\mu = e\tau/m^*$  can be found from these parameters if  $m^*$  is known. Also, the dc resistivity  $\rho = m^*/ne^2\tau = \omega_p^2\tau$  can be found from these quantities, even if  $m^*$  is not known.

From the theory discussed above, measured reflection, transmission, and absorption data can be related to the microscopic semiconductor parameters. Thus, concentrations of impurity oxygen and carbon in silicon, for instance, in the parts-per-million range can be determined. Infrared analysis can also be used to determine carrier concentrations, mobilities, and resistivities for carrier concentrations as low as  $10^{14} \text{ cm}^{-3}$ , with results that agree well with conventional Hall effect and resistivity data.

Further, analysis of infrared reflectivity for thin films of semiconductors, which show interference effects, can be used to accurately determine the thicknesses of films in the micrometer range. For nonabsorbing films, the peaks of observed interference fringes occur at the wavelengths

$$\lambda_p = \frac{2n(\omega)d}{p} \quad (8)$$

where  $d$  is the layer thickness,  $n(\omega)$  is the real part of the refractive index, and  $p$  is the interference order, an integer or half integer  $1/2, 1, 3/2, \dots$ .  $n(\omega)$  is known for semiconductors of interest, so that  $d$  can be derived from Eq. (8).

Infrared methods can also be used to determine the presence of shallow impurities. A shallow donor impurity behaves like a hydrogen atom immersed in a medium with dielectric constant  $\epsilon$  and conduction band effective mass ratio  $m^*/m_0$ , where  $m_0$  is the free electron mass. From the Bohr model, the ionization energy (in eV) is

$$E_{\text{ion}} = \frac{13.6}{\epsilon^2} \left( \frac{m^*}{m_0} \right) \quad (9)$$

which is approximately 6 meV for GaAs. This simple model cannot predict ionization energies for different impurities in different materials, but shows that shallow donor ionization energies lie in the infrared region. Their exact values, and hence identification of the particular impurity, can be found from infrared photoconductivity spectra.

The theory developed above can be used to analyze inhomogeneous microstructures composed of layers of different semiconductors. Each layer is described by the same infrared theory and parameters that define its bulk behavior, to give its complex refractive index. Then, using standard theory for the reflection and transmission at each interface, the total infrared response of the structure can be calculated by computer. This model works well in fitting such data to determine average carrier properties, layer thicknesses, and phonon behavior which is related to microstructure properties and quality.

### 3.3 Experimental and Technical Details

Infrared spectroscopy often requires only minimal sample preparation, and the low energy and power of infrared radiation sources guarantee that the samples are not altered by the measurement. Because infrared light typically penetrates several micrometers into a semiconductor, this radiation can also be used to examine the various layered regions of an entire microstructure such as a superlattice.

Low source intensity and low detector sensitivity in the infrared region make Fourier transform spectroscopy the method of choice for obtaining IR spectra. In the Fourier method, infrared light, having traversed or been reflected from a sample, is analyzed with an interferometer. The optical intensity reaching the detector through the interferometer is the optical Fourier transform of the desired transmission or reflection spectrum. The interference spectrum is computationally transformed back into an intensity spectrum by means of the Fast Fourier transform algorithm on a computer. The light throughput advantage of a large interferometer aperture rather than the narrow slit of a conventional dispersive monochromator is referred to as the Jacquinot advantage. In addition, the interferometer allows simultaneous observation of many wavelengths, the so-called Fellgett advantage.

Figure 3 is a schematic diagram of a Michelson interferometer. Radiation from a broad-band source,  $s$ , is divided by a beamsplitter, BS. Light reflected from the beamsplitter is also reflected

from fixed mirror M1, whereas light transmitted through the beamsplitter is reflected from a movable second mirror, M2. The two light beams recombine to produce a net intensity whose magnitude depends on the difference  $\Delta$  between the paths that the two beams traverse. As mirror M2 moves,  $\Delta$  varies continuously. The intensity function  $I(\Delta)$ , called the interferogram, is

$$I(\Delta) = \int_0^\infty S(f) [1 + \cos(2\pi f\Delta)] df, \quad (10)$$

where  $S(f)$  is the intensity spectrum of the source as modified by the sample, and  $f = \omega/\pi c$  is the optical frequency in  $\text{cm}^{-1}$ . Equation (10) is the cosine Fourier transform of  $S(f)$ , which can be calculated from the inverse transform

$$S(f) = \int_0^\infty \left[ I(\Delta) - \frac{1}{2} I(0) \right] \cos(2\pi f\Delta) d\Delta. \quad (11)$$

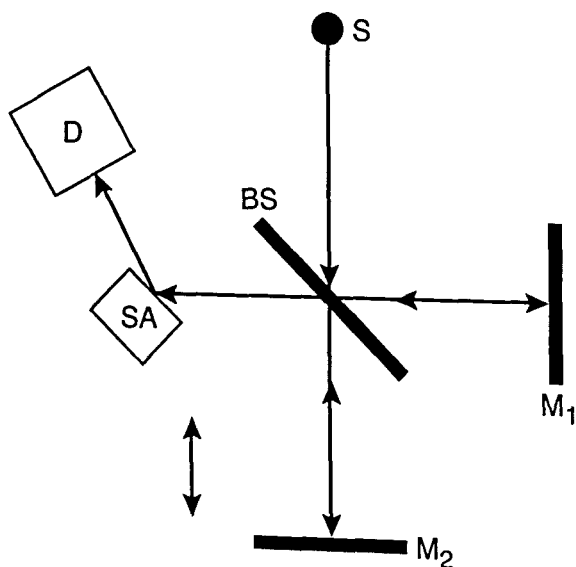


Fig. 3. Diagram of a Michelson interferometer configured for sample reflectance measurements. S, source; BS, beamsplitter; M1, fixed mirror; M2, movable mirror, which moves as indicated by the double-headed arrow; SA, sample; D, detector. The type of source and beamsplitter depends on the region of the infrared where data are to be obtained. The light beams reflected from M1 and M2 recombine to form the interferogram signal, which is measured by the detector.

This is implemented in the laboratory by processing the measured  $I(\Delta)$  with a computer to carry out the inverse transform. The spectral resolution in wavenumbers of the Fourier system is  $1/L$ , where  $L$

is the total travel of the movable mirror. Most machines use a rapid scan method, where the mirror is swept through its entire travel in a short time. Many sweeps are averaged together to enhance the signal-to-noise ratio.

Because of the small intensities of infrared sources, especially at the very long wavelengths of the far infrared spectrum, high-quality detectors are important. Liquid helium bolometers give the highest sensitivity, but are expensive and complex to operate. Mercury-cadmium-telluride detectors operating at liquid nitrogen temperatures work well in the mid infrared spectrum. Pyroelectric detectors operate at room temperature and are simple and rugged. They are sufficiently sensitive, from ultraviolet to millimeter wavelengths, for much semiconductor work.

Commercial Fourier transform infrared systems are available that cover the near infrared to the far infrared spectrum, by suitable choice of light source, beam splitter, and detector. To avoid the effect of water vapor absorption on the desired spectrum, these spectrometers are evacuated. Often, semiconductor samples must be cooled in order to better study electronic properties by removing the effects of lattice vibrations or phonons in the absorption spectra. This can be accomplished to 77 K with liquid nitrogen, and to 4.2 K with a liquid helium cryogenic system or by a mechanical refrigerator.

### 3.4 Illustrative Applications

Figure 4 illustrates the absorption peaks for interstitial oxygen at  $1107 \text{ cm}^{-1}$  and substitutional carbon at  $605 \text{ cm}^{-1}$  in Czochralski-grown silicon. Such absorption data can be converted into oxygen concentration values, giving a rapid, nondestructive way to determine this important quantity. Figure 5 demonstrates how a semiconductor film, in this case an epitaxial layer of high-resistivity silicon deposited on low-resistivity silicon, gives clear interference fringes that can be used to measure the layer thickness. Figure 6 correlates resistivity obtained from infrared measurements with resistivity obtained from carrier transport measurements. The data, from epitaxial n- and p-type  $\text{Hg}_{1-x}\text{Cd}_x\text{Te}$  films, are compared to results from conventional electrical measurements, which require ohmic contacts that can be difficult to apply. Figure 7 shows infrared reflectance data for an  $\text{AlAs-GaAs}$  superlattice. As the caption discusses in detail, the TO phonon mode for each constituent material is clear, as are interference fringes and other features. The simple theory for infrared phonon response gives a

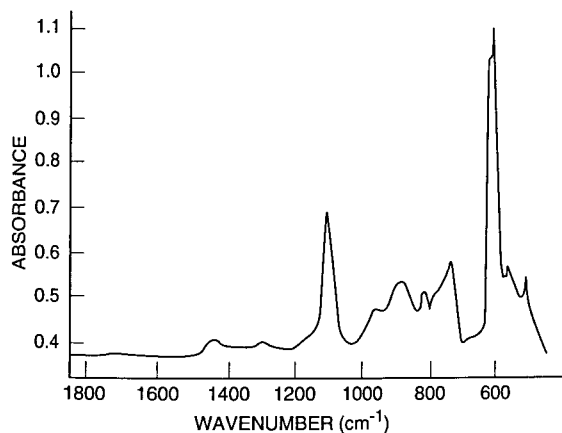


Fig. 4. Infrared absorbance for a Czochralski-grown silicon wafer 2 mm thick, derived from transmission spectra using a commercial Fourier spectrometer with a mercury-cadmium-telluride detector. The characteristic interstitial oxygen line at  $1107\text{ cm}^{-1}$  and the substitutional carbon line at  $605\text{ cm}^{-1}$  appear. Much of the remaining structure is due to silicon phonon modes. The absorbance at  $1107\text{ cm}^{-1}$  is linearly related to the oxygen concentration. Calibration data exist to convert absorbance into oxygen concentration in parts per million atomic or atoms per cubic centimeter. (See Sec. 3.5, Applications Refs., Krishnan, Stout, and Watanabe, in *Practical Fourier Transform Infrared Spectroscopy*, J. R. Ferraro and K. Krishnan, Eds., Academic Press, San Diego (1990), fig. 5, p. 298.)

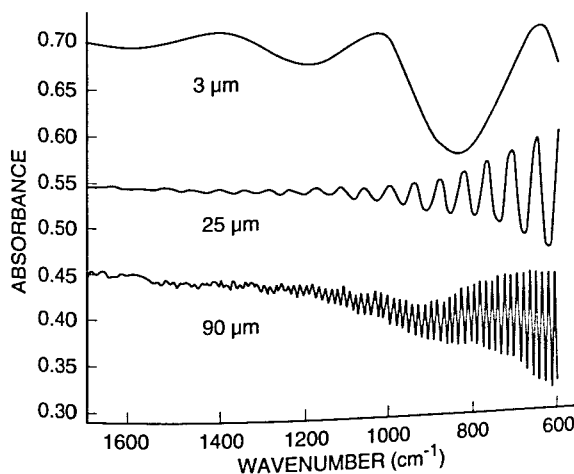


Fig. 5. Infrared reflectance spectra from structures consisting of low carrier concentration silicon epitaxial layers on high concentration silicon substrates, showing interference fringes that can be used to determine epitaxial layer thickness. Layers of different thickness produce different fringe spacings, according to Eq. (8). (See Sec. 3.5, Applications Refs., Krishnan, Stout, and Watanabe, in *Practical Fourier Transform Infrared Spectroscopy*, J. R. Ferraro and K. Krishnan, Eds., Academic Press, San Diego (1990), fig. 25, p. 333.)

fit which reproduces all the main features of the spectra, and allows an estimate of layer thickness.

Table 4 gives the sensitivities of typical quantities measured by infrared spectroscopy such as interstitial oxygen concentrations in Si and GaAs, substitutional carbon concentrations in Si and GaAs, and B, P, and As concentrations in Si. For more specific details, the reader should refer to the citations given in the table.

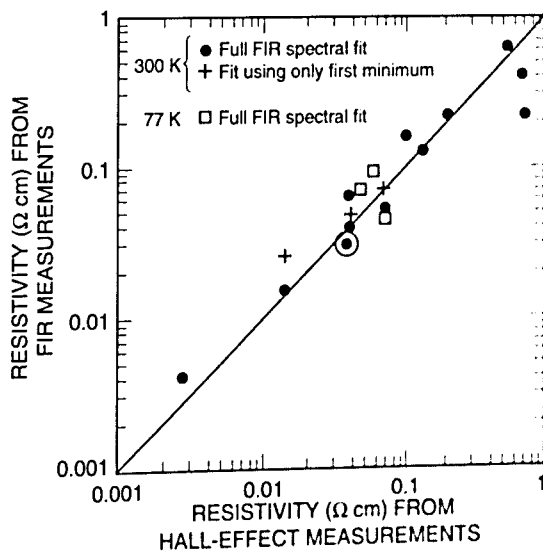


Fig. 6. Infrared values for dc resistivity compared to resistivity values from standard electrical (resistivity-Hall effect) measurements, for several n- and p-type  $\text{Hg}_{1-x}\text{Cd}_x\text{Te}$  films on CdTe substrates. The films were typically several micrometers thick with  $x$  values of 0.2 to 0.4. Results at both 300 K and 77 K are shown. Resistivity values marked "Full FIR spectral fit" were derived from fits to the full far infrared (FIR) spectrum over the range  $20\text{ cm}^{-1}$  to  $230\text{ cm}^{-1}$ , using the theory developed in this section. Resistivity values marked "Fit using only first minimum" were derived from the measured position of one particular feature of the FIR spectra, the so-called plasmon-phonon minimum whose location depends on resistivity. The solid line represents perfect agreement between the infrared and the conventional electrical results. The contactless infrared method agrees well with the time-consuming and destructive electrical method requiring contacts. (See Sec. 3.5, Applications Refs., Jones, Boyd, Konkel, Perkowitz, and Braunstein (1986), fig. 2, p. 2057.)

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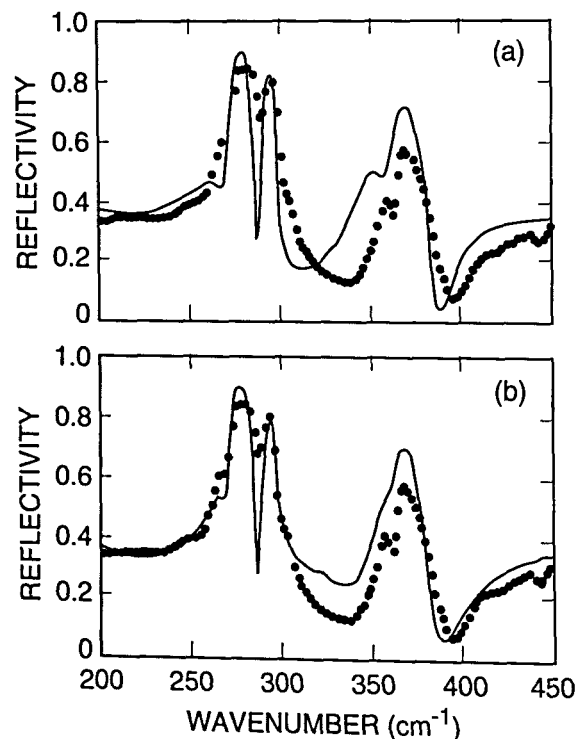


Fig. 7. Infrared reflectivity spectra for an AlAs-GaAs superlattice with 50 layer pairs. Panels (a) and (b) show the same data points. The peaks at  $275\text{ cm}^{-1}$  and  $365\text{ cm}^{-1}$  are the GaAs TO mode and AlAs TO mode, respectively. The peak at  $290\text{ cm}^{-1}$  and shoulder at  $355\text{ cm}^{-1}$  are interference fringes. The minima in the spectra lie at the positions of the structure's longitudinal optical phonon modes, which are sensitive to layer thickness. In Panel (a), the fitted solid line uses known phonon parameters for GaAs and AlAs, and the grower's nominal layer thickness  $d_{\text{AlAs}} = d_{\text{GaAs}} = 10\text{ nm}$ . The improved fit in Panel (b) uses the same phonon parameters, but allowed each layer thickness to vary for the best result. The numbers reported by Sudharsanan et al. gave  $d_{\text{AlAs}} = (7.5 \pm 0.2)\text{ nm}$  and  $d_{\text{GaAs}} = (8.2 \pm 0.2)\text{ nm}$ , in agreement with the x-ray results  $d_{\text{AlAs}} = (8.3 \pm 0.8)\text{ nm}$  and  $d_{\text{GaAs}} = (8.3 \pm 0.8)\text{ nm}$ . (See Sec. 3.5, Applications Refs., Sudharsanan, Perkowitz, Lou, Drummond, and Doyle (1988), fig. 1, p. 658.)

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## 4. Optical Microscopy

### 4.1 Introduction

In applications where the dimensions of interest are below the optical diffraction limit ( $\sim 0.8 \mu\text{m}$ ), electron microscopy is used by necessity. However, traditional optical methods remain useful for a large number of applications such as examining topological features larger than  $\sim 1.0 \mu\text{m}$ , examining defects, or counting etchpits. Several specialized forms of optical microscopy are highly valuable: Nomarski, scanning laser, and microspectrophotometry. In Nomarski microscopy, interference methods are used to increase the contrast between small differences in the surface level of a semiconductor wafer. Scanning microscopy in both the visible and infrared spectral ranges allows two-dimensional imaging of features in a layer or structure. Finally, microspectrophotometry allows film thickness determination from spectral analysis of reflected light.

Scanning microscopy is also used in both the visible and the infrared spectral ranges to form two-dimensional images of inhomogeneities in a semiconductor. The form called confocal microscopy produces three-dimensional images [1]. One visible light-scanning technique of special interest is the optical-beam-induced current method (abbreviated OBIC, or sometimes LBIC, for laser-beam-induced current), which detects grain boundaries, dislocations, and other defects in semiconductors and semiconductor devices. OBIC images represent spatial distributions of electrically active defects that include inclusions, strain, damage, precipitates, stacking faults, twin boundaries, dislocation clusters, and bandgap and doping variations. In this technique, a focused laser beam is scanned across the surface of the sample, and the induced current between two remote contacts on the sample is measured as a function of the laser beam position. The induced current is a result of the charge-separation effect of the regions in the vicinity of the light. Light incident on the area of the sample which is homogeneous and defect-free does not generate any induced current. Infrared scanning has been used to study individual precipitate particles in Si ingots, and to examine GaAs and other materials.

**Table 4.** Infrared sensitivity. Given are sensitivities for the measurement of interstitial oxygen [ $O_i$ ], substitutional carbon [ $C_s$ ], and nitrogen [Si-N-Si], in crystalline Si and substitutional carbon [ $C_{Ga}$ ] and interstitial oxygen [ $O_i$ ] in crystalline GaAs. Also given are sensitivities for measurement of compositions,  $x$ , of  $Al_xGa_{1-x}As$  and  $Hg_xCd_{1-x}Te$  and for carrier concentrations,  $N_d$ , in Si and GaAs. The sensitivity of far infrared low-temperature absorption measurements for substitutional boron [ $B_s$ ], phosphorus [ $P_s$ ], and arsenic [ $As_s$ ] are also given. The notations used for the measured quantity column are absorption coefficients,  $\alpha$ , at subscripted wavelength in  $cm^{-1}$ , e.g.,  $\alpha_{1107}$ ; absorption coefficient full width product,  $\alpha\Delta$ , at subscripted wavelength, e.g.,  $\alpha\Delta_{845}$ ; LO phonon frequency,  $\omega_{LO}$ ; plasma resonance frequency,  $\omega_p$ ; transmission,  $T$ ; and frequency,  $\omega$

Method	Matrix	Quantity	Measured quantity	Conversion	Sensitivity <sup>a</sup>	Ref. (see below)
LVM	Si	[ $O_i$ ]	$\alpha_{1107}$ @300 K	$[O_i] = \alpha \times 3.03 \pm 0.02 \times 10^{17} \text{ cm}^{-2}$	$\pm 2 \times 10^{15} \text{ cm}^{-3}$	1
LVM	Si	[ $O_i$ ]	$\alpha_{1107}$ @300 K	$[O_i] = \alpha \times 3.14 \times 10^{17} \text{ cm}^{-2}$	$\pm 2 \times 10^{15} \text{ cm}^{-3}$	2
LVM	Si	[ $C_s$ ]	$\alpha_{605}$ @300 K	$[C_s] = \alpha \times 1.1 \times 10^{17} \text{ cm}^{-2}$	$\pm 2 \times 10^{16} \text{ cm}^{-3}$	3
Absorption	Si	[Si-N-Si]	$\alpha_{963}$ @300 K	$[N_s] = \alpha \times 1.3 \times 10^{17} \text{ cm}^{-2}$	$\pm 2 \times 10^{15} \text{ cm}^{-3}$	4
LVM	GaAs	[ $C_{Ga}$ ]	$\alpha\Delta_{583}$ @77 K	$[C_s] = \alpha\Delta \times 1.1 \times 10^{16} \text{ cm}^{-1}$ $[C_s] = \alpha\Delta \times 8 \pm 2 \times 10^{15} \text{ cm}^{-1}$	$\pm 2 \times 10^{14} \text{ cm}^{-3}$	5 6
LVM	GaAs	[ $O_i$ ]	$\alpha\Delta_{845}$ @10 K	$[C_s] = \alpha\Delta \times 8 \times 10^{16} \text{ cm}^{-1}$	$\pm 2 \times 10^{15} \text{ cm}^{-3}$	7
Phonon frequency	$Al_xGa_{1-x}As$	$x$	$\omega_{LO}$ or $\omega_{TO}$ @300 K	$(\omega_{LO}/2\pi c)/\text{cm}^{-1} = 292.4 + 70.8x - 26.8x^2 - 41.13x^3$		8
IR cut off	$Hg_xCd_{1-x}Te$	$x$	$T$ vs $\omega$	Ref. 9		9
IR plasma frequency	Si	$N_d$	$\omega_p$ @300 K	$\omega_p^2 = 4\pi N_d e^2 / \epsilon m^*$		10
IR plasma frequency	GaAs	$N_d$	$\omega_p$ @300 K	$\omega_p^2 = 4\pi N_d e^2 / \epsilon m^*$		11
Absorption	Si	[ $B_s$ ]	$\alpha\Delta_{320}$ @12 K	$[B_s] = \alpha \times 1.1 \times 10^{17} \text{ cm}^{-2}$	$\pm 1.5 \times 10^{12} \text{ cm}^{-3}$	12
Absorption	Si	[ $P_s$ ]	$\alpha\Delta_{316}$ @12 K	$[P_s] = \alpha \times 1.1 \times 10^{17} \text{ cm}^{-2}$	$\pm 1.5 \times 10^{12} \text{ cm}^{-3}$	12
Absorption	Si	[ $As_s$ ]	$\alpha\Delta_{382}$ @12 K	$[As_s] = \alpha \times 1.1 \times 10^{17} \text{ cm}^{-2}$	$\pm 1.5 \times 10^{12} \text{ cm}^{-3}$	12

<sup>a</sup> Calculated as the concentration-equivalent-of-noise assuming  $\pm 0.1\%$  noise in transmission.

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## 4.2 Physical Basis

**4.2.1 Nomarski Microscopy** In Nomarski microscopy, two microscopic images of a surface are formed so that they are slightly displaced in space and of opposite phase. Interference bands appear where the images overlap. The physical displacement and the interference bands heighten the visibility of small variations in surface levels.

**4.2.2 Scanning Microscopy** In scanning microscopy, a spot of light, whose size is limited by diffraction, is scanned over a specimen. The image of the specimen is developed point by point in sequential fashion, to be displayed or stored for analysis. If the specimen is broadly illuminated and scanned in a raster pattern by a point detector (or raster scanned by a point source, with the light sensed by a broad area detector), a two-dimensional image results. In the variation known as confocal scanning, the specimen is illuminated in only a small region at any one time, and a point detector senses light only from that same region. This makes it possible to develop a three-dimensional image. Confocal scanning also enhances resolution.

The light can be sensed by any of several conventional detectors. In the OBIC method, however, the detector is an external circuit that measures the current produced locally by the incident light. Light intensity from a laser of even modest power creates a high density of carriers in the sample, due to electron-hole excitation. The electrons and holes are affected by the electric fields associated with macroscopic defects, such as grain boundaries in polycrystalline silicon, so that the motion of the electrons and holes induces a current which is sensed by an external circuit. Hence, OBIC images clearly show the presence of defects, and map out their locations.

**4.2.3 Microspectrophotometry** Reflection spectrophotometry depends on the interference pattern caused by reflections from top and bottom surfaces of a transparent film. The equations governing reflection from stratified dielectric media are derived in most optics texts [2]. Microspectrophotometry is normally used for determining the film thickness of a single layer on a substrate or the film thicknesses in a relatively simple multilayer stack. As in ellipsometry, values of the functions  $n(\omega)$  and  $k(\omega)$  for each of the layers of interest are needed to determine the thicknesses. The advantages of reflectometry relative to ellipsometry are that most of the information is carried in the wavelength dependences, and it is relatively simple to focus the beam down to spot sizes on the order of micrometers [3].

## 4.3 Experimental and Technical Details

**4.3.1 Nomarski microscopy** In Nomarski microscopy, two microscopic images of a surface are formed by a Wollaston prism. The prism is placed between the eyepiece and the objective of the microscope, as shown in Fig. 8.

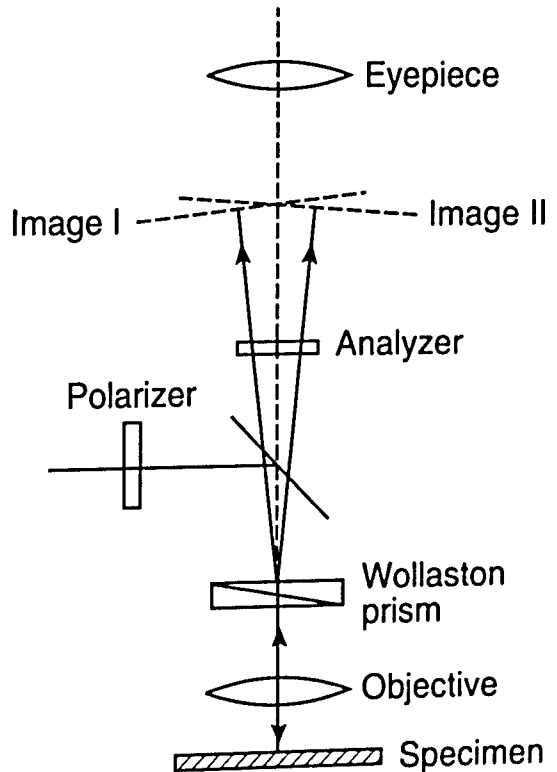


Fig. 8. Schematic diagram of a Nomarski interference microscope. The Wollaston prism consists of identical prisms of crystalline quartz, one with its optical axis parallel to the plane of the paper and the specimen surface, the other perpendicular to the plane of the paper. (See Sec. 4.5, General Refs., Modin and Modin (1973), fig. 3.17, p. 130.)

Light traversing the prism is divided into two beams polarized at right angles to each other and diverging by some angle, giving two microscopic images. The microscope includes a polarizer set so that the incident light lies at  $45^\circ$  to the plane of vibration of the prism. With an analyzer set at right angles to the polarizer, this gives two images of the same intensity but  $180^\circ$  apart in phase. Hence, interference bands form where the images overlap. These fringes, combined with the displacement of the images, magnify surface variations. The edges of surface features become clearly visible, and the thickness of films deposited on the surface can be found.

**4.3.2 Scanning Microscopy** Figure 9 shows the main components of a scanning microscope. It includes a light source, usually a laser; a scanning system, which either moves the laser beam across a fixed sample or moves the sample relative to a fixed optical system; optical elements to focus and manipulate the beam; and a detector. The type of detector used depends on the scanning and imaging methods and on the wavelengths; it may be a single photomultiplier tube or a detector array. In the OBIC method, it is an external circuit that measures the photocurrent.

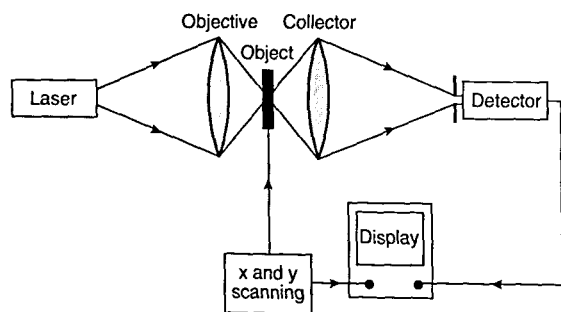


Fig. 9. Schematic diagram showing the main elements of a scanning microscope. (See Sec. 4.5, General Refs., Wilson and Sheppard (1984), fig. 1.1, p. 2.)

As stated above, in some systems, the light beam is scanned across a fixed sample. This allows rapid acquisition and display of images; however, there are complications in designing the movable optical system, and in maintaining good image quality. In other designs, the light beam is fixed and the sample is moved to produce the raster pattern. Although these systems are relatively slow, the optical design is simple and produces images of high quality.

The OBIC technique (a typical experimental arrangement is illustrated in Fig. 10) is one of the most important for semiconductor materials and devices, and can readily be implemented with small lasers as sources. A 1 mW HeNe laser produces  $3 \times 10^{15}$  photons per second. Based on a calculation using typical parameters for electron-hole generation in a semiconductor, this intensity is enough to generate a large density of electron-hole pairs, about  $10^{20} \text{ cm}^{-3}$ . The electric fields associated with defects or doped regions separate the electron and hole in each pair. These separated carriers can induce a current by flowing through an appropriate external circuit. (Depending on whether the sample includes a p-n junction or not and on the nature of the circuit, either photovoltages or photocurrents can be measured.)

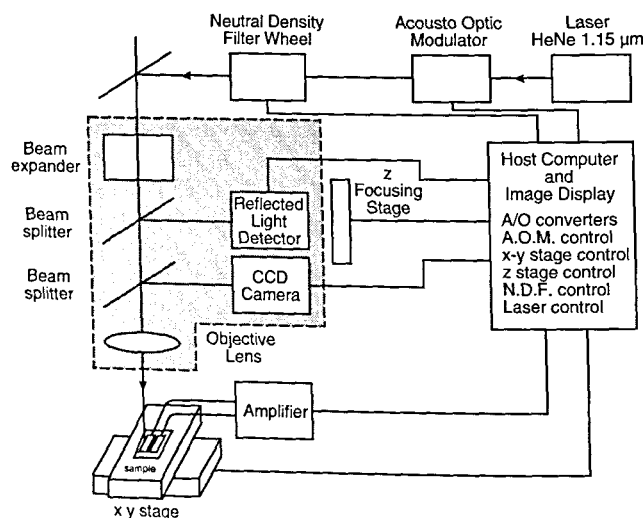


Fig. 10. Schematic diagram of an optical-beam-induced current (OBIC) system, also called LBIC (laser-beam-induced current). (See Sec. 4.5, General Refs., Moore, Hennessy, Bajaj, and Tennant (1988), fig. 1.)

Scanning methods can be used equally well in the visible and in the infrared regions. In one typical infrared system, the source is a semiconductor laser operating at  $1.3\ \mu\text{m}$  wavelength (giving a spot diameter of about  $2\ \mu\text{m}$ ), with detection accomplished by germanium photodiodes. The sample is mechanically moved to produce raster scanning, and the resulting images are taken at resolutions of 512 pixels by 512 pixels.

**4.3.3 Microspectrophotometry** Interference of light waves reflected from each interface of a multilayer film structure determines the reflectance of the structure. The reflectance spectrum depends on angle of incidence of the radiation, the refractive indices of the media, polarization of the radiation, and film thicknesses [4]. Whereas the same equations describing reflection and transmission apply in both ellipsometry and reflectance spectrophotometry, the problem is somewhat simplified in the case of reflectometry, where polarization is usually ignored. Normally, the reflected light intensity is recorded versus wavelength. Then, the thicknesses are calculated by fitting measured spectra to calculated spectra based on a model of the layer structure and known dielectric constants. Measurements can also be made of the reflectance versus polarization angle or versus angle of incidence, but this is not normally done in microscopic measurements because these parameters are difficult to change systematically within the microscope environment. The most frequent application of microspectrophotometry is the determination of thicknesses of simple dielectric stacks on a substrate; but microspectrophotometry can also be used like ellipsometry to find the dielectric function of film layers and, hence, film layer composition [4]. Because of the relaxed constraint on the angle of incidence and the relative speed of processing data, microspectrophotometry is an ideal way to map the uniformity of wafer film thickness.

#### 4.4 Illustrative Applications

Figure 11 shows the power of OBIC imaging to detect flaws in semiconductor materials such as silicon, even when the material is incorporated in an operating device such as a transistor. Figure 12 shows an infrared scanning system micrograph of oxide particles embedded in Czochralski-grown silicon, even displaying those particles smaller than the infrared beam diameter of  $2\ \mu\text{m}$ . By focusing to different depths in the sample, it is possible to obtain some depth-dependent information as well.

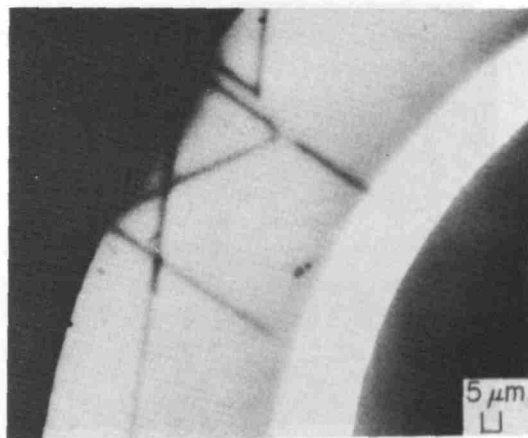


Fig. 11. An OBIC image formed by monitoring the emitter-base current in a silicon transistor while a laser beam is scanned across the transistor. The dark straight lines are lines of dislocations in the silicon. (See Sec. 4.5, General Refs., Wilson and Sheppard (1984), fig. 1.6, p. 8.)

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#### General

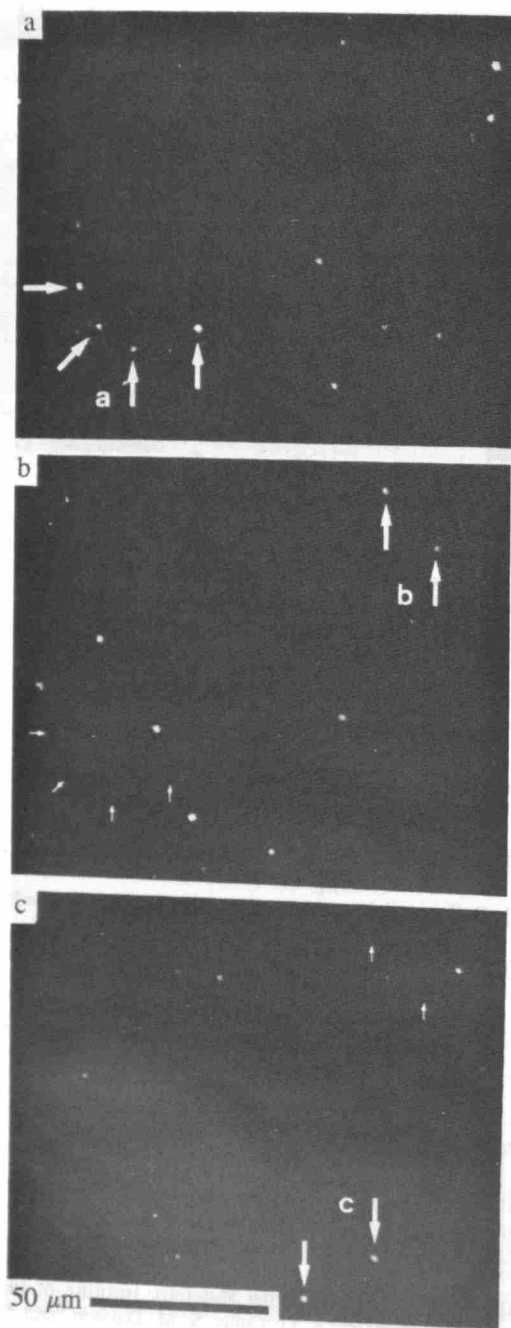
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**Fig. 12.** Infrared scanning microscope images of oxide particles in heat-treated (100) Czochralski silicon. The microscope used a semiconductor laser emitting at  $1.3\ \mu\text{m}$ , to give a spot size of  $\sim 2\ \mu\text{m}$ . Particles of this size or greater are directly imaged. Smaller particles can still be seen, although as spots  $2\ \mu\text{m}$  across, because the system can detect intensity variations of about 0.5 %. The depth of focus is  $30\ \mu\text{m}$ . Panels (b) and (c) show successively deeper probes into the sample, relative to Panel (a). The focal plane is  $60\ \mu\text{m}$  deeper in Panel (b) and  $120\ \mu\text{m}$  deeper in Panel (c). The sets of oxide images marked “a,” “b,” and “c” can be followed in and out of focus through the panels. (See Sec. 4.5, Applications Refs., Laczik, Booker, Falster, and Shaw (1989), fig. 1, p. 808.)

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## 5. Modulation Spectroscopy

### 5.1 Introduction

Modulation spectroscopy is a sensitive technique which can determine fine details of interband transitions in semiconductors. In semiconductor superlattices and other microstructures, detailed knowledge of the complex interband transitions can be used to characterize quantum well widths, potential barrier heights and widths, electric fields, and the amount of strain in strain layer systems.

### 5.2 Physical Basis

The principle behind modulation spectroscopy is that a periodic physical perturbation applied to a sample elicits the derivative of the sample's optical response to that perturbation. The derivative feature amplifies weak features in the response function and suppresses large constant background levels. This gives modulation methods very high sensitivity to small spectral features that are invisible in conventional spectroscopy.

To illustrate the origin of the derivative response, consider the reflectivity  $R$  of a sample. This depends on the sample's dielectric function, which depends on many physical properties. For example, the dielectric function depends on an applied electric field  $E$ ; hence,  $R$  also depends on  $E$ . If the applied electric field has a dc component  $E_0$  and a small ac component  $E_1 \cos \Omega t$  ( $\Omega$  is the modulation angular frequency), the reflectivity can be written as  $R(E) = R(E_0 + E_1 \cos \Omega t)$ . If  $E_1 \ll E_0$ , this expression can be expanded in a Taylor series, where only the first two terms are kept; that is

$$R(E) \cong R(E_0) + \frac{dR}{dE} (E_1 \cos \Omega t). \quad (12)$$

The first term depends on  $E_0$  but not on time, whereas the second term is a periodic function of

time at the modulation frequency  $\Omega$ . Hence, the ac portion of the reflectance at frequency  $\Omega$  can be detected with a lock-in amplifier; this signal is proportional to the derivative  $dR/dE$ . Thus, small structures in the optical spectrum of  $R(E)$  are enhanced, even with the sample at room temperature. A periodic perturbation can be applied to any physical property affecting the sample's optical response. Examples are electroreflectance, where a periodic electric field is applied to a sample while its reflectance spectrum is measured; and photorelectance, where optically injected carriers from a chopped laser beam modulate the "built-in" surface or internal electric fields, thereby modulating the reflectance of the sample. Other forms of modulation spectroscopy have been reviewed by Aspnes [1]. The following discussion concentrates on electroreflectance and photorelectance, two forms of modulation spectroscopy currently in common usage. Because photorelectance results from the modulation of "built-in" electric fields, this discussion applies generally to either electroreflectance or photorelectance.

The enhancement of spectroscopic structures that appear at energies corresponding to energy gaps and other critical points in the joint density of states of the material under study is one useful result of modulation methods. The method becomes more useful still when the measured spectral line shapes can be connected to microscopic parameters through theory. The relationship that makes this connection is [2]

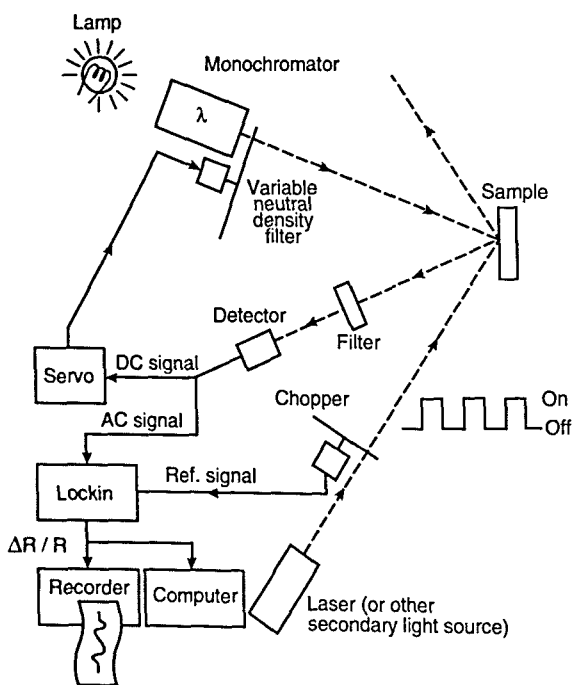
$$\frac{\Delta R}{R} = \alpha \Delta \epsilon_1 + \beta \Delta \epsilon_2, \quad (13)$$

where  $\Delta R$  is the change in reflectivity due to the applied modulation,  $\Delta \epsilon_1$  and  $\Delta \epsilon_2$  are the changes in the real and imaginary parts, respectively, of the complex dielectric function  $\epsilon = \epsilon_1 + i\epsilon_2$ , and  $\alpha$  and  $\beta$  are called the Seraphin coefficients. Near the energy gap of a bulk sample,  $\beta = 0$ ; however, for complex microstructures where interference effects occur, both  $\alpha$  and  $\beta$  need to be considered, and hence  $\Delta \epsilon_1$  and  $\Delta \epsilon_2$  must both be known. These can be calculated from general band theory and from dielectric function theory. In the case of electroreflectance and photorelectance, different spectral line shapes are obtained, and concomitantly different analyses are required, depending on the magnitude of the electric field. The modulation field is usually described in terms of three regimes [2]: high field (Stark effect), intermediate field (Franz-Keldysh effect), or low field. The high field case is

not usually studied under modulation conditions, as a high electric field breaks down the normal selection rules and results in a Stark shift of the band structure. The analysis of spectra based on intermediate and low field theories is discussed in reference to representative spectra, in the illustrative applications section below.

### 5.3 Experimental and Technical Details

A modulation measurement requires a light source, a monochromator, and a detector as in conventional spectroscopy, and a means to apply the modulation to the sample. These elements are shown in Fig. 13. The source can be an incandescent or discharge lamp. Generally, a monochromator of 0.25 m focal length provides adequate energy resolution, but higher resolution may be needed in some cases.



**Fig. 13.** Diagram of a photoreflectance spectrometer, illustrating lamp with following optics and electronics to obtain the spectrum, and a laser to supply modulated light. The variable neutral density filter holds the constant part of the detected signal independent of wavelength, facilitating evaluation of the ratio of  $\Delta R/R$ . (See Sec. 5.5, General Refs., Pollak and Glemboki (1988), fig. 4, p. 25.)

The light reflected from the sample is detected by a photomultiplier tube or a photodiode. It contains a steady (dc) component  $RI_0$  ( $I_0$  is the incident light intensity) and a periodically modulated (ac)

component  $\Delta RI_0$ . To obtain  $\Delta R/R$ , the dc signal and the ac signal must be separately measured and then a ratio of these signals is taken. It is also possible to electronically hold the dc signal (corresponding to  $RI_0$ ) constant during the measurement. This can be done by a feedback loop that changes the gain of the detector to keep its dc output constant, or, as shown in Fig. 13, by mounting a circular continuously variable neutral density filter on a servo motor and inserting it before the sample.

For photoreflectance, light from a modulated optical source such as a laser, whose photon energy exceeds the sample's energy gap, impinges on the sample. For electroreflectance of a doped semiconductor, the varying electric field can be applied between an ohmic contact on the sample's back surface, and a transparent gate electrode on the front of the sample; 5 nm to 10 nm of deposited gold or aluminum is an adequate electrode. A second method is to put the sample in an electrolyte such as a KCl solution, or an acidic solution. The resulting electric field at the sample surface can be changed by varying a voltage applied between the sample and a platinum counter electrode. Photoreflectance and electroreflectance spectroscopy both provide highly detailed spectra even at room temperature, so that sample cooling is usually not needed.

### 5.4 Illustrative Applications

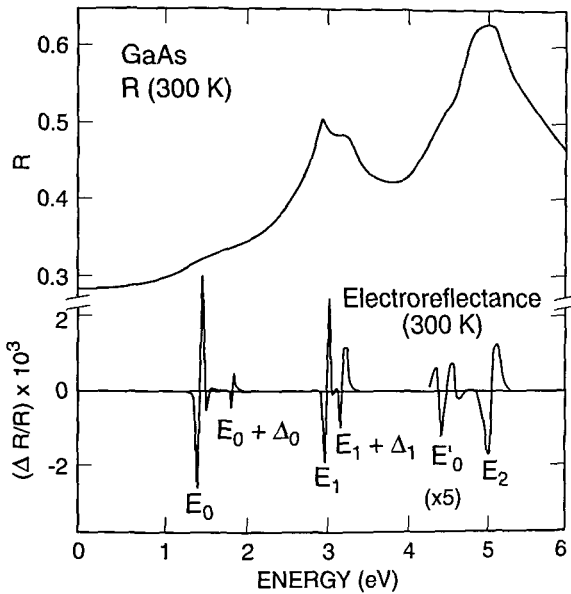
Figure 14a shows the sensitivity of modulation spectroscopy, by comparing the reflectivity spectrum of GaAs in the interband region to the much more detailed  $\Delta R/R$  spectrum obtained by electroreflectance. Figure 14a is illustrative of the low field case. Here the spectra near the energy gap can be fitted using [3]

$$\frac{\Delta R}{R} = R[e^{i\theta} (\hbar\omega - E_g + i\Gamma)^{-m}], \quad (14)$$

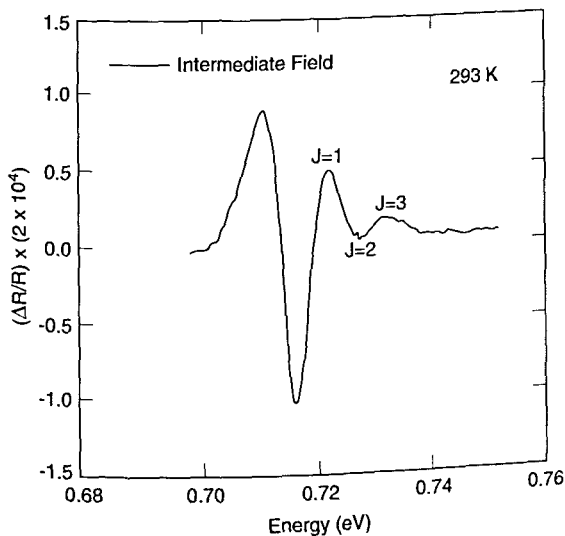
where  $\hbar\omega$  is the photon energy,  $E_g$  is the gap energy,  $\theta$  is the phase factor,  $\Gamma$  is the lifetime broadening parameter, and the quantity  $m$  takes on the values 2, 2.5, and, 3 for excitonic, three-dimensional, and two-dimensional critical points, respectively. Hence, the critical point type and energy can be determined from fitting this line shape. Aspnes [3] has also developed a "three-point" method for extracting critical point energies which for simple spectra eliminates the need for a full spectrum fit.

Shown in Fig. 14b [4] is the photoreflectance spectra of a moderately n-type doped





**Fig. 14a.** Conventional interband reflectivity spectrum for GaAs at 300 K, compared to the interband  $\Delta R/R$  spectrum at 300 K obtained by electroreflectance. The broad features in the plot for reflectivity  $R$ , such as the shoulder at the gap energy  $E_0$ , become obvious sharp lines in the  $\Delta R/R$  data which lie on a baseline of zero signal. Structure at  $E_0 + \Delta_0$  which was invisible in the reflectivity spectrum is apparent in the  $\Delta R/R$  curve. (See Sec. 5.5, General Refs., Pollack and Glebocki (1988), fig. 1, p. 25.)



**Fig. 14b.** Photoreflectance spectra for the intermediate field case for a moderately doped sample of InGaAs/InP with labeled extrema ( $J = 1, 2, 3$ ).

( $\sim 1 \times 10^{16} \text{ cm}^{-3}$ ) sample of  $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}$  illustrating the intermediate field line shape. This case can be

identified by the presence of oscillatory behavior, the so-called Franz-Keldysh oscillations at energies greater than the energy gap of the material. Modulation intensities are usually greater for the high field case than for the low field case. Materials information (electric fields and energy gap values) is typically extracted from Franz-Keldysh oscillations using the Aspnes asymptotic approximation [5]

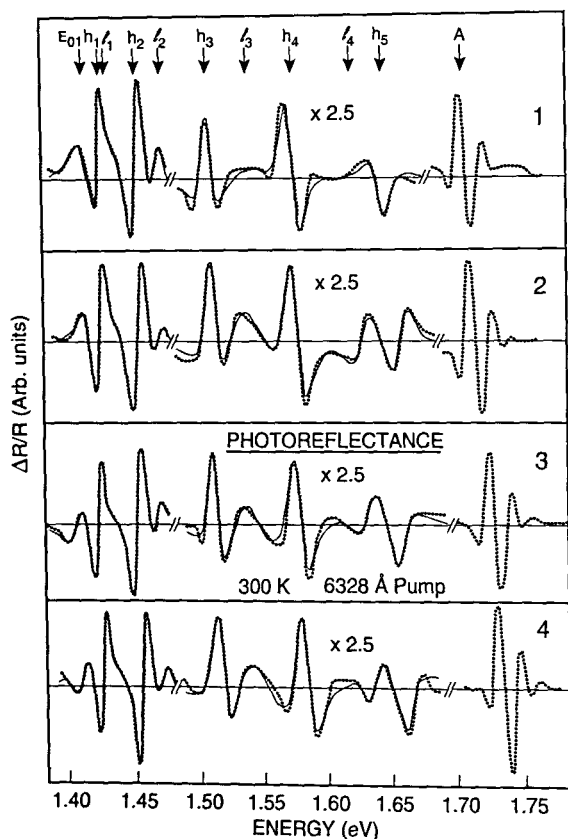
$$\frac{\Delta R}{R} = (\hbar\omega - E_g)^{-1} \exp \frac{I(\hbar\omega - E_g)^{1/2}}{(\hbar\Omega)^{3/2}} \times \cos \left[ \theta + \frac{2}{3} \left( \frac{\hbar\omega - E_g}{\hbar\Omega} \right)^{3/2} \right], \quad (15)$$

where  $\theta$ ,  $I$ , and  $E_g$  are defined above, and  $\hbar\Omega$  is the electro-optic parameter  $[e^2 E^2 \hbar^2 / 32 \pi^2 \mu]^{1/4}$ . Here,  $e$  is the electron charge,  $E$  is the dc electric field,  $\hbar$  is Planck's constant, and  $\mu$  is the reduced interband effective mass. Since successive extrema represent a change of  $\pi$  in the argument of the cosine term in Eq. 15, the energy of the  $j$ th extrema [5] can be written as

$$j\pi = \theta + \frac{2}{3} \left[ \frac{(\hbar\omega - E_g)}{\hbar\Omega} \right]^{3/2}. \quad (16)$$

Hence, the phase factor and electro-optic energy can be obtained from the intercept and slope of a plot of  $(\hbar\omega - E_g)^{3/2}$  vs  $j$ . It is noteworthy that the electric field in a structure under study can be extracted from the electro-optic energy, requiring only independent knowledge of the effective mass of the material. Hence, electroreflectance and photoreflectance provide very important methods for nondestructive determination of surface and junction electric fields. These fields can, in turn, be related to doping densities in a space charge region [6] through the Schottky equation.

Figure 15 presents photoreflectance data used to characterize a GaAs/ $\text{Al}_{0.24}\text{Ga}_{0.76}\text{As}$  multiple quantum well. The chopped laser beam, 100  $\mu\text{m}$  in diameter, had been moved along the structure to give spectra from different spatial regions. Each of the resulting spectra was theoretically fitted, to determine how the well width and Al mole fraction value changed with position over a distance of 1.4 cm.



**Fig. 15.** Photoreflectance spectra of GaAs/Al<sub>x</sub>Ga<sub>1-x</sub>As multiple quantum well (MQW) with nominal  $x$  value 0.24, and nominal barrier and well thickness of 15 nm and 22 nm, respectively. Spectra (1) to (4) were measured at locations spaced 0.47 cm apart along a straight line. In each, the peak at 1.42 eV marked  $E_0$  comes from the direct gap of the GaAs substrate, the peak marked "A" near 1.72 eV comes from the direct gap of the Al<sub>x</sub>Ga<sub>1-x</sub>As barriers, and the remaining features marked  $h_n$  and  $h_n$  ( $n = 1, 2, 3, \dots$ ) between 1.43 and 1.68 eV come from light and heavy hole interband transitions characteristic of the MQW energy bands. The Al<sub>x</sub>Ga<sub>1-x</sub>As,  $h_1$ , and  $h_1$  features shift with spatial position. Fits to the data show that the well width ranges from 21.4 nm to 21.0 nm, and  $x$  ranges from 0.225 to 0.247, between positions (1) and (4), 1.4 cm apart. (See Sec. 5.5, Applications Refs., Parayanthal, Shen, Pollak, Glembocki, Shanabrook, and Beard (1986), fig. 1, p. 1261.)

Table 5 presents the sensitivities to typical quantities measured by photoreflectance spectroscopy such as composition, stress, electric field strength, surface photovoltage, and doping density. For more specific details, the reader should refer to the citations given in the table.

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## 6. Photoluminescence

### 6.1 Introduction

Photoluminescence (PL) depends on the fact that electrons residing in the valence band of a semiconductor can be excited via optical absorption to the conduction band, to an impurity, or to a defect level in the energy gap. PL can be used to determine the energy gap of a semiconductor sample. This technique is especially useful for III-V and II-VI ternary alloys like AlGa<sub>1-x</sub>As and ZnCd<sub>1-x</sub>Te, because the energy gap, which varies with the compositional parameter  $x$ , must be accurately known for most applications. When this process is inverted,  $x$  can be found from the gap value and the known relation between gap energy and composition. Photoluminescence also detects the presence of impurities and crystalline defects in semiconductors, which affect materials quality and device performance. Each impurity produces a characteristic feature or set of features in the spectrum. Hence, the impurity type can be identified, and multiple impurities can be detected in a single PL spectrum. In some cases, PL can measure the concentration of impurities. Comparison of PL peak halfwidths from sample to sample gives an indication of impurity concentration, carrier concentration, and crystal perfection.

### 6.2 Physical Basis

Photoluminescence results from radiative relaxation of an optically excited population. In order to cause this excitation, the incoming photon energy

**Table 5.** Photorefectance spectroscopy sensitivity. Given are sensitivities for the measurement of crystallinity,  $x$ ; stress,  $\chi$ ; field strength,  $F_{dc}$ ; surface photovoltage,  $V_F$ ; and doping density,  $N_d$ . The notations used for the measured quantity column are intensity,  $I$ ; energy,  $h\nu$ ; damping,  $\Gamma$ ; bandgap,  $E_g$ ; splitting energy,  $\Delta E_{split}$ ; deformation potential,  $b$ ; compliances,  $S_{11}$  and  $S_{12}$ ; energy of Franz Keldysh oscillation lobe,  $E_m$ ; oscillation number,  $m$ ; energy difference,  $E_2 - E_1$ ; shift of critical point,  $\delta E_{cp}$ ; and spacing of Franz Keldysh oscillations,  $\Delta E_{FKO}$ .  $\Delta V$  is the built-in potential minus the photovoltage of the laser minus the thermal energy

Method	Matrix	Quantity	Measured quantity	Conversion	Sensitivity*	Ref. (see below)
PR	Si	crystallinity	$I, h\nu, \Gamma$	qualitative		1
PR	$\text{In}_x\text{Ga}_{1-x}\text{As}$	$x$	$E_g$	$E_g/\text{eV} = 1.425 - 1.337x + 0.270x^2$	$x = 0$ to 0.15	2
PR	GaAs/Si	stress	$\Delta E_{split}$	$\Delta E_{split} = 2b(S_{11} - S_{12})\chi$	$\chi = (150 \pm 50)$ MPa	3
PR	GaAs/GaAlAs	field strength	$E_m$ vs $m$	$m\pi = 0 + (4/3)[(E_m - E_0)/hO]^{3/2}$	$F_{dc} \sim (2 \text{ to } 4) \times 10^5$ V/cm	4
PR	metal/GaAs	surface photovoltage	$E_m$ vs $m$	$m\pi = 0 + (4/3)[(E_m - E_0)/hO]^{3/2}$	$V_F = (0.73 \pm 0.02)$ V	5
PR	GaAs	doping density	$E_2 - E_1$	$N_d = (\Delta V)N_d = (E_2 - E_1)^3 (3.46 \times 10^{20}) \text{ cm}^{-3}$	$N_d = (1 \times 10^{14} \text{ to } 1 \times 10^{16}) \text{ cm}^{-3}$	6
PR	GaAs	doping density	$\delta E_{cp}$	$\delta E_{cp}/\delta N_d = (5.8 \pm 0.5) \times 10^{-20} \text{ eV cm}^3$	$N_d > 1 \times 10^{16} \text{ cm}^{-3}$	7
PR	GaAs	doping density	$\Delta E_{FKO}$	$\Delta E_{FKO} = \text{const.} \times N_d^{1/3}$	$N_d = (6 \times 10^{17} \text{ to } 3 \times 10^{18}) \text{ cm}^{-3}$	8

\* Values quoted in references below.

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must equal or exceed the energy difference between the initial and final states of the electron. Such an excited electron usually returns to its initial state after a short time. If the excited electron returns to its initial state by radiative means, the process emits a photon whose energy is the difference between the excited and the initial state energies. The spectral distribution of the emitted photons shows an emission peak at the energy (or wavelength) corresponding to each excited level.

Photoluminescence is complicated by the behavior of the electron during its excited period. The excited electron leaves behind it a deficiency in the valence band, a mobile hole. The Coulomb attraction between the excited electron and the hole can bind the two particles into a system called a free exciton, much as a proton and an electron form a bound hydrogen atom. The exciton can move as a unit through the crystal, but carries no current because its net charge is zero. From this perspective, the return of the electron to its initial state can be viewed as the collapse of the temporary excitonic state, when the electron recombines with the hole.

The exciton influences the PL spectrum in several ways. Because it is a bound state, the excited state energy is slightly less than the bandgap energy, generally by a few meV. Hence, for PL near the energy gap, the equation for the energy of the emitted photon is

$$\hbar\omega = E_g - E_{ex}, \quad (17)$$

where  $E_{ex}$  is the binding energy of the excitonic state. This equation applies for a direct energy gap semiconductor. For an indirect gap semiconductor, a phonon must also be involved to properly conserve momentum. Then the equation for the emitted photon energy is ( $E_{ph}$  is the photon energy)

$$\hbar\omega = E_g - E_{ex} - E_{ph}. \quad (18)$$

However, this free exciton recombination dominates only when the sample is very pure. When donor, acceptor, or neutral impurities are present, free excitons respond to the Coulomb fields of these defects to form bound excitons. Each type of exciton produces a PL peak when recombination occurs, and each can be identified in the spectrum.

### 6.3 Experimental and Technical Details

Figure 16 shows the main elements of a standard PL arrangement. Any of several commercially available types of laser may be used, provided that the

energy of the laser's photons exceeds the energy gap of the material, and the laser power is adequate to excite a usable PL signal. An argon ion laser is suitable for many semiconductors of technological interest such as Si (1.12 eV),  $\text{Al}_x\text{Ga}_{1-x}\text{As}$  (1.42 eV to 2.16 eV) and  $\text{Zn}_x\text{Cd}_{1-x}\text{Te}$ . Laser powers  $\leq 50$  mW are usually adequate, but power densities must be minimized to avoid sample heating effects. It is generally possible to avoid heating and still obtain adequate signal to noise by defocusing the laser or reducing the incident laser power.

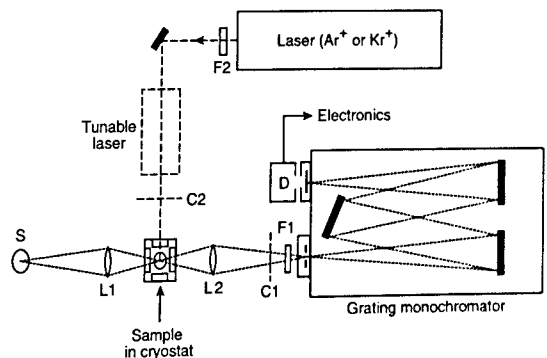


Fig. 16. Schematic diagram of a photoluminescence arrangement, showing the exciting  $\text{Ar}^+$  or  $\text{Kr}^+$  laser, filter F2 to block unwanted laser lines, the sample mounted in a cryostat, lens L2 to bring the PL radiation to the monochromator entrance slit, chopping wheel C1 to modulate the light for lock-in detection, filter F1 to exclude the laser line from the monochromator, the grating monochromator itself, and detector D followed by appropriate electronics to process and analyze the signal. The tunable dye laser and chopping wheel C2 shown in dashed outline are auxiliary equipment for luminescence excitation measurements, a related technique. Lamp S and lens L1 allow auxiliary absorption spectroscopy, using the same monochromator and detector. (See Sec. 6.5, General Refs., Lightowers (1990), fig. 4, p. 138.)

The sample's PL radiation passes through a monochromator and then to a detector, to yield the spectral distribution of intensity versus wavelength or energy. A standard photomultiplier tube is usually employed for visible and near visible applications. Quantum detectors such as germanium and InAs photodiodes are employed for the near infrared. All of these give the best signal-to-noise ratio when cooled to temperatures as low as 77 K for solid-state photodiodes. Improvement in sensitivity comes with the use of an optical multi-channel analyzer such as a Si photodiode array. The array has the advantage of providing complete spectra in a short time.

In spectral regions where signal to noise is detector limited, decided improvements in sensitivity and

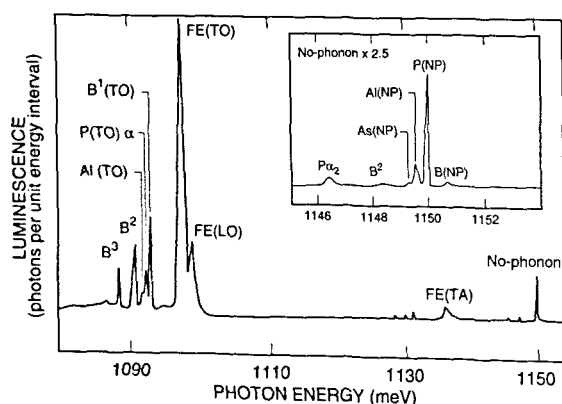
decreases in measurement times come if the grating monochromator in Fig. 16 is replaced by an Michelson interferometer to carry out Fourier transform spectroscopy. This instrument has already been discussed in the section on infrared spectroscopy.

It is usually necessary to cool the sample below room temperature to observe the best PL spectra. Cooling reduces the thermal broadening of the excited carrier spectrum of the order  $k_B T$ , and also reduces the importance of nonradiative de-excitation processes. Cooling to liquid nitrogen temperature is often adequate. The sample can be mounted to a cold finger connected to a liquid nitrogen dewar, and can be held to within a few degrees of 77 K.

When necessary, cooling to liquid helium temperatures can be conveniently obtained by a continuous-flow liquid helium system. With proper shielding and an adequate flow rate of helium (typically 1 L/h to 3 L/h), sample temperatures as low as 6 K to 10 K can be maintained. Temperatures down to  $\sim 10$  K can be reached by mechanical refrigerators. If necessary, temperatures to 4 K can be obtained by immersion in liquid helium or to 2 K by pumped helium methods.

## 6.4 Illustrative Applications

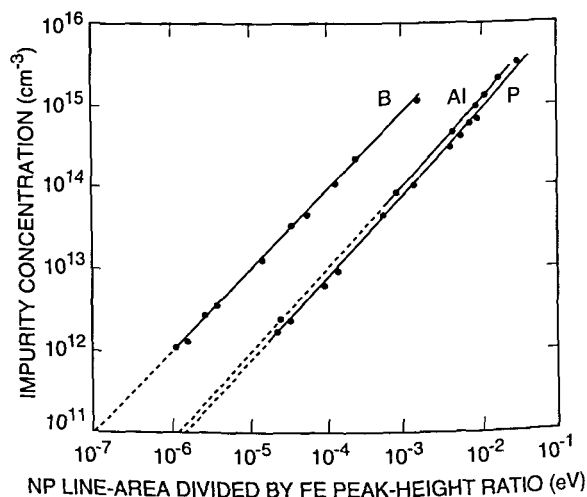
Figure 17 shows how specific impurities in a semiconductor such as silicon clearly appear in PL



**Fig. 17.** PL spectrum of high-resistivity ( $> 20 \text{ k}\Omega \text{ cm}$ ) near-intrinsic silicon showing the presence of the following impurities and their concentrations, in units of  $10^{12} \text{ cm}^{-3}$ : B, 1.36; P, 1.69; Al, 0.61; and As, 0.14. The fingerprint features for each element are marked. Free-exciton lines are marked FE. Because silicon is an indirect-gap semiconductor, phonon modes must be involved in FE transitions. They are indicated as TO (transverse optical), LO (longitudinal optical), and TA (transverse acoustic). Peaks labeled NP (no phonon) come from bound excitons, which do not require phonon assistance. The technique for deriving quantitative impurity concentration data from such spectra is discussed in the caption for Fig. 18. (See Sec. 6.5, General Refs., Lightowers (1990), fig. 9, p. 144.)

spectra. The caption explains the source of each peak. Figure 18 illustrates the conversion of PL data into accurate values for impurity concentrations. Figure 19 shows how two-dimensional PL mapping can help evaluate the homogeneity and quality of a semiconductor wafer, in this case an epitaxial layer of InGaAsP grown on InP. The technique uses the fact that each parameter that describes a PL peak can be related to a sample property. The peak position, for instance, gives the energy gap value, which for an alloy like InGaAsP varies with the proportions of the component elements. Hence, a map of peak PL wavelength correlates well with a map of composition.

Table 6 presents the sensitivities of typical quantities measured by photoluminescence such as composition in III-V and II-VI alloys and the concentration of B, P, As, and Al in Si. The reader should refer to the citations in the table for more specific details.



**Fig. 18.** Calibration chart to convert PL information like that in Fig. 17 into impurity concentration for B, Al, and P in silicon. It is difficult to establish absolute intensity standards for PL, because of differences in laser excitation power and focusing, temperature, and other factors. This chart uses a calibration method which is internal to a given spectrum, and hence avoids many of the problems of absolute calibration, although it was established using careful independent measurements of concentrations, and of temperature and light intensity. The area of the NP peak for the particular impurity is ratioed against the height of the FE(TO) peak in the same spectrum. More recent work has extended the upper limit of the calibration curves to about  $10^{17} \text{ cm}^{-3}$ . (See Sec. 6.5, General Refs., Lightowers (1990), fig. 14, p. 148.)

**Table 6.** Photoluminescence sensitivity. Given are sensitivities for the measurement of substitutional boron, [B<sub>s</sub>]; phosphorus, [P<sub>s</sub>]; arsenic, [As<sub>s</sub>]; and aluminum, [Al<sub>s</sub>], in crystalline Si. Sensitivities for determination of ternary composition,  $x$ , are given for Al <sub>$x$</sub> Ga <sub>$1-x$</sub> As, In <sub>$x$</sub> Ga <sub>$1-x$</sub> As, and Zn <sub>$x$</sub> Cd <sub>$1-x$</sub> Te. The notations used for the measured quantity column are the boron transverse optical b1 multiexciton peak intensity,  $I(\text{B}_{\text{TOB1}})$ ; free exciton intensity,  $I(\text{FE})$ ; phosphorus no-phonon peak intensity,  $I(\text{P}_{\text{NP}})$ ; arsenic no-phonon peak intensity,  $I(\text{As}_{\text{NP}})$ ; aluminum no-phonon peak intensity,  $I(\text{Al}_{\text{NP}})$ ; and energy,  $h\nu$

Method	Matrix	Quantity	Measured quantity	Conversion	Sensitivity <sup>a</sup>	Ref. (see below)
Exciton intensity ratio	Si	[B <sub>s</sub> ]	$I(\text{B}_{\text{TOB1}})/I(\text{FE})$ @4.2 K	$\log[\text{B}_s/\text{cm}^3] = 1.435 \log[I_{\text{B}}/I_{\text{FE}}] + 12.81$	$\pm 2 \times 10^{10} \text{ cm}^{-3}$	1
Exciton intensity ratio	Si	[P <sub>s</sub> ]	$I(\text{P}_{\text{NP}})/I(\text{FE})$ @4.2 K	$\log[\text{P}_s/\text{cm}^3] = 1.280 \log[I_{\text{P}}/I_{\text{FE}}] + 12.79$	$\pm 4 \times 10^{10} \text{ cm}^{-3}$	1
Exciton intensity ratio	Si	[As <sub>s</sub> ]	$I(\text{As}_{\text{NP}})/I(\text{FE})$ @4.2 K	$\log[\text{As}_s/\text{cm}^3] = 1.049 \log[I_{\text{As}}/I_{\text{FE}}] + 12.76$	$\pm 1 \times 10^{11} \text{ cm}^{-3}$	1
Exciton intensity ratio	Si	[Al <sub>s</sub> ]	$I(\text{Al}_{\text{NP}})/I(\text{FE})$ @4.2 K	$\log[\text{Al}_s/\text{cm}^3] = 1.359 \log[I_{\text{Al}}/I_{\text{FE}}] + 13.19$	$\pm 8 \times 10^{10} \text{ cm}^{-3}$	1
Peak energy	Al <sub><math>x</math></sub> Ga <sub><math>1-x</math></sub> As	$x$	$h\nu$ @300 K	$h\nu/\text{eV} = 1.424 + 1.247x$ ( $0 < x < 0.45$ )	$\pm 0.002x$	2
Peak energy	In <sub><math>x</math></sub> Ga <sub><math>1-x</math></sub> As	$x$	$h\nu$ @300 K	$h\nu/\text{eV} = 1.424 - 1.337x + 0.270x^2$	$\pm 0.002x$	3
Peak energy	Zn <sub><math>x</math></sub> Cd <sub><math>1-x</math></sub> Te	$x$	$h\nu$ @4.2 K	$h\nu/\text{eV} = 1.605 + 0.505x + 0.285x^2$	$\pm 0.0002x$	4

<sup>a</sup> Calculated as the concentration-equivalent-of-noise assuming  $\pm 0.02$  signal-to-noise ratio for intensity measurements and  $\pm 2$  meV and  $\pm 0.2$  meV energy precision at room temperature and 4.2 K, respectively.

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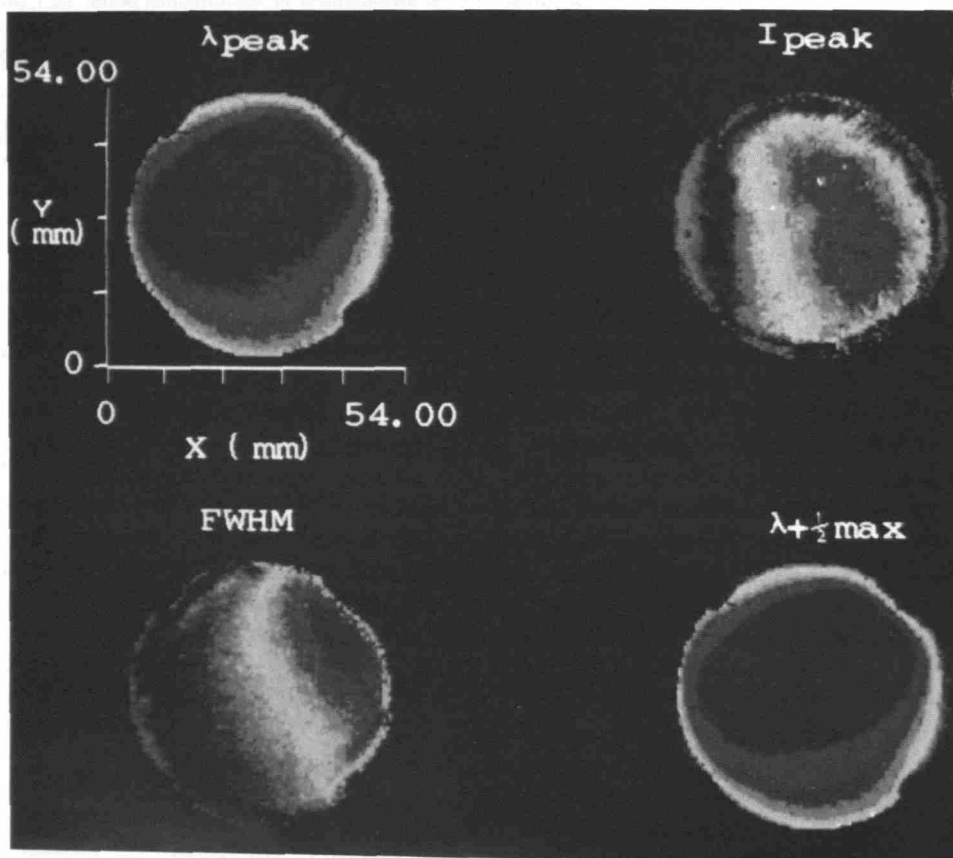


Fig. 19. Two-dimensional maps of PL parameters from a 50 mm wafer of epitaxial InGaAsP grown on InP, obtained using a commercial system with  $x$ - $y$  scanning capability. Upper left, wavelength of the PL peak, which is related to sample composition; upper right, peak intensity, related to defect density; lower left, peak full width at half maximum (FWHM), related to closeness of the lattice match between layer and substrate; lower right, upper wavelength at which PL intensity falls to 50 % of the peak value, related to sample composition. Spatial variations in all the parameters are clearly seen. (See Sec. 6.5, Applications Refs., Hennessy, Miner, and Moore (1990), fig. 3.)

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## 7. Raman Scattering

### 7.1 Introduction

Raman scattering results when photons interact with optical lattice vibrations (phonons) of a semiconductor crystal lattice. The way in which these phonons appear in a Raman spectrum depends on the crystallinity of a sample and on its crystal orientation. Hence, Raman scattering can determine whether a sample is amorphous or crystalline, and whether the crystal is of good quality or is altered by damage or imperfections. The method is also sensitive to strain effects, which change semiconductor lattice structure and hence phonon frequencies. Since phonon frequencies and amplitudes in an alloy semiconductor like  $\text{Al}_x\text{Ga}_{1-x}\text{As}$  change with the degree of alloying, Raman scattering can be used to measure composition as well. By changing the wavelength of the light exciting the scattering, the penetration depth can be changed, which gives the capability to probe layered or inhomogeneous structures.

In microprobe Raman scattering, a microscope is coupled to the Raman system, making it possible to probe regions as small as  $\sim 1 \mu\text{m}$  across. This allows for the identification of contaminating impurities in extremely small regions of the specimen. In resonance Raman scattering, the scattering process is strengthened when the incoming photon energy matches the energy gap or other higher-order critical point energies in the sample's band structure. This resonance strengthens the inherently weak Raman process and also gives band structure information as well as phonon information.

### 7.2 Physical Basis

Raman scattering, a two-photon process, is more complex than one-photon optical processes such as photoluminescence. If light impinges on the surface of a semiconductor, a large portion is reflected, transmitted, absorbed, or elastically scattered (Rayleigh scattering), with no change in frequency. A small part of the light interacts inelastically with phonon modes, so that the outgoing photons have frequencies shifted from the incoming values. These are the Raman-scattered photons. Since the photons can either gain energy or lose energy in their phonon interactions, the scattered light can be of higher frequency (anti-Stokes-shifted) or of lower frequency (Stokes-shifted) than the incident light. Because of statistical considerations, the Stokes modes are stronger and are usually the ones observed in Raman measurements at room temperature.

The up-shifted and down-shifted photons can be treated as side bands of the exciting light that come from the nonlinear interaction between the light and the material. This can be seen by examining the crystal polarization  $P$  due to the phonons, which is given by

$$P = \alpha E \quad (19)$$

where  $E$  is the applied electric field  $E_0 \cos \omega t$  and the polarizability  $\alpha$  is given by

$$\alpha = \alpha_1 u + \alpha_2 u^2 + \alpha_3 u^3 + \dots, \quad (20)$$

where  $u$  is the phonon displacement, and  $\alpha_1, \alpha_2, \dots$  are constants. The first term in Eq. (20) is the dipole approximation, and the other terms represent more complex anharmonic contributions. If the phonon vibrates at frequency  $\Omega$ ,  $u$  is of the form  $u = u_0 \cos(\Omega t)$  and Eq. (19) becomes

$$P = E_0 [\alpha_1 u_0 \cos(\omega t) \cos(\Omega t) + \alpha_2 u_0^2 \cos(\omega t) \cos^2(\Omega t) + \dots] \quad (21)$$

From standard trigonometric identities, Eq. (21) can be rewritten as expressions that contain  $\cos(\omega + \Omega)t$ ,  $\cos(\omega \pm 2\Omega)t$ ,  $\dots$ ,  $\cos(\omega + n\Omega)t$ . The leading term  $\cos(\omega \pm \Omega)t$  represents the fundamental Raman-shifted bands at frequency  $\omega + \Omega$  (so-called anti-Stokes lines) and  $\omega - \Omega$  (Stokes lines), and the others represent the interaction of the photon with multiple phonons ( $n = 2, 3, \dots$ ).

This simple development of the theory gives the shift in photon frequency, that is, where the Raman bands lie relative to the exciting wavelength. However, the intensity and line shape of the Raman bands are more difficult to calculate. Although some appropriate theory exists, it is not easy to apply to specific semiconductors. In general, Raman scattering is a weak process, and the higher order terms in Eq. (20) generally contribute weakly. Beyond these qualitative trends, line-shape analysis of Raman spectra of semiconductors is not well developed. However, it is true that smaller half-widths correlate with higher levels of sample crystalline perfection.

When carried out in detail, the calculation of the Raman intensity depends strongly on the orientation and polarization of the exciting light relative to the crystal axes, since such geometric considerations determine how the field and the polarization interact. Hence, the Raman spectrum from a given crystal depends on its orientation, with various "allowed" and "forbidden" Raman modes for different orientations.

An exception to the statement that Raman scattering is weak occurs in resonant Raman scattering. If the energy of the exciting photon is chosen to match a fundamental feature in the semiconductor band structure, such as the energy gap or higher order critical points in the band structure, the amount of energy imparted to the lattice increases dramatically, and so does the strength of the Raman modes.

### 7.3 Experimental and Technical Details

The overriding consideration in Raman scattering is the weakness of the signal, and the difficulty of separating it from unavoidable accompanying spectral information. Weak Raman peaks usually must be measured in the immediate neighborhood of intense Rayleigh scattering, which occurs at the energy of the exciting photon. Raman measurements require the strongest possible light sources that will not damage the sample, special optical methods to filter out the Rayleigh peak, and sensitive detection schemes to capture the few emerging Raman-shifted photons.

Any monochromatic light source can act as a Raman source. Most often, lasers operating at visible frequencies are employed to provide the necessary power. To give flexibility in varying the penetration depth, and some capability to excite resonance Raman scattering, it is better to use lasers that can be tuned over several powerful lines in the visible. Argon-ion and krypton-ion lasers are good choices; they are powerful, commercially available, and easily tunable, one from the ultraviolet to the green, the other toward the red end of the spectrum. For maximum flexibility in tuning, say for exact resonant coincidence, a tunable dye laser is the best choice. With the range of available dyes, these lasers can be tuned through the energy gaps of most semiconductors. The power is much lower than that of ion lasers but the increased signal due to the resonant effect more than compensates for this.

The optical arrangement for Raman spectroscopy is similar to that for photoluminescence (fig. 16), but with one important exception: a single monochromator is usually inadequate to separate the Raman signal from the strong accompanying Rayleigh light. A double monochromator is standard, consisting of two tandem gratings turning together and sequentially dispersing the light. In recent years, holographic notch filters have matured sufficiently that they can be used to eliminate the Rayleigh signal and allow the use of a single monochromator. Triple monochromators are sometimes used.

Raman scattering excited in the visible or ultraviolet can be detected by visible or ultraviolet detectors, so photomultiplier tubes (PMT) and array detectors work well. The PMTs should be chosen to give broad spectral coverage and to display a low dark count for maximum sensitivity. Cooled operation to reduce dark count is also important. As in photoluminescence work, it is possible to use Fourier methods to enhance Raman sensitivity or to reduce data collection time.

### 7.4 Illustrative Applications

The sensitivity of Raman scattering to phonon modes makes it possible to distinguish between amorphous and crystalline semiconductors. Figure 20 illustrates the direct way in which Raman spectra follow the increasing presence of crystalline silicon, as annealing proceeds on amorphous material.

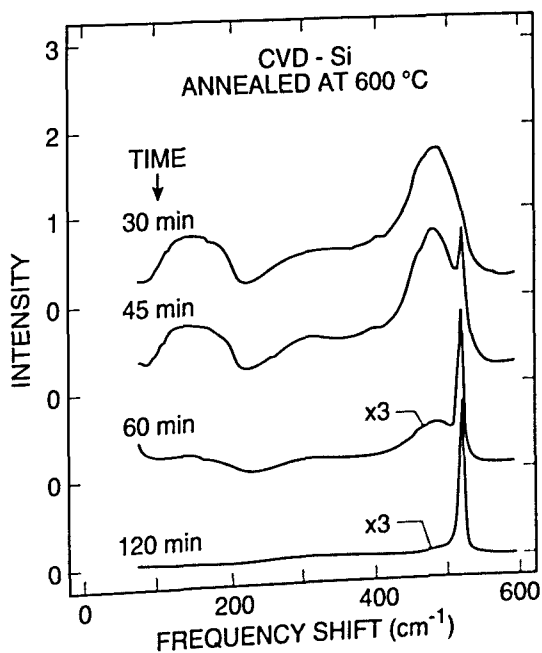
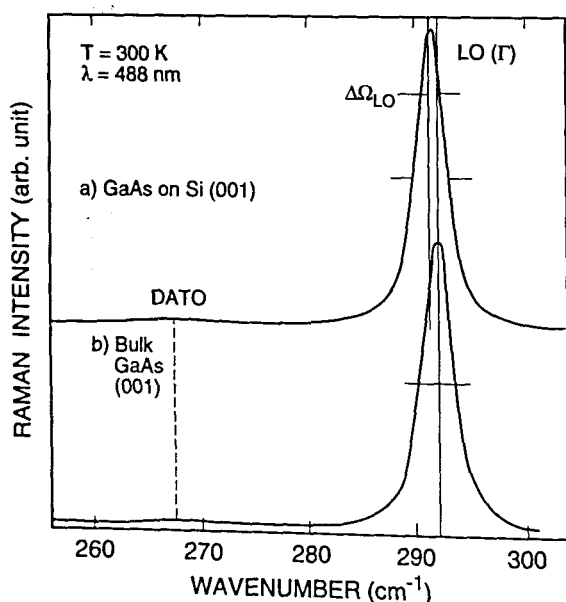


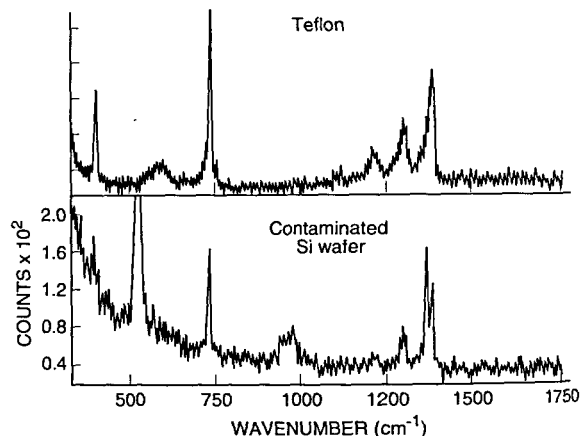
Fig. 20. Raman spectra of silicon grown by chemical vapor deposition, showing change in the character of the silicon after annealing. The top spectrum, taken after 30 min of annealing, is virtually the same as from as-grown material. It shows only broad peaks coming from amorphous silicon. After annealing for 45 min, a sharp line appears at  $520\text{ cm}^{-1}$ , which comes from the optical phonon characteristic of crystalline silicon. The broad structure continues to decrease with annealing time, until after 120 min, the spectrum indicates that little or no amorphous silicon remains. (See Sec. 7.5, General Refs., Nemanich (1986), fig. 1, p. 26.)

Figure 21 shows how strain in a semiconductor appears in a Raman spectrum. The Raman peak for epitaxial GaAs grown on a silicon substrate shifts relative to that for bulk GaAs, because the epilayer lattice spacing changes under the strain induced by the mismatch between film and substrate. Microprobe Raman analysis can be helpful for examining contamination by small particles or for examining thin films, as illustrated in Fig. 22.

Table 7 gives the sensitivities of typical quantities measured by Raman spectroscopy such as stress, impurity concentrations of C and Zn in GaAs, alloy composition, and temperature. For more specific details, the reader should refer to the citations in the table.



**Fig. 21.** Raman spectra of bulk (100) GaAs (lower curve) compared to that from a GaAs film 2  $\mu\text{m}$  thick grown on (100) silicon (upper curve). The main peak near  $292\text{ cm}^{-1}$  comes from the longitudinal optical (LO) phonon. Peak halfwidths are the same in both curves, indicating similar sample quality. The barely visible disorder-activated transverse optical (DATO) peak remains equally small in both spectra, also indicating that there is no significant disorder. However, the peak position for the film is  $0.7\text{ cm}^{-1}$  lower than for the bulk sample, because the epilayer is stressed. Raman methods can easily detect and measure such small changes in peak position. (See Sec. 7.5, Applications Refs., Freundlich, Neu, Leycuras, Carles, and Verie (1988), fig. 1, p. 252.)



**Fig. 22.** Raman microprobe spectrum of a silicon wafer with surface contamination (lower plot) compared to the Raman spectrum of polytetrafluorethylene or teflon (upper plot). The peaks in the lower spectrum at  $520\text{ cm}^{-1}$  and  $950\text{ cm}^{-1}$  are known phonon modes for silicon. The additional peaks arise from the contaminant. They resemble the teflon spectrum and suggest that the contamination came during wafer processing, which included polishing in a slurry containing organic solvents, and etching in a  $\text{CF}_4/\text{H}_2$  plasma. Polymer could have been deposited on the wafer either as teflon from a container holding the slurry, or during the plasma etch. (See Sec. 7.5, Applications Refs., Adar (1986), fig. 2, p. 234.)

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**Table 7.** Raman spectroscopy sensitivity. Given are sensitivities for the measurement of stress;  $\sigma$ ; crystallinity; surface damage; boron 11 concentration,  $[B^{11}]$ ; temperature; composition; substitutional carbon concentration,  $C_s$ ; substitutional zinc concentration,  $Zn_s$ ; built-in potential,  $V_{bi}$ ; and composition,  $x$ . The notations used for the measured quantity column are frequency of the LO phonon,  $\omega_{LO}$ ; frequency of the TO phonon,  $\omega_{TO}$ ; crystallite diameter,  $L$ ; intensity at a given energy,  $I(2000\text{ cm}^{-1})$ ; frequency,  $(\omega)$ , frequency shift,  $\Delta\omega$ ; intensity of the two LO mode,  $I(2LO)$ ; intensity of the TO mode,  $I_{TO}$ ; intensity of the LO mode,  $I_{LO}$  or  $I(LO)$ ; intensity of the L<sup>-</sup> plasmon branch,  $I(L^-)$ ; intensity of the anti-Stokes peak,  $I_{AS}$ ; and intensity of the Stokes peak,  $I_S$

Method	Matrix	Quantity	Measured quantity	Conversion	Sensitivity*	Ref. (see below)
RS	Si	Stress	$\omega_{LO}$	$\sigma = (2.49 \times 10^{10} \text{ Pa}^{-1}) \times \Delta\omega$	$\pm 1 \times 10^7 \text{ Pa}$	1
RS	Si	Crystallinity	$L$ @300 K	Ref. 2		2
RS	Si	Surface damage	$I(2000\text{ cm}^{-1})$	Ref. 3		3
RS	Si	$[B^{11}]$	$I(620\text{ cm}^{-1})$	Ref. 4		4
RS	Si	Temperature	$\omega$ and $\Delta\omega$	Ref. 5		5
RS	$Si_xGe_{1-x}$	$x$	$\omega$	Ref. 6		6
RS	GaAs	Crystallinity	$L$ @300 K	Ref. 7		7
RS	GaAs	Crystallinity	$I(2LO)/I(540)$ @300 K	Ref. 8		8
RS	GaAs	Crystallinity	$I_{TO}/I_{LO}$ @300 K	Ref. 9		9
ERS	GaAs	$C_s, Zn_s$	$I(148\text{ cm}^{-1}),$ $I(174\text{ cm}^{-1})$ 6 K	Ref. 10	$< 1 \times 10^{15} \text{ cm}^{-3}$	10
RS	GaAs	$V_{bi}$	$I(LO)/I(L^-)$	Ref. 11	$\pm 0.2 \text{ V}$	11
RS	$Al_xGa_{1-x}As$	$x$	$\omega_{LO}$	$(\omega_{LO}/2\pi\text{c})/\text{cm}^{-1} =$ $292.4 + 70.8x - 26.8x^2 - 41.13x^3$	$\pm 0.01x$	12
RS	GaAs	Temperature	$\omega_{LO}, \omega_{TO}$	$I_{AS}/I_S$	$\pm 20^\circ\text{C}$	13

\* Calculated as the concentration-equivalent-of-noise or uncertainty in frequency.

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